

# Mathematica 11.3 Integration Test Results

Test results for the 35 problems in "1.1.1.7 P(x) (a+b x)^m (c+d x)^n (e+f x)^p (g+h x)^q.m"

Problem 1: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \frac{(a + b x)^2 (A + B x)}{\sqrt{c + d x} \sqrt{e + f x} \sqrt{g + h x}} dx$$

Optimal (type 4, 700 leaves, 9 steps):

$$\frac{1}{15 d^2 f^2 h^2} 2 b (7 a B d f h + b (5 A d f h - 4 B (d f g + d e h + c f h))) \sqrt{c + d x} \sqrt{e + f x} \sqrt{g + h x} + \frac{2 b B (a + b x) \sqrt{c + d x} \sqrt{e + f x} \sqrt{g + h x}}{5 d f h} +$$

$$\left( 2 \sqrt{-d e + c f} (15 a^2 B d^2 f^2 h^2 + 10 a b d f h (3 A d f h - 2 B (d f g + d e h + c f h))) - \right.$$

$$\left. b^2 (10 A d f h (d f g + d e h + c f h) - B (8 c^2 f^2 h^2 + 7 c d f h (f g + e h) + d^2 (8 f^2 g^2 + 7 e f g h + 8 e^2 h^2))) \right)$$

$$\sqrt{\frac{d (e + f x)}{d e - c f}} \sqrt{g + h x} \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{f} \sqrt{c + d x}}{\sqrt{-d e + c f}}\right], \frac{(d e - c f) h}{f (d g - c h)}\right] \Big/$$

$$\left( 15 d^3 f^{5/2} h^3 \sqrt{e + f x} \sqrt{\frac{d (g + h x)}{d g - c h}} \right) - \frac{1}{15 d^3 f^{5/2} h^3 \sqrt{e + f x} \sqrt{g + h x}}$$

$$2 \sqrt{-d e + c f} (15 a^2 d^2 f^2 h^2 (B g - A h) + 10 a b d f h (3 A d f g h - B (c h (f g - e h) + d g (2 f g + e h)))) -$$

$$\left. b^2 (5 A d f h (c h (f g - e h) + d g (2 f g + e h)) - B (4 c^2 f h^2 (f g - e h) + c d h (3 f^2 g^2 + e f g h - 4 e^2 h^2) + d^2 g (8 f^2 g^2 + 3 e f g h + 4 e^2 h^2))) \right)$$

$$\sqrt{\frac{d (e + f x)}{d e - c f}} \sqrt{\frac{d (g + h x)}{d g - c h}} \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{f} \sqrt{c + d x}}{\sqrt{-d e + c f}}\right], \frac{(d e - c f) h}{f (d g - c h)}\right]$$

Result (type 4, 12443 leaves):

$$\sqrt{c + d x} \sqrt{e + f x} \left( \frac{2 b (-4 b B d f g - 4 b B d e h - 4 b B c f h + 5 A b d f h + 10 a B d f h)}{15 d^2 f^2 h^2} + \frac{2 b^2 B x}{5 d f h} \right)$$

$$\sqrt{g+hx} + \frac{1}{15d^4f^2h^2} \left( \frac{1}{fh \sqrt{e + \frac{(c+dx)(f-\frac{cf}{c+dx})}{d}} \sqrt{g + \frac{(c+dx)(h-\frac{ch}{c+dx})}{d}}} \right.$$

$$2 \left( 8b^2Bd^2f^2g^2 + 7b^2Bd^2efgh + 7b^2Bcdf^2gh - 10Ab^2d^2f^2gh - 20abBd^2f^2gh + \right.$$

$$8b^2Bd^2e^2h^2 + 7b^2Bcdefh^2 - 10Ab^2d^2efh^2 - 20abBd^2efh^2 + 8b^2Bc^2f^2h^2 -$$

$$10Ab^2cdf^2h^2 - 20abBcdf^2h^2 + 30aAbd^2f^2h^2 + 15a^2Bd^2f^2h^2 \left. \right) (c+dx)^{3/2}$$

$$\left( f + \frac{de}{c+dx} - \frac{cf}{c+dx} \right) \left( h + \frac{dg}{c+dx} - \frac{ch}{c+dx} \right) - \frac{1}{fh \sqrt{e + \frac{(c+dx)(f-\frac{cf}{c+dx})}{d}} \sqrt{g + \frac{(c+dx)(h-\frac{ch}{c+dx})}{d}}}$$

$$2(c+dx) \sqrt{\left( f + \frac{de}{c+dx} - \frac{cf}{c+dx} \right) \left( h + \frac{dg}{c+dx} - \frac{ch}{c+dx} \right)}$$

$$\left( \left( 8i b^2 B d^4 e f^2 g^3 h \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \left( \text{EllipticE} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}} \right] \right), \right. \right.$$

$$\left. \left. \frac{f(-dg+ch)}{(-de+cf)h} \right] - \text{EllipticF} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) \right) /$$

$$\left( \sqrt{-\frac{-de+cf}{f}} (-dg+ch) \sqrt{\left( f + \frac{de-cf}{c+dx} \right) \left( h + \frac{dg-ch}{c+dx} \right)} \right) - \left( 8i b^2 B c d^3 \right.$$

$$f^3 g^3 h \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \left( \text{EllipticE} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}} \right] \right), \right.$$

$$\left. \left. \frac{f(-dg+ch)}{(-de+cf)h} \right] - \text{EllipticF} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) \right) /$$

$$\begin{aligned}
 & \left( \sqrt{-\frac{-de+cf}{f}} (-dg+ch) \sqrt{\left(f + \frac{de-cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} \right) + \left( 7 i b^2 B d^4 e^2 \right. \\
 & f g^2 h^2 \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \left( \text{EllipticE}\left[ i \text{ArcSinh}\left[ \frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}} \right], \right. \right. \\
 & \left. \left. \frac{f(-dg+ch)}{(-de+cf)h} \right] - \text{EllipticF}\left[ i \text{ArcSinh}\left[ \frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) \Big/ \\
 & \left( \sqrt{-\frac{-de+cf}{f}} (-dg+ch) \sqrt{\left(f + \frac{de-cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} \right) - \left( 8 i b^2 B c d^3 \right. \\
 & e f^2 g^2 h^2 \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \left( \text{EllipticE}\left[ i \text{ArcSinh}\left[ \frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}} \right], \right. \right. \\
 & \left. \left. \frac{f(-dg+ch)}{(-de+cf)h} \right] - \text{EllipticF}\left[ i \text{ArcSinh}\left[ \frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) \Big/ \\
 & \left( \sqrt{-\frac{-de+cf}{f}} (-dg+ch) \sqrt{\left(f + \frac{de-cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} \right) - \\
 & \left( 10 i A b^2 d^4 e f^2 g^2 h^2 \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \right. \\
 & \left. \left( \text{EllipticE}\left[ i \text{ArcSinh}\left[ \frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] - \right. \right.
 \end{aligned}$$

$$\left. \left( \text{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) \right) /$$

$$\left( \sqrt{-\frac{de+cf}{f}} (-dg+ch) \sqrt{\left(f + \frac{de-cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} \right) -$$

$$\left( 20 i a b B d^4 e f^2 g^2 h^2 \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \right)$$

$$\left( \text{EllipticE} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) -$$

$$\left. \left( \text{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) \right) /$$

$$\left( \sqrt{-\frac{de+cf}{f}} (-dg+ch) \sqrt{\left(f + \frac{de-cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} \right) +$$

$$\left( i b^2 B c^2 d^2 f^3 g^2 h^2 \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \right)$$

$$\left( \text{EllipticE} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) -$$

$$\left. \left( \text{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) \right) /$$

$$\begin{aligned}
 & \left( \sqrt{-\frac{-de+cf}{f}} (-dg+ch) \sqrt{\left(f + \frac{de-cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} \right) + \\
 & \left( 10 i A b^2 c d^3 f^3 g^2 h^2 \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \right. \\
 & \left( \text{EllipticE}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}}\right], \frac{f(-dg+ch)}{(-de+cf)h}\right] - \right. \\
 & \left. \left. \text{EllipticF}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}}\right], \frac{f(-dg+ch)}{(-de+cf)h}\right] \right) \right) / \\
 & \left( \sqrt{-\frac{-de+cf}{f}} (-dg+ch) \sqrt{\left(f + \frac{de-cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} \right) + \\
 & \left( 20 i a b B c d^3 f^3 g^2 h^2 \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \right. \\
 & \left( \text{EllipticE}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}}\right], \frac{f(-dg+ch)}{(-de+cf)h}\right] - \right. \\
 & \left. \left. \text{EllipticF}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}}\right], \frac{f(-dg+ch)}{(-de+cf)h}\right] \right) \right) / \\
 & \left( \sqrt{-\frac{-de+cf}{f}} (-dg+ch) \sqrt{\left(f + \frac{de-cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} \right) +
 \end{aligned}$$

$$\left( 8 i b^2 B d^4 e^3 g h^3 \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \left( \text{EllipticE} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] - \text{EllipticF} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) \right) /$$

$$\left( \sqrt{-\frac{-de+cf}{f}} (-dg+ch) \sqrt{\left(f + \frac{de-cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} \right) -$$

$$\left( 8 i b^2 B c d^3 e^2 f g h^3 \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \right)$$

$$\left( \text{EllipticE} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] - \right)$$

$$\text{EllipticF} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) /$$

$$\left( \sqrt{-\frac{-de+cf}{f}} (-dg+ch) \sqrt{\left(f + \frac{de-cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} \right) -$$

$$\left( 10 i A b^2 d^4 e^2 f g h^3 \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \right)$$

$$\left( \text{EllipticE} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] - \right)$$

$$\left. \left( \text{EllipticF} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) \right) /$$

$$\left( \sqrt{-\frac{de+cf}{f}} (-dg+ch) \sqrt{\left(f + \frac{de- cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} \right) -$$

$$\left( 20 i a b B d^4 e^2 f g h^3 \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \right)$$

$$\left( \text{EllipticE} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) -$$

$$\left. \left( \text{EllipticF} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) \right) /$$

$$\left( \sqrt{-\frac{de+cf}{f}} (-dg+ch) \sqrt{\left(f + \frac{de- cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} \right) +$$

$$\left( i b^2 B c^2 d^2 e f^2 g h^3 \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \right)$$

$$\left( \text{EllipticE} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) -$$

$$\left. \left( \text{EllipticF} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) \right) /$$

$$\begin{aligned}
 & \left( \sqrt{-\frac{-de+cf}{f}} (-dg+ch) \sqrt{\left(f + \frac{de-cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} \right) + \\
 & \left( 10 i A b^2 c d^3 e f^2 g h^3 \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \right. \\
 & \left( \text{EllipticE}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}}\right], \frac{f(-dg+ch)}{(-de+cf)h}\right] - \right. \\
 & \left. \left. \text{EllipticF}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}}\right], \frac{f(-dg+ch)}{(-de+cf)h}\right] \right) \right) / \\
 & \left( \sqrt{-\frac{-de+cf}{f}} (-dg+ch) \sqrt{\left(f + \frac{de-cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} \right) + \\
 & \left( 20 i a b B c d^3 e f^2 g h^3 \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \right. \\
 & \left( \text{EllipticE}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}}\right], \frac{f(-dg+ch)}{(-de+cf)h}\right] - \right. \\
 & \left. \left. \text{EllipticF}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}}\right], \frac{f(-dg+ch)}{(-de+cf)h}\right] \right) \right) / \\
 & \left( \sqrt{-\frac{-de+cf}{f}} (-dg+ch) \sqrt{\left(f + \frac{de-cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} \right) +
 \end{aligned}$$

$$\left( 30 i a A b d^4 e f^2 g h^3 \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \right.$$

$$\left( \text{EllipticE} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] - \right.$$

$$\left. \left. \text{EllipticF} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) \right) /$$

$$\left( \sqrt{-\frac{-de+cf}{f}} (-dg+ch) \sqrt{\left(f + \frac{de-cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} \right) +$$

$$\left( 15 i a^2 B d^4 e f^2 g h^3 \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \right.$$

$$\left( \text{EllipticE} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] - \right.$$

$$\left. \left. \text{EllipticF} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) \right) /$$

$$\left( \sqrt{-\frac{-de+cf}{f}} (-dg+ch) \sqrt{\left(f + \frac{de-cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} \right) -$$

$$\left( i b^2 B c^3 d f^3 g h^3 \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \left( \text{EllipticE} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}} \right], \right. \right. \right.$$

$$\left. \left. \left. \frac{f(-dg+ch)}{(-de+cf)h} \right] - \text{EllipticF}\left[\text{i ArcSinh}\left[\frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}}\right], \frac{f(-dg+ch)}{(-de+cf)h}\right] \right) \right) /$$

$$\left( \sqrt{-\frac{-de+cf}{f}} (-dg+ch) \sqrt{\left(f + \frac{de-cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} \right) -$$

$$\left( 30 \text{i a B c d}^3 f^3 g h^3 \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \right)$$

$$\left( \text{EllipticE}\left[\text{i ArcSinh}\left[\frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}}\right], \frac{f(-dg+ch)}{(-de+cf)h}\right] - \right.$$

$$\left. \left. \left. \text{EllipticF}\left[\text{i ArcSinh}\left[\frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}}\right], \frac{f(-dg+ch)}{(-de+cf)h}\right] \right) \right) \right) /$$

$$\left( \sqrt{-\frac{-de+cf}{f}} (-dg+ch) \sqrt{\left(f + \frac{de-cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} \right) -$$

$$\left( 15 \text{i a}^2 \text{B c d}^3 f^3 g h^3 \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \right)$$

$$\left( \text{EllipticE}\left[\text{i ArcSinh}\left[\frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}}\right], \frac{f(-dg+ch)}{(-de+cf)h}\right] - \right.$$

$$\left. \left. \left. \text{EllipticF}\left[\text{i ArcSinh}\left[\frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}}\right], \frac{f(-dg+ch)}{(-de+cf)h}\right] \right) \right) \right) /$$

$$\begin{aligned}
 & \left( \sqrt{-\frac{-de+cf}{f}} (-dg+ch) \sqrt{\left(f + \frac{de-cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} \right) - \\
 & \left( 8 i b^2 B c d^3 e^3 h^4 \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \left( \text{EllipticE}\left[ i \text{ArcSinh}\left[ \frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}} \right], \right. \right. \right. \\
 & \left. \left. \left. \frac{f(-dg+ch)}{(-de+cf)h} \right] - \text{EllipticF}\left[ i \text{ArcSinh}\left[ \frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) \right) / \\
 & \left( \sqrt{-\frac{-de+cf}{f}} (-dg+ch) \sqrt{\left(f + \frac{de-cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} \right) + \\
 & \left( i b^2 B c^2 d^2 e^2 f h^4 \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \left( \text{EllipticE}\left[ i \text{ArcSinh}\left[ \frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}} \right], \right. \right. \right. \\
 & \left. \left. \left. \frac{f(-dg+ch)}{(-de+cf)h} \right] - \text{EllipticF}\left[ i \text{ArcSinh}\left[ \frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) \right) / \\
 & \left( \sqrt{-\frac{-de+cf}{f}} (-dg+ch) \sqrt{\left(f + \frac{de-cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} \right) + \\
 & \left( 10 i A b^2 c d^3 e^2 f h^4 \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \right. \\
 & \left. \left( \text{EllipticE}\left[ i \text{ArcSinh}\left[ \frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] - \right. \right.
 \end{aligned}$$

$$\left. \left( \text{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) \right/$$

$$\left( \sqrt{-\frac{de+cf}{f}} (-dg+ch) \sqrt{\left(f + \frac{de-cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} \right) +$$

$$\left( 20 i a b B c d^3 e^2 f h^4 \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \right.$$

$$\left. \left( \text{EllipticE} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] - \right. \right.$$

$$\left. \left. \text{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) \right/$$

$$\left( \sqrt{-\frac{de+cf}{f}} (-dg+ch) \sqrt{\left(f + \frac{de-cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} \right) -$$

$$\left( i b^2 B c^3 d e f^2 h^4 \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \left( \text{EllipticE} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \right. \right. \right.$$

$$\left. \left. \left. \frac{f(-dg+ch)}{(-de+cf)h} \right] - \text{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) \right) \right/$$

$$\left( \sqrt{-\frac{de+cf}{f}} (-dg+ch) \sqrt{\left(f + \frac{de-cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} \right) -$$

$$\left( 30 i a A b c d^3 e f^2 h^4 \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \right.$$

$$\left( \text{EllipticE}\left[ i \text{ArcSinh}\left[ \frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] - \right.$$

$$\left. \left. \text{EllipticF}\left[ i \text{ArcSinh}\left[ \frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) \right) /$$

$$\left( \sqrt{-\frac{-de+cf}{f}} (-dg+ch) \sqrt{\left(f + \frac{de-cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} \right) -$$

$$\left( 15 i a^2 B c d^3 e f^2 h^4 \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \right.$$

$$\left( \text{EllipticE}\left[ i \text{ArcSinh}\left[ \frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] - \right.$$

$$\left. \left. \text{EllipticF}\left[ i \text{ArcSinh}\left[ \frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) \right) /$$

$$\left( \sqrt{-\frac{-de+cf}{f}} (-dg+ch) \sqrt{\left(f + \frac{de-cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} \right) +$$

$$\left( 8 i b^2 B c^4 f^3 h^4 \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \left( \text{EllipticE}\left[ i \text{ArcSinh}\left[ \frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}} \right], \right. \right. \right.$$

$$\left. \left( \frac{f(-dg+ch)}{(-de+cf)h} \right) - \text{EllipticF} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) /$$

$$\left( \sqrt{-\frac{de+cf}{f}} (-dg+ch) \sqrt{\left(f + \frac{de-cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} \right) -$$

$$\left( 10 i A b^2 c^3 d f^3 h^4 \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \right)$$

$$\left( \text{EllipticE} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] - \right.$$

$$\left. \text{EllipticF} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) /$$

$$\left( \sqrt{-\frac{de+cf}{f}} (-dg+ch) \sqrt{\left(f + \frac{de-cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} \right) -$$

$$\left( 20 i a b B c^3 d f^3 h^4 \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \right)$$

$$\left( \text{EllipticE} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] - \right.$$

$$\left. \text{EllipticF} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) /$$

$$\begin{aligned}
 & \left( \sqrt{-\frac{-de+cf}{f}} (-dg+ch) \sqrt{\left(f+\frac{de-cf}{c+dx}\right) \left(h+\frac{dg-ch}{c+dx}\right)} \right) + \\
 & \left( 30 i a A b c^2 d^2 f^3 h^4 \sqrt{1-\frac{-de+cf}{f(c+dx)}} \sqrt{1-\frac{-dg+ch}{h(c+dx)}} \right. \\
 & \left( \text{EllipticE}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}}\right], \frac{f(-dg+ch)}{(-de+cf)h}\right] - \right. \\
 & \left. \left. \text{EllipticF}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}}\right], \frac{f(-dg+ch)}{(-de+cf)h}\right] \right) \right) / \\
 & \left( \sqrt{-\frac{-de+cf}{f}} (-dg+ch) \sqrt{\left(f+\frac{de-cf}{c+dx}\right) \left(h+\frac{dg-ch}{c+dx}\right)} \right) + \\
 & \left( 15 i a^2 B c^2 d^2 f^3 h^4 \sqrt{1-\frac{-de+cf}{f(c+dx)}} \sqrt{1-\frac{-dg+ch}{h(c+dx)}} \right. \\
 & \left( \text{EllipticE}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}}\right], \frac{f(-dg+ch)}{(-de+cf)h}\right] - \right. \\
 & \left. \left. \text{EllipticF}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}}\right], \frac{f(-dg+ch)}{(-de+cf)h}\right] \right) \right) / \\
 & \left( \sqrt{-\frac{-de+cf}{f}} (-dg+ch) \sqrt{\left(f+\frac{de-cf}{c+dx}\right) \left(h+\frac{dg-ch}{c+dx}\right)} \right) -
 \end{aligned}$$

$$\left( 4 i b^2 B d^3 e f^2 g^2 h \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \right. \\ \left. \text{EllipticF}\left[ i \text{ArcSinh}\left[ \frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) /$$

$$\left( \sqrt{-\frac{-de+cf}{f}} \sqrt{\left( f + \frac{de-cf}{c+dx} \right) \left( h + \frac{dg-ch}{c+dx} \right)} \right) +$$

$$\left( 4 i b^2 B c d^2 f^3 g^2 h \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \right. \\ \left. \text{EllipticF}\left[ i \text{ArcSinh}\left[ \frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) /$$

$$\left( \sqrt{-\frac{-de+cf}{f}} \sqrt{\left( f + \frac{de-cf}{c+dx} \right) \left( h + \frac{dg-ch}{c+dx} \right)} \right) -$$

$$\left( 4 i b^2 B d^3 e^2 f g h^2 \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \right. \\ \left. \text{EllipticF}\left[ i \text{ArcSinh}\left[ \frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) /$$

$$\left( \sqrt{-\frac{-de+cf}{f}} \sqrt{\left( f + \frac{de-cf}{c+dx} \right) \left( h + \frac{dg-ch}{c+dx} \right)} \right) +$$

$$\left( i b^2 B c d^2 e f^2 g h^2 \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \right. \\ \left. \text{EllipticF}\left[ i \text{ArcSinh}\left[ \frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) /$$

$$\left( \sqrt{-\frac{-de+cf}{f}} \sqrt{\left( f + \frac{de-cf}{c+dx} \right) \left( h + \frac{dg-ch}{c+dx} \right)} \right) +$$

$$\left( 5 i A b^2 d^3 e f^2 g h^2 \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \right. \\ \left. \text{EllipticF}\left[ i \text{ArcSinh}\left[ \frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) /$$

$$\left( \sqrt{-\frac{-de+cf}{f}} \sqrt{\left( f + \frac{de-cf}{c+dx} \right) \left( h + \frac{dg-ch}{c+dx} \right)} \right) +$$

$$\left( 10 i a b B d^3 e f^2 g h^2 \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \right. \\ \left. \text{EllipticF}\left[ i \text{ArcSinh}\left[ \frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) /$$

$$\left( \sqrt{-\frac{-de+cf}{f}} \sqrt{\left( f + \frac{de-cf}{c+dx} \right) \left( h + \frac{dg-ch}{c+dx} \right)} \right) +$$

$$\left( 3 \, i \, b^2 \, B \, c^2 \, d \, f^3 \, g \, h^2 \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \right. \\ \left. \text{EllipticF}\left[ i \, \text{ArcSinh}\left[ \frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) /$$

$$\left( \sqrt{-\frac{-de+cf}{f}} \sqrt{\left(f + \frac{de-cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} \right) -$$

$$\left( 5 \, i \, A \, b^2 \, c \, d^2 \, f^3 \, g \, h^2 \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \right. \\ \left. \text{EllipticF}\left[ i \, \text{ArcSinh}\left[ \frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) /$$

$$\left( \sqrt{-\frac{-de+cf}{f}} \sqrt{\left(f + \frac{de-cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} \right) -$$

$$\left( 10 \, i \, a \, b \, B \, c \, d^2 \, f^3 \, g \, h^2 \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \right. \\ \left. \text{EllipticF}\left[ i \, \text{ArcSinh}\left[ \frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) /$$

$$\left( \sqrt{-\frac{-de+cf}{f}} \sqrt{\left(f + \frac{de-cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} \right) +$$

$$\left( 4 \, i \, b^2 \, B \, c \, d^2 \, e^2 \, f \, h^3 \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \right. \\ \left. \text{EllipticF} \left[ i \, \text{ArcSinh} \left[ \frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) /$$

$$\left( \sqrt{-\frac{-de+cf}{f}} \sqrt{\left( f + \frac{de-cf}{c+dx} \right) \left( h + \frac{dg-ch}{c+dx} \right)} \right) +$$

$$\left( 3 \, i \, b^2 \, B \, c^2 \, d \, e \, f^2 \, h^3 \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \right. \\ \left. \text{EllipticF} \left[ i \, \text{ArcSinh} \left[ \frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) /$$

$$\left( \sqrt{-\frac{-de+cf}{f}} \sqrt{\left( f + \frac{de-cf}{c+dx} \right) \left( h + \frac{dg-ch}{c+dx} \right)} \right) -$$

$$\left( 5 \, i \, A \, b^2 \, c \, d^2 \, e \, f^2 \, h^3 \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \right. \\ \left. \text{EllipticF} \left[ i \, \text{ArcSinh} \left[ \frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) /$$

$$\left( \sqrt{-\frac{-de+cf}{f}} \sqrt{\left( f + \frac{de-cf}{c+dx} \right) \left( h + \frac{dg-ch}{c+dx} \right)} \right) -$$

$$\left( 10 i a b B c d^2 e f^2 h^3 \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \right. \\ \left. \text{EllipticF}\left[ i \text{ArcSinh}\left[ \frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) /$$

$$\left( \sqrt{-\frac{-de+cf}{f}} \sqrt{\left( f + \frac{de-cf}{c+dx} \right) \left( h + \frac{dg-ch}{c+dx} \right)} \right) + \left( 8 i b^2 B c^3 f^3 h^3 \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \right. \\ \left. \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \text{EllipticF}\left[ i \text{ArcSinh}\left[ \frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) /$$

$$\left( \sqrt{-\frac{-de+cf}{f}} \sqrt{\left( f + \frac{de-cf}{c+dx} \right) \left( h + \frac{dg-ch}{c+dx} \right)} \right) - \left( 10 i A b^2 c^2 d f^3 h^3 \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \right. \\ \left. \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \text{EllipticF}\left[ i \text{ArcSinh}\left[ \frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) /$$

$$\left( \sqrt{-\frac{-de+cf}{f}} \sqrt{\left( f + \frac{de-cf}{c+dx} \right) \left( h + \frac{dg-ch}{c+dx} \right)} \right) - \left( 20 i a b B c^2 d f^3 h^3 \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \right. \\ \left. \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \text{EllipticF}\left[ i \text{ArcSinh}\left[ \frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) /$$

$$\left( \sqrt{-\frac{-de+cf}{f}} \sqrt{\left( f + \frac{de-cf}{c+dx} \right) \left( h + \frac{dg-ch}{c+dx} \right)} \right) +$$

$$\left( 30 i a A b c d^2 f^3 h^3 \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \right.$$

$$\left. \text{EllipticF}\left[ i \text{ArcSinh}\left[ \frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) /$$

$$\left( \sqrt{-\frac{-de+cf}{f}} \sqrt{\left(f + \frac{de-cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} \right) +$$

$$\left( 15 i a^2 B c d^2 f^3 h^3 \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \right.$$

$$\left. \text{EllipticF}\left[ i \text{ArcSinh}\left[ \frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) /$$

$$\left( \sqrt{-\frac{-de+cf}{f}} \sqrt{\left(f + \frac{de-cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} \right) -$$

$$\left( 15 i a^2 A d^3 f^3 h^3 \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \text{EllipticF}\left[ i \text{ArcSinh}\left[ \frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}} \right], \right. \right.$$

$$\left. \left. \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) / \left( \sqrt{-\frac{-de+cf}{f}} \sqrt{\left(f + \frac{de-cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} \right)$$

**Problem 2: Result unnecessarily involves imaginary or complex numbers.**

$$\int \frac{(a+bx)(A+Bx)}{\sqrt{c+dx}\sqrt{e+fx}\sqrt{g+hx}} dx$$

Optimal (type 4, 405 leaves, 8 steps):

$$\frac{2 b B \sqrt{c+d x} \sqrt{e+f x} \sqrt{g+h x}}{3 d f h} + \left( 2 \sqrt{-d e+c f} (3 a B d f h+b (3 A d f h-2 B (d f g+d e h+c f h))) \sqrt{\frac{d (e+f x)}{d e-c f}} \sqrt{g+h x} \right. \\ \left. \text{EllipticE}\left[\text{ArcSin}\left[\frac{\sqrt{f} \sqrt{c+d x}}{\sqrt{-d e+c f}}\right], \frac{(d e-c f) h}{f (d g-c h)}\right] \right) / \left( 3 d^2 f^{3/2} h^2 \sqrt{e+f x} \sqrt{\frac{d (g+h x)}{d g-c h}} \right) - \\ \left( 2 \sqrt{-d e+c f} (3 a d f h (B g-A h)+b (3 A d f g h-B (c h (f g-e h)+d g (2 f g+e h)))) \right. \\ \left. \sqrt{\frac{d (e+f x)}{d e-c f}} \sqrt{\frac{d (g+h x)}{d g-c h}} \text{EllipticF}\left[\text{ArcSin}\left[\frac{\sqrt{f} \sqrt{c+d x}}{\sqrt{-d e+c f}}\right], \frac{(d e-c f) h}{f (d g-c h)}\right] \right) / \\ \left( 3 d^2 f^{3/2} h^2 \sqrt{e+f x} \sqrt{g+h x} \right)$$

Result (type 4, 450 leaves):

$$\frac{1}{3 d^3 f^2 h^2 \sqrt{e+f x} \sqrt{g+h x}} \sqrt{c+d x} \left( 2 b B d^2 f h (e+f x) (g+h x) - \frac{1}{c+d x} \right. \\ \left. 2 d^2 (-3 A b d f h-3 a B d f h+2 b B (d f g+d e h+c f h)) (e+f x) (g+h x) + \frac{1}{\sqrt{-c+\frac{d e}{f}}} \right. \\ \left. 2 i (d e-c f) h (3 A b d f h+3 a B d f h-2 b B (d f g+d e h+c f h)) \sqrt{c+d x} \sqrt{\frac{d (e+f x)}{f (c+d x)}} \right. \\ \left. \sqrt{\frac{d (g+h x)}{h (c+d x)}} \text{EllipticE}\left[i \text{ArcSinh}\left[\frac{\sqrt{-c+\frac{d e}{f}}}{\sqrt{c+d x}}\right], \frac{d f g-c f h}{d e h-c f h}\right] + \frac{1}{\sqrt{-c+\frac{d e}{f}}} \right. \\ \left. 2 i d h (3 a d f (-B e+A f) h+b (-3 A d e f h+B c f (-f g+e h)+B d e (f g+2 e h))) \right. \\ \left. \sqrt{c+d x} \sqrt{\frac{d (e+f x)}{f (c+d x)}} \sqrt{\frac{d (g+h x)}{h (c+d x)}} \text{EllipticF}\left[i \text{ArcSinh}\left[\frac{\sqrt{-c+\frac{d e}{f}}}{\sqrt{c+d x}}\right], \frac{d f g-c f h}{d e h-c f h}\right] \right)$$

**Problem 3: Result unnecessarily involves imaginary or complex numbers.**

$$\int \frac{A + Bx}{\sqrt{c+dx} \sqrt{e+fx} \sqrt{g+hx}} dx$$

Optimal (type 4, 284 leaves, 6 steps):

$$\left( 2B\sqrt{-de+cf} \sqrt{\frac{d(e+fx)}{de-cf}} \sqrt{g+hx} \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{f}\sqrt{c+dx}}{\sqrt{-de+cf}}\right], \frac{(de-cf)h}{f(dg-ch)}\right] \right) /$$

$$\left( d\sqrt{f}h\sqrt{e+fx} \sqrt{\frac{d(g+hx)}{dg-ch}} \right) - \left( 2\sqrt{-de+cf} (Bg-Ah) \sqrt{\frac{d(e+fx)}{de-cf}} \sqrt{\frac{d(g+hx)}{dg-ch}} \right.$$

$$\left. \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{f}\sqrt{c+dx}}{\sqrt{-de+cf}}\right], \frac{(de-cf)h}{f(dg-ch)}\right] \right) / (d\sqrt{f}h\sqrt{e+fx}\sqrt{g+hx})$$

Result (type 4, 319 leaves):

$$- \left( \left( 2 \left( -Bd^2 \sqrt{-c + \frac{de}{f}} (e+fx)(g+hx) - iB(de-cf)h(c+dx)^{3/2} \sqrt{\frac{d(e+fx)}{f(c+dx)}} \sqrt{\frac{d(g+hx)}{h(c+dx)}} \right. \right. \right.$$

$$\left. \left. \operatorname{EllipticE}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{-c + \frac{de}{f}}}{\sqrt{c+dx}}\right], \frac{dfg-afh}{deh-afh}\right] + i d (Be - Af) h (c+dx)^{3/2} \right. \right.$$

$$\left. \left. \sqrt{\frac{d(e+fx)}{f(c+dx)}} \sqrt{\frac{d(g+hx)}{h(c+dx)}} \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{-c + \frac{de}{f}}}{\sqrt{c+dx}}\right], \frac{dfg-afh}{deh-afh}\right] \right) \right) /$$

$$\left( d^2 \sqrt{-c + \frac{de}{f}} fh \sqrt{c+dx} \sqrt{e+fx} \sqrt{g+hx} \right)$$

**Problem 4: Result unnecessarily involves imaginary or complex numbers.**

$$\int \frac{A + Bx}{(a+bx) \sqrt{c+dx} \sqrt{e+fx} \sqrt{g+hx}} dx$$

Optimal (type 4, 313 leaves, 9 steps):

$$\left( 2B \sqrt{-de+cf} \sqrt{\frac{d(e+fx)}{de-cf}} \sqrt{\frac{d(g+hx)}{dg-ch}} \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{f}\sqrt{c+dx}}{\sqrt{-de+cf}}\right], \frac{(de-cf)h}{f(dg-ch)}\right] \right) /$$

$$\left( bd\sqrt{f}\sqrt{e+fx}\sqrt{g+hx} \right) -$$

$$\left( 2\left(A - \frac{aB}{b}\right) \sqrt{-de+cf} \sqrt{\frac{d(e+fx)}{de-cf}} \sqrt{\frac{d(g+hx)}{dg-ch}} \operatorname{EllipticPi}\left[-\frac{b(de-cf)}{(bc-ad)f}, \right.$$

$$\left. \operatorname{ArcSin}\left[\frac{\sqrt{f}\sqrt{c+dx}}{\sqrt{-de+cf}}\right], \frac{(de-cf)h}{f(dg-ch)}\right] \right) / \left( (bc-ad)\sqrt{f}\sqrt{e+fx}\sqrt{g+hx} \right)$$

Result (type 4, 244 leaves):

$$\left( 2i\sqrt{e+fx} \sqrt{\frac{d(g+hx)}{h(c+dx)}} \left( b(-Bc+Ad) \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{-c+\frac{de}{f}}}{\sqrt{c+dx}}\right], \frac{dfg-afh}{deh-afh}\right] + \right.$$

$$\left. (-Ab+aB)d \operatorname{EllipticPi}\left[\frac{(bc-ad)f}{b(-de+cf)}, i \operatorname{ArcSinh}\left[\frac{\sqrt{-c+\frac{de}{f}}}{\sqrt{c+dx}}\right], \frac{dfg-afh}{deh-afh}\right] \right) \right) /$$

$$\left( b(-bc+ad) \sqrt{-c+\frac{de}{f}} f \sqrt{\frac{d(e+fx)}{f(c+dx)}} \sqrt{g+hx} \right)$$

**Problem 5: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{A+Bx}{(a+bx)^2 \sqrt{c+dx} \sqrt{e+fx} \sqrt{g+hx}} dx$$

Optimal (type 4, 678 leaves, 12 steps):

$$\begin{aligned}
 & - \frac{b (A b - a B) \sqrt{c+d x} \sqrt{e+f x} \sqrt{g+h x}}{(b c - a d) (b e - a f) (b g - a h) (a + b x)} + \left( (A b - a B) \sqrt{f} \sqrt{-d e + c f} \right. \\
 & \quad \left. \sqrt{\frac{d (e+f x)}{d e - c f}} \sqrt{g+h x} \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{f} \sqrt{c+d x}}{\sqrt{-d e + c f}}\right], \frac{(d e - c f) h}{f (d g - c h)}\right] \right) / \\
 & \quad \left( (b c - a d) (b e - a f) (b g - a h) \sqrt{e+f x} \sqrt{\frac{d (g+h x)}{d g - c h}} \right) - \\
 & \quad \left( (A b - a B) \sqrt{f} \sqrt{-d e + c f} \sqrt{\frac{d (e+f x)}{d e - c f}} \sqrt{\frac{d (g+h x)}{d g - c h}} \right. \\
 & \quad \left. \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{f} \sqrt{c+d x}}{\sqrt{-d e + c f}}\right], \frac{(d e - c f) h}{f (d g - c h)}\right] \right) / \\
 & \quad (b (b c - a d) (b e - a f) \sqrt{e+f x} \sqrt{g+h x}) + \\
 & \quad \left( \sqrt{-d e + c f} (3 a^2 A b d f h - a^3 B d f h - b^3 (2 B c e g - A (d e g + c f g + c e h))) + \right. \\
 & \quad \left. a b^2 (B (d e g + c f g + c e h) - 2 A (d f g + d e h + c f h)) \right) \sqrt{\frac{d (e+f x)}{d e - c f}} \\
 & \quad \left( \sqrt{\frac{d (g+h x)}{d g - c h}} \operatorname{EllipticPi}\left[-\frac{b (d e - c f)}{(b c - a d) f}, \operatorname{ArcSin}\left[\frac{\sqrt{f} \sqrt{c+d x}}{\sqrt{-d e + c f}}\right], \frac{(d e - c f) h}{f (d g - c h)}\right] \right) / \\
 & \quad (b (b c - a d)^2 \sqrt{f} (b e - a f) (b g - a h) \sqrt{e+f x} \sqrt{g+h x})
 \end{aligned}$$

Result(type 4, 14516 leaves):

$$\begin{aligned}
 & - \frac{b (A b - a B) \sqrt{c+d x} \sqrt{e+f x} \sqrt{g+h x}}{(b c - a d) (b e - a f) (b g - a h) (a + b x)} - \\
 & \quad \frac{1}{d (-b c + a d) (-b e + a f) (-b g + a h)} \left( \frac{(A b - a B) (c+d x)^{3/2} \left( f + \frac{d e}{c+d x} - \frac{c f}{c+d x} \right) \left( h + \frac{d g}{c+d x} - \frac{c h}{c+d x} \right)}{\sqrt{e + \frac{(c+d x) \left( f - \frac{c f}{c+d x} \right)}{d}} \sqrt{g + \frac{(c+d x) \left( h - \frac{c h}{c+d x} \right)}{d}}} \right) + \\
 & \quad \left( (c+d x) \left( -b + \frac{b c}{c+d x} - \frac{a d}{c+d x} \right) \sqrt{f + \frac{d e}{c+d x} - \frac{c f}{c+d x}} \sqrt{h + \frac{d g}{c+d x} - \frac{c h}{c+d x}} \right)
 \end{aligned}$$

$$\sqrt{\left( fh + \frac{d^2 eg}{(c+dx)^2} - \frac{cdfg}{(c+dx)^2} - \frac{cdeh}{(c+dx)^2} + \frac{c^2 fh}{(c+dx)^2} + \frac{dfg}{c+dx} + \frac{deh}{c+dx} - \frac{2cfh}{c+dx} \right)}$$

$$\left( (bc - ad) h (-2bBeg + Abfg + aBfg + Abeh + aBeh - 2Afh) \right) /$$

$$\left( (-bg + ah) \sqrt{f + \frac{de}{c+dx} - \frac{cf}{c+dx}} \sqrt{h + \frac{dg}{c+dx} - \frac{ch}{c+dx}} - \frac{(Ab - aB)(de - cf) \sqrt{h + \frac{dg}{c+dx} - \frac{ch}{c+dx}}}{\sqrt{f + \frac{de}{c+dx} - \frac{cf}{c+dx}}} + \right.$$

$$\left. \left( 2b^3 Bceg - Ab^3 deg - ab^2 Bdeg - Ab^3 cfg - ab^2 Bcfg + 2aAb^2 dfg - Ab^3 ceh - ab^2 Bceh + 2aAb^2 deh + 2aAb^2 cfh - 3a^2 Abd fh + a^3 Bdfh \right) \sqrt{h + \frac{dg}{c+dx} - \frac{ch}{c+dx}} / \left( (-bg + ah) \left( b - \frac{bc}{c+dx} + \frac{ad}{c+dx} \right) \sqrt{f + \frac{de}{c+dx} - \frac{cf}{c+dx}} \right) \right)$$

$$\left( \left( iAbd^2 efg \sqrt{1 - \frac{-de + cf}{f(c+dx)}} \sqrt{1 - \frac{-dg + ch}{h(c+dx)}} \left( \text{EllipticE} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{-dg + ch}{h}}}{\sqrt{c+dx}} \right], \right. \right. \right. \right.$$

$$\left. \left. \left. \frac{(-de + cf)h}{f(-dg + ch)} \right] - \text{EllipticF} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{-dg + ch}{h}}}{\sqrt{c+dx}} \right], \frac{(-de + cf)h}{f(-dg + ch)} \right] \right) \right) /$$

$$\left( (bc - ad)(-de + cf) \sqrt{-\frac{-dg + ch}{h}} \sqrt{\left( fh + \frac{d^2 eg - cdfg - cdeh + c^2 fh}{(c+dx)^2} + \frac{dfg + deh - 2cfh}{c+dx} \right)} - \left( iAbd^2 efg \sqrt{1 - \frac{-de + cf}{f(c+dx)}} \right) \right)$$

$$\begin{aligned}
 & \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \left( \text{EllipticE} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{-dg+ch}{h}}}{\sqrt{c+dx}} \right], \frac{(-de+cf)h}{f(-dg+ch)} \right] - \right. \\
 & \left. \text{EllipticF} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{-dg+ch}{h}}}{\sqrt{c+dx}} \right], \frac{(-de+cf)h}{f(-dg+ch)} \right] \right) / \left( (bc-ad)(-de+cf) \right) \\
 & \sqrt{-\frac{-dg+ch}{h}} \sqrt{\left( fh + \frac{d^2eg - cdfg - cdeh + c^2fh}{(c+dx)^2} + \frac{dfg+deh-2cfh}{c+dx} \right)} - \\
 & \left( i A b c d f^2 g \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \left( \text{EllipticE} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{-dg+ch}{h}}}{\sqrt{c+dx}} \right], \right. \right. \right. \\
 & \left. \left. \frac{(-de+cf)h}{f(-dg+ch)} \right] - \text{EllipticF} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{-dg+ch}{h}}}{\sqrt{c+dx}} \right], \frac{(-de+cf)h}{f(-dg+ch)} \right] \right) / \left( \right. \\
 & \left. (bc-ad)(-de+cf) \sqrt{-\frac{-dg+ch}{h}} \sqrt{\left( fh + \frac{d^2eg - cdfg - cdeh + c^2fh}{(c+dx)^2} + \right. \right. \\
 & \left. \left. \frac{dfg+deh-2cfh}{c+dx} \right)} \right) + \left( i A B c d f^2 g \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \right. \\
 & \left. \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \left( \text{EllipticE} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{-dg+ch}{h}}}{\sqrt{c+dx}} \right], \frac{(-de+cf)h}{f(-dg+ch)} \right] - \right. \right. \\
 & \left. \left. \text{EllipticF} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{-dg+ch}{h}}}{\sqrt{c+dx}} \right], \frac{(-de+cf)h}{f(-dg+ch)} \right] \right) \right) / \left( (bc-ad)(-de+cf) \right)
 \end{aligned}$$

$$\begin{aligned}
 & \sqrt{-\frac{-dg+ch}{h}} \sqrt{\left( fh + \frac{d^2eg - cdfg - cdeh + c^2fh}{(c+dx)^2} + \frac{dfg+deh-2cfh}{c+dx} \right)} - \\
 & \left( iAbcdefh \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \left( \text{EllipticE}\left[ i \text{ArcSinh}\left[ \frac{\sqrt{-\frac{-dg+ch}{h}}}{\sqrt{c+dx}} \right], \right. \right. \right. \\
 & \left. \left. \left. \frac{(-de+cf)h}{f(-dg+ch)} \right] - \text{EllipticF}\left[ i \text{ArcSinh}\left[ \frac{\sqrt{-\frac{-dg+ch}{h}}}{\sqrt{c+dx}} \right], \frac{(-de+cf)h}{f(-dg+ch)} \right] \right) \right) / \\
 & \left( (bc-ad)(-de+cf) \sqrt{-\frac{-dg+ch}{h}} \sqrt{\left( fh + \frac{d^2eg - cdfg - cdeh + c^2fh}{(c+dx)^2} + \right. \right. \\
 & \left. \left. \frac{dfg+deh-2cfh}{c+dx} \right) \right) + \left( iab cdefh \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \right. \\
 & \left. \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \left( \text{EllipticE}\left[ i \text{ArcSinh}\left[ \frac{\sqrt{-\frac{-dg+ch}{h}}}{\sqrt{c+dx}} \right], \frac{(-de+cf)h}{f(-dg+ch)} \right] - \right. \right. \\
 & \left. \left. \text{EllipticF}\left[ i \text{ArcSinh}\left[ \frac{\sqrt{-\frac{-dg+ch}{h}}}{\sqrt{c+dx}} \right], \frac{(-de+cf)h}{f(-dg+ch)} \right] \right) \right) / \left( (bc-ad)(-de+cf) \right. \\
 & \left. \sqrt{-\frac{-dg+ch}{h}} \sqrt{\left( fh + \frac{d^2eg - cdfg - cdeh + c^2fh}{(c+dx)^2} + \frac{dfg+deh-2cfh}{c+dx} \right) \right) + \\
 & \left( iAbc^2f^2h \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \left( \text{EllipticE}\left[ i \text{ArcSinh}\left[ \frac{\sqrt{-\frac{-dg+ch}{h}}}{\sqrt{c+dx}} \right], \right. \right. \right.
 \end{aligned}$$

$$\left. \left. \left. \frac{(-de+cf)h}{f(-dg+ch)} \right] - \text{EllipticF} \left[ \text{i ArcSinh} \left[ \frac{\sqrt{-\frac{dg+ch}{h}}}{\sqrt{c+dx}} \right], \frac{(-de+cf)h}{f(-dg+ch)} \right] \right) \right) /$$

$$\left( (bc-ad)(-de+cf) \sqrt{-\frac{dg+ch}{h}} \sqrt{\left( fh + \frac{d^2eg - cdfg - cdeh + c^2fh}{(c+dx)^2} + \right.} \right.$$

$$\left. \left. \frac{dfg+deh-2cfh}{c+dx} \right) \right) - \left( \text{i a B c}^2 f^2 h \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \right.$$

$$\left. \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \left( \text{EllipticE} \left[ \text{i ArcSinh} \left[ \frac{\sqrt{-\frac{dg+ch}{h}}}{\sqrt{c+dx}} \right], \frac{(-de+cf)h}{f(-dg+ch)} \right] - \right. \right.$$

$$\left. \left. \text{EllipticF} \left[ \text{i ArcSinh} \left[ \frac{\sqrt{-\frac{dg+ch}{h}}}{\sqrt{c+dx}} \right], \frac{(-de+cf)h}{f(-dg+ch)} \right] \right) \right) / \left( (bc-ad)(-de+cf) \right.$$

$$\left. \sqrt{-\frac{dg+ch}{h}} \sqrt{\left( fh + \frac{d^2eg - cdfg - cdeh + c^2fh}{(c+dx)^2} + \frac{dfg+deh-2cfh}{c+dx} \right)} \right) -$$

$$\left( \text{i A b}^2 d^2 e g \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \text{EllipticF} \left[ \right. \right.$$

$$\left. \left. \text{i ArcSinh} \left[ \frac{\sqrt{-\frac{dg+ch}{h}}}{\sqrt{c+dx}} \right], \frac{(-de+cf)h}{f(-dg+ch)} \right] \right) / \left( (bc-ad)^2 \sqrt{-\frac{dg+ch}{h}} \right.$$

$$\left. \sqrt{\left( fh + \frac{d^2eg - cdfg - cdeh + c^2fh}{(c+dx)^2} + \frac{dfg+deh-2cfh}{c+dx} \right)} \right) +$$

$$\left( \begin{aligned} & i a b B d^2 e g \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \text{EllipticF} \left[ \right. \\ & \quad \left. i \text{ArcSinh} \left[ \frac{\sqrt{\frac{-dg+ch}{h}}}{\sqrt{c+dx}}, \frac{(-de+cf)h}{f(-dg+ch)} \right] \right] / \left( (bc-ad)^2 \sqrt{\frac{-dg+ch}{h}} \right. \\ & \quad \left. \sqrt{\left( fh + \frac{d^2 eg - cdfg - cdeh + c^2 fh}{(c+dx)^2} + \frac{dfg + deh - 2cfh}{c+dx} \right)} \right) + \end{aligned} \right.$$

$$\left( \begin{aligned} & 2 i b B d e g \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \text{EllipticF} \left[ \right. \\ & \quad \left. i \text{ArcSinh} \left[ \frac{\sqrt{\frac{-dg+ch}{h}}}{\sqrt{c+dx}}, \frac{(-de+cf)h}{f(-dg+ch)} \right] \right] / \left( (bc-ad) \sqrt{\frac{-dg+ch}{h}} \right. \\ & \quad \left. \sqrt{\left( fh + \frac{d^2 eg - cdfg - cdeh + c^2 fh}{(c+dx)^2} + \frac{dfg + deh - 2cfh}{c+dx} \right)} \right) + \end{aligned} \right.$$

$$\left( \begin{aligned} & i A b^2 c d f g \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \text{EllipticF} \left[ \right. \\ & \quad \left. i \text{ArcSinh} \left[ \frac{\sqrt{\frac{-dg+ch}{h}}}{\sqrt{c+dx}}, \frac{(-de+cf)h}{f(-dg+ch)} \right] \right] / \left( (bc-ad)^2 \sqrt{\frac{-dg+ch}{h}} \right. \\ & \quad \left. \sqrt{\left( fh + \frac{d^2 eg - cdfg - cdeh + c^2 fh}{(c+dx)^2} + \frac{dfg + deh - 2cfh}{c+dx} \right)} \right) - \end{aligned} \right.$$

$$\left( \begin{aligned} & i a b B c d f g \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \text{EllipticF} \left[ \right. \\ & \left. i \text{ArcSinh} \left[ \frac{\sqrt{\frac{-dg+ch}{h}}}{\sqrt{c+dx}}, \frac{(-de+cf)h}{f(-dg+ch)} \right] \right] / \left( (bc-ad)^2 \sqrt{\frac{-dg+ch}{h}} \right. \\ & \left. \left. \sqrt{\left( fh + \frac{d^2 eg - cdfg - cdeh + c^2 fh}{(c+dx)^2} + \frac{dfg+deh-2cfh}{c+dx} \right)} \right) \right) - \end{aligned}$$

$$\left( \begin{aligned} & 2 i A b d f g \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \text{EllipticF} \left[ \right. \\ & \left. i \text{ArcSinh} \left[ \frac{\sqrt{\frac{-dg+ch}{h}}}{\sqrt{c+dx}}, \frac{(-de+cf)h}{f(-dg+ch)} \right] \right] / \left( (bc-ad) \sqrt{\frac{-dg+ch}{h}} \right. \\ & \left. \left. \sqrt{\left( fh + \frac{d^2 eg - cdfg - cdeh + c^2 fh}{(c+dx)^2} + \frac{dfg+deh-2cfh}{c+dx} \right)} \right) \right) + \end{aligned}$$

$$\left( \begin{aligned} & i A b^2 c d e h \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \text{EllipticF} \left[ \right. \\ & \left. i \text{ArcSinh} \left[ \frac{\sqrt{\frac{-dg+ch}{h}}}{\sqrt{c+dx}}, \frac{(-de+cf)h}{f(-dg+ch)} \right] \right] / \left( (bc-ad)^2 \sqrt{\frac{-dg+ch}{h}} \right. \\ & \left. \left. \sqrt{\left( fh + \frac{d^2 eg - cdfg - cdeh + c^2 fh}{(c+dx)^2} + \frac{dfg+deh-2cfh}{c+dx} \right)} \right) \right) - \end{aligned}$$

$$\left( \begin{aligned} & i a b B c d e h \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \text{EllipticF} \left[ \right. \\ & \left. i \text{ArcSinh} \left[ \frac{\sqrt{\frac{-dg+ch}{h}}}{\sqrt{c+dx}}, \frac{(-de+cf)h}{f(-dg+ch)} \right] \right] / \left( (bc-ad)^2 \sqrt{\frac{-dg+ch}{h}} \right. \\ & \left. \sqrt{\left( fh + \frac{d^2 eg - cdfg - cdeh + c^2 fh}{(c+dx)^2} + \frac{dfg+deh-2cfh}{c+dx} \right)} \right) - \\ & \left( \begin{aligned} & 2 i A b d e h \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \text{EllipticF} \left[ \right. \\ & \left. i \text{ArcSinh} \left[ \frac{\sqrt{\frac{-dg+ch}{h}}}{\sqrt{c+dx}}, \frac{(-de+cf)h}{f(-dg+ch)} \right] \right] / \left( (bc-ad) \sqrt{\frac{-dg+ch}{h}} \right. \\ & \left. \sqrt{\left( fh + \frac{d^2 eg - cdfg - cdeh + c^2 fh}{(c+dx)^2} + \frac{dfg+deh-2cfh}{c+dx} \right)} \right) - \\ & \left( \begin{aligned} & i A b^2 c^2 f h \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \text{EllipticF} \left[ \right. \\ & \left. i \text{ArcSinh} \left[ \frac{\sqrt{\frac{-dg+ch}{h}}}{\sqrt{c+dx}}, \frac{(-de+cf)h}{f(-dg+ch)} \right] \right] / \left( (bc-ad)^2 \sqrt{\frac{-dg+ch}{h}} \right. \\ & \left. \sqrt{\left( fh + \frac{d^2 eg - cdfg - cdeh + c^2 fh}{(c+dx)^2} + \frac{dfg+deh-2cfh}{c+dx} \right)} \right) + \end{aligned} \end{aligned} \right)$$

$$\begin{aligned}
 & \left( i a b B c^2 f h \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \text{EllipticF} \left[ \right. \right. \\
 & \quad \left. \left. i \text{ArcSinh} \left[ \frac{\sqrt{\frac{-dg+ch}{h}}}{\sqrt{c+dx}}, \frac{(-de+cf)h}{f(-dg+ch)} \right] \right] / \left( (bc-ad)^2 \sqrt{\frac{-dg+ch}{h}} \right. \right. \\
 & \quad \left. \left. \sqrt{\left( fh + \frac{d^2 eg - cdfg - cdeh + c^2 fh}{(c+dx)^2} + \frac{dfg + deh - 2cfh}{c+dx} \right)} \right) + \right. \\
 & \left( 2 i A b c f h \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \text{EllipticF} \left[ \right. \right. \\
 & \quad \left. \left. i \text{ArcSinh} \left[ \frac{\sqrt{\frac{-dg+ch}{h}}}{\sqrt{c+dx}}, \frac{(-de+cf)h}{f(-dg+ch)} \right] \right] / \left( (bc-ad) \sqrt{\frac{-dg+ch}{h}} \right. \right. \\
 & \quad \left. \left. \sqrt{\left( fh + \frac{d^2 eg - cdfg - cdeh + c^2 fh}{(c+dx)^2} + \frac{dfg + deh - 2cfh}{c+dx} \right)} \right) - \right. \\
 & \left( 2 i a B c f h \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \text{EllipticF} \left[ \right. \right. \\
 & \quad \left. \left. i \text{ArcSinh} \left[ \frac{\sqrt{\frac{-dg+ch}{h}}}{\sqrt{c+dx}}, \frac{(-de+cf)h}{f(-dg+ch)} \right] \right] / \left( (bc-ad) \sqrt{\frac{-dg+ch}{h}} \right. \right. \\
 & \quad \left. \left. \sqrt{\left( fh + \frac{d^2 eg - cdfg - cdeh + c^2 fh}{(c+dx)^2} + \frac{dfg + deh - 2cfh}{c+dx} \right)} \right) + \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left( 2 i a A d f h \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \operatorname{EllipticF} \left[ \right. \right. \\
 & \quad \left. \left. i \operatorname{ArcSinh} \left[ \frac{\sqrt{-\frac{-dg+ch}{h}}}{\sqrt{c+dx}} \right], \frac{(-de+cf)h}{f(-dg+ch)} \right] \right) / \left( (bc-ad) \sqrt{-\frac{-dg+ch}{h}} \right. \\
 & \quad \left. \sqrt{\left( fh + \frac{d^2 eg - cdfg - cdeh + c^2 fh}{(c+dx)^2} + \frac{dfg + deh - 2cfh}{c+dx} \right)} \right) + \frac{1}{(bc-ad)^3} \\
 & A b^3 d^2 e g \left( \left( i c \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \operatorname{EllipticPi} \left[ \frac{(bc-ad)h}{b(-dg+ch)}, \right. \right. \right. \\
 & \quad \left. \left. i \operatorname{ArcSinh} \left[ \frac{\sqrt{-\frac{-dg+ch}{h}}}{\sqrt{c+dx}} \right], \frac{(-de+cf)h}{f(-dg+ch)} \right] \right) / \left( \sqrt{-\frac{-dg+ch}{h}} \sqrt{\left( fh + \right. \right.} \\
 & \quad \left. \left. \frac{d^2 eg}{(c+dx)^2} - \frac{cdfg}{(c+dx)^2} - \frac{cdeh}{(c+dx)^2} + \frac{c^2 fh}{(c+dx)^2} + \frac{dfg}{c+dx} + \frac{deh}{c+dx} - \frac{2cfh}{c+dx} \right)} \right) - \\
 & \left( i a d \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \operatorname{EllipticPi} \left[ \frac{(bc-ad)h}{b(-dg+ch)}, i \operatorname{ArcSinh} \left[ \right. \right. \right. \\
 & \quad \left. \left. \frac{\sqrt{-\frac{-dg+ch}{h}}}{\sqrt{c+dx}} \right], \frac{(-de+cf)h}{f(-dg+ch)} \right] \right) / \left( b \sqrt{-\frac{-dg+ch}{h}} \sqrt{\left( fh + \frac{d^2 eg}{(c+dx)^2} - \right. \right.} \\
 & \quad \left. \left. \frac{cdfg}{(c+dx)^2} - \frac{cdeh}{(c+dx)^2} + \frac{c^2 fh}{(c+dx)^2} + \frac{dfg}{c+dx} + \frac{deh}{c+dx} - \frac{2cfh}{c+dx} \right)} \right) - \frac{1}{(bc-ad)^3}
 \end{aligned}$$

$$\begin{aligned}
 & a b^2 B d^2 e g \left( \left( i c \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \operatorname{EllipticPi} \left[ \frac{(bc-ad)h}{b(-dg+ch)}, \right. \right. \right. \\
 & \quad \left. \left. \left. i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{-dg+ch}{h}}}{\sqrt{c+dx}} \right], \frac{(-de+cf)h}{f(-dg+ch)} \right] \right) / \left( \sqrt{\frac{-dg+ch}{h}} \sqrt{\left( fh + \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{d^2 e g}{(c+dx)^2} - \frac{c d f g}{(c+dx)^2} - \frac{c d e h}{(c+dx)^2} + \frac{c^2 f h}{(c+dx)^2} + \frac{d f g}{c+dx} + \frac{d e h}{c+dx} - \frac{2 c f h}{c+dx} \right) \right) - \\
 & \left( i a d \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \operatorname{EllipticPi} \left[ \frac{(bc-ad)h}{b(-dg+ch)}, i \operatorname{ArcSinh} \left[ \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{\sqrt{\frac{-dg+ch}{h}}}{\sqrt{c+dx}} \right], \frac{(-de+cf)h}{f(-dg+ch)} \right] \right) / \left( b \sqrt{\frac{-dg+ch}{h}} \sqrt{\left( fh + \frac{d^2 e g}{(c+dx)^2} - \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{c d f g}{(c+dx)^2} - \frac{c d e h}{(c+dx)^2} + \frac{c^2 f h}{(c+dx)^2} + \frac{d f g}{c+dx} + \frac{d e h}{c+dx} - \frac{2 c f h}{c+dx} \right) \right) - \frac{1}{(bc-ad)^2} \\
 & 2 b^2 B d e g \left( \left( i c \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \operatorname{EllipticPi} \left[ \frac{(bc-ad)h}{b(-dg+ch)}, \right. \right. \right. \\
 & \quad \left. \left. \left. i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{-dg+ch}{h}}}{\sqrt{c+dx}} \right], \frac{(-de+cf)h}{f(-dg+ch)} \right] \right) / \left( \sqrt{\frac{-dg+ch}{h}} \sqrt{\left( fh + \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{d^2 e g}{(c+dx)^2} - \frac{c d f g}{(c+dx)^2} - \frac{c d e h}{(c+dx)^2} + \frac{c^2 f h}{(c+dx)^2} + \frac{d f g}{c+dx} + \frac{d e h}{c+dx} - \frac{2 c f h}{c+dx} \right) \right) -
 \end{aligned}$$



$$\frac{1}{(bc-ad)^3} a b^2 B c d f g \left( \left( i c \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \text{EllipticPi} \left[ \frac{(bc-ad)h}{b(-dg+ch)}, i \text{ArcSinh} \left[ \frac{\sqrt{\frac{-dg+ch}{h}}}{\sqrt{c+dx}} \right], \frac{(-de+cf)h}{f(-dg+ch)} \right] \right) / \right.$$

$$\left( \sqrt{\frac{-dg+ch}{h}} \sqrt{\left( fh + \frac{d^2 eg}{(c+dx)^2} - \frac{cdfg}{(c+dx)^2} - \frac{cdeh}{(c+dx)^2} + \frac{c^2 fh}{(c+dx)^2} + \frac{dfg}{c+dx} + \frac{deh}{c+dx} - \frac{2cfh}{c+dx} \right)} \right) - \left( i a d \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \right.$$

$$\left. \text{EllipticPi} \left[ \frac{(bc-ad)h}{b(-dg+ch)}, i \text{ArcSinh} \left[ \frac{\sqrt{\frac{-dg+ch}{h}}}{\sqrt{c+dx}} \right], \frac{(-de+cf)h}{f(-dg+ch)} \right] \right) / \left( b \sqrt{\frac{-dg+ch}{h}} \sqrt{\left( fh + \frac{d^2 eg}{(c+dx)^2} - \frac{cdfg}{(c+dx)^2} - \frac{cdeh}{(c+dx)^2} + \frac{c^2 fh}{(c+dx)^2} + \frac{dfg}{c+dx} + \frac{deh}{c+dx} - \frac{2cfh}{c+dx} \right)} \right) + \frac{1}{(bc-ad)^2}$$

$$2 A b^2 d f g \left( \left( i c \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \text{EllipticPi} \left[ \frac{(bc-ad)h}{b(-dg+ch)}, i \text{ArcSinh} \left[ \frac{\sqrt{\frac{-dg+ch}{h}}}{\sqrt{c+dx}} \right], \frac{(-de+cf)h}{f(-dg+ch)} \right] \right) / \left( \sqrt{\frac{-dg+ch}{h}} \sqrt{\left( fh + \right.} \right.$$

$$\left. \left( \frac{d^2 e g}{(c+dx)^2} - \frac{c d f g}{(c+dx)^2} - \frac{c d e h}{(c+dx)^2} + \frac{c^2 f h}{(c+dx)^2} + \frac{d f g}{c+dx} + \frac{d e h}{c+dx} - \frac{2 c f h}{c+dx} \right) \right) -$$

$$\left( i a d \sqrt{1 - \frac{-d e + c f}{f (c+dx)}} \sqrt{1 - \frac{-d g + c h}{h (c+dx)}} \text{EllipticPi} \left[ \frac{(b c - a d) h}{b (-d g + c h)}, \right. \right.$$

$$\left. \left. i \text{ArcSinh} \left[ \frac{\sqrt{\frac{-d g + c h}{h}}}{\sqrt{c+dx}} \right], \frac{(-d e + c f) h}{f (-d g + c h)} \right] \right) / \left( b \sqrt{\frac{-d g + c h}{h}} \sqrt{\left( f h + \right. \right.$$

$$\left. \left. \frac{d^2 e g}{(c+dx)^2} - \frac{c d f g}{(c+dx)^2} - \frac{c d e h}{(c+dx)^2} + \frac{c^2 f h}{(c+dx)^2} + \frac{d f g}{c+dx} + \frac{d e h}{c+dx} - \frac{2 c f h}{c+dx} \right) \right) \right) -$$

$$\frac{1}{(b c - a d)^3} A b^3 c d e h \left( \left( i c \sqrt{1 - \frac{-d e + c f}{f (c+dx)}} \sqrt{1 - \frac{-d g + c h}{h (c+dx)}} \text{EllipticPi} \left[ \right. \right. \right.$$

$$\left. \left. \left. \frac{(b c - a d) h}{b (-d g + c h)}, i \text{ArcSinh} \left[ \frac{\sqrt{\frac{-d g + c h}{h}}}{\sqrt{c+dx}} \right], \frac{(-d e + c f) h}{f (-d g + c h)} \right] \right) / \right.$$

$$\left. \left( \sqrt{\frac{-d g + c h}{h}} \sqrt{\left( f h + \frac{d^2 e g}{(c+dx)^2} - \frac{c d f g}{(c+dx)^2} - \frac{c d e h}{(c+dx)^2} + \frac{c^2 f h}{(c+dx)^2} + \right. \right. \right.$$

$$\left. \left. \left. \frac{d f g}{c+dx} + \frac{d e h}{c+dx} - \frac{2 c f h}{c+dx} \right) \right) - \left( i a d \sqrt{1 - \frac{-d e + c f}{f (c+dx)}} \sqrt{1 - \frac{-d g + c h}{h (c+dx)}} \right.$$

$$\left. \left. \text{EllipticPi} \left[ \frac{(b c - a d) h}{b (-d g + c h)}, i \text{ArcSinh} \left[ \frac{\sqrt{\frac{-d g + c h}{h}}}{\sqrt{c+dx}} \right], \frac{(-d e + c f) h}{f (-d g + c h)} \right] \right) / \right.$$

$$\begin{aligned}
 & \left( b \sqrt{-\frac{-dg+ch}{h}} \sqrt{\left( fh + \frac{d^2 eg}{(c+dx)^2} - \frac{cdfg}{(c+dx)^2} - \frac{cdeh}{(c+dx)^2} + \right.} \right. \\
 & \quad \left. \left. \frac{c^2 fh}{(c+dx)^2} + \frac{dfg}{c+dx} + \frac{deh}{c+dx} - \frac{2cfh}{c+dx} \right) \right) + \frac{1}{(bc-ad)^3} \\
 & ab^2 B c d e h \left( \left( i c \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \operatorname{EllipticPi}\left[\frac{(bc-ad)h}{b(-dg+ch)}\right], \right. \right. \\
 & \quad \left. \left. i \operatorname{ArcSinh}\left[\frac{\sqrt{-\frac{-dg+ch}{h}}}{\sqrt{c+dx}}\right], \frac{(-de+cf)h}{f(-dg+ch)} \right] \right) / \left( \sqrt{-\frac{-dg+ch}{h}} \sqrt{\left( fh + \right.} \right. \\
 & \quad \left. \left. \frac{d^2 eg}{(c+dx)^2} - \frac{cdfg}{(c+dx)^2} - \frac{cdeh}{(c+dx)^2} + \frac{c^2 fh}{(c+dx)^2} + \frac{dfg}{c+dx} + \frac{deh}{c+dx} - \frac{2cfh}{c+dx} \right) \right) - \\
 & \left( i a d \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \operatorname{EllipticPi}\left[\frac{(bc-ad)h}{b(-dg+ch)}\right], \right. \\
 & \quad \left. i \operatorname{ArcSinh}\left[\frac{\sqrt{-\frac{-dg+ch}{h}}}{\sqrt{c+dx}}\right], \frac{(-de+cf)h}{f(-dg+ch)} \right] \right) / \left( b \sqrt{-\frac{-dg+ch}{h}} \sqrt{\left( fh + \right.} \right. \\
 & \quad \left. \left. \frac{d^2 eg}{(c+dx)^2} - \frac{cdfg}{(c+dx)^2} - \frac{cdeh}{(c+dx)^2} + \frac{c^2 fh}{(c+dx)^2} + \frac{dfg}{c+dx} + \frac{deh}{c+dx} - \frac{2cfh}{c+dx} \right) \right) + \\
 & \frac{1}{(bc-ad)^2} 2 A b^2 d e h \left( \left( i c \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \operatorname{EllipticPi}\left[ \right. \right. \right.
 \end{aligned}$$

$$\left. \frac{(bc-ad)h}{b(-dg+ch)}, \operatorname{ArcSinh}\left[\frac{\sqrt{-\frac{dg+ch}{h}}}{\sqrt{c+dx}}\right], \frac{(-de+cf)h}{f(-dg+ch)}\right] /$$

$$\left( \sqrt{-\frac{dg+ch}{h}} \sqrt{\left( fh + \frac{d^2eg}{(c+dx)^2} - \frac{cdfg}{(c+dx)^2} - \frac{cdeh}{(c+dx)^2} + \frac{c^2fh}{(c+dx)^2} + \right.} \right.$$

$$\left. \frac{dfg}{c+dx} + \frac{deh}{c+dx} - \frac{2cfh}{c+dx} \right) - \left( iad \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \right.$$

$$\left. \operatorname{EllipticPi}\left[\frac{(bc-ad)h}{b(-dg+ch)}, \operatorname{ArcSinh}\left[\frac{\sqrt{-\frac{dg+ch}{h}}}{\sqrt{c+dx}}\right], \frac{(-de+cf)h}{f(-dg+ch)}\right] \right) /$$

$$\left( b \sqrt{-\frac{dg+ch}{h}} \sqrt{\left( fh + \frac{d^2eg}{(c+dx)^2} - \frac{cdfg}{(c+dx)^2} - \frac{cdeh}{(c+dx)^2} + \right.} \right.$$

$$\left. \frac{c^2fh}{(c+dx)^2} + \frac{dfg}{c+dx} + \frac{deh}{c+dx} - \frac{2cfh}{c+dx} \right) + \frac{1}{(bc-ad)^3}$$

$$Ab^3c^2fh \left( \left( i c \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \operatorname{EllipticPi}\left[\frac{(bc-ad)h}{b(-dg+ch)}, \right. \right. \right.$$

$$\left. \left. \operatorname{ArcSinh}\left[\frac{\sqrt{-\frac{dg+ch}{h}}}{\sqrt{c+dx}}\right], \frac{(-de+cf)h}{f(-dg+ch)}\right] \right) / \left( \sqrt{-\frac{dg+ch}{h}} \sqrt{\left( fh + \right.} \right.$$

$$\left. \frac{d^2eg}{(c+dx)^2} - \frac{cdfg}{(c+dx)^2} - \frac{cdeh}{(c+dx)^2} + \frac{c^2fh}{(c+dx)^2} + \frac{dfg}{c+dx} + \frac{deh}{c+dx} - \frac{2cfh}{c+dx} \right) -$$



$$\left. \left( \frac{c^2 f h}{(c+dx)^2} + \frac{d f g}{c+dx} + \frac{d e h}{c+dx} - \frac{2 c f h}{c+dx} \right) \right) - \frac{1}{(bc-ad)^2}$$

$$2 A b^2 c f h \left( \left( i c \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \operatorname{EllipticPi} \left[ \frac{(bc-ad)h}{b(-dg+ch)}, \right. \right. \right.$$

$$\left. \left. \left. i \operatorname{ArcSinh} \left[ \frac{\sqrt{-\frac{-dg+ch}{h}}}{\sqrt{c+dx}} \right], \frac{(-de+cf)h}{f(-dg+ch)} \right] \right) / \left( \sqrt{-\frac{-dg+ch}{h}} \sqrt{fh +} \right. \right.$$

$$\left. \left. \frac{d^2 e g}{(c+dx)^2} - \frac{c d f g}{(c+dx)^2} - \frac{c d e h}{(c+dx)^2} + \frac{c^2 f h}{(c+dx)^2} + \frac{d f g}{c+dx} + \frac{d e h}{c+dx} - \frac{2 c f h}{c+dx} \right) \right) -$$

$$\left( i a d \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \operatorname{EllipticPi} \left[ \frac{(bc-ad)h}{b(-dg+ch)}, \right. \right.$$

$$\left. \left. \left. i \operatorname{ArcSinh} \left[ \frac{\sqrt{-\frac{-dg+ch}{h}}}{\sqrt{c+dx}} \right], \frac{(-de+cf)h}{f(-dg+ch)} \right] \right) / \left( b \sqrt{-\frac{-dg+ch}{h}} \sqrt{fh +} \right. \right.$$

$$\left. \left. \frac{d^2 e g}{(c+dx)^2} - \frac{c d f g}{(c+dx)^2} - \frac{c d e h}{(c+dx)^2} + \frac{c^2 f h}{(c+dx)^2} + \frac{d f g}{c+dx} + \frac{d e h}{c+dx} - \frac{2 c f h}{c+dx} \right) \right) +$$

$$\frac{1}{(bc-ad)^2} 2 a b B c f h \left( \left( i c \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \operatorname{EllipticPi} \left[ \right. \right. \right.$$

$$\left. \left. \left. \frac{(bc-ad)h}{b(-dg+ch)}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{-\frac{-dg+ch}{h}}}{\sqrt{c+dx}} \right], \frac{(-de+cf)h}{f(-dg+ch)} \right] \right) / \right.$$

$$\begin{aligned}
 & \left( \sqrt{-\frac{dg+ch}{h}} \sqrt{\left( fh + \frac{d^2 eg}{(c+dx)^2} - \frac{cdfg}{(c+dx)^2} - \frac{cdeh}{(c+dx)^2} + \frac{c^2 fh}{(c+dx)^2} + \right.} \right. \\
 & \quad \left. \frac{dfg}{c+dx} + \frac{deh}{c+dx} - \frac{2cfh}{c+dx} \right) - \left( i ad \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \right. \\
 & \quad \left. \text{EllipticPi}\left[ \frac{(bc-ad)h}{b(-dg+ch)}, i \text{ArcSinh}\left[ \frac{\sqrt{-\frac{dg+ch}{h}}}{\sqrt{c+dx}} \right], \frac{(-de+cf)h}{f(-dg+ch)} \right] \right) / \\
 & \left( b \sqrt{-\frac{dg+ch}{h}} \sqrt{\left( fh + \frac{d^2 eg}{(c+dx)^2} - \frac{cdfg}{(c+dx)^2} - \frac{cdeh}{(c+dx)^2} + \right.} \right. \\
 & \quad \left. \frac{c^2 fh}{(c+dx)^2} + \frac{dfg}{c+dx} + \frac{deh}{c+dx} - \frac{2cfh}{c+dx} \right) - \frac{1}{(bc-ad)^2} \\
 & 2 a A b d f h \left( \left( i c \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \text{EllipticPi}\left[ \frac{(bc-ad)h}{b(-dg+ch)}, \right. \right. \right. \\
 & \quad \left. \left. i \text{ArcSinh}\left[ \frac{\sqrt{-\frac{dg+ch}{h}}}{\sqrt{c+dx}} \right], \frac{(-de+cf)h}{f(-dg+ch)} \right] \right) / \left( \sqrt{-\frac{dg+ch}{h}} \sqrt{\left( fh + \right.} \right. \\
 & \quad \left. \frac{d^2 eg}{(c+dx)^2} - \frac{cdfg}{(c+dx)^2} - \frac{cdeh}{(c+dx)^2} + \frac{c^2 fh}{(c+dx)^2} + \frac{dfg}{c+dx} + \frac{deh}{c+dx} - \frac{2cfh}{c+dx} \right) - \\
 & \left( i a d \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \text{EllipticPi}\left[ \frac{(bc-ad)h}{b(-dg+ch)}, \right. \right.
 \end{aligned}$$



$$\begin{aligned}
 & \left( \operatorname{ArcSinh} \left[ \frac{\sqrt{-\frac{dg+ch}{h}}}{\sqrt{c+dx}} \right], \frac{(-de+cf)h}{f(-dg+ch)} \right) / \left( \sqrt{-\frac{dg+ch}{h}} \sqrt{\left( fh + \right. \right.} \\
 & \left. \left. \frac{d^2 eg}{(c+dx)^2} - \frac{cdfg}{(c+dx)^2} - \frac{cdeh}{(c+dx)^2} + \frac{c^2 fh}{(c+dx)^2} + \frac{dfg}{c+dx} + \frac{deh}{c+dx} - \frac{2cfh}{c+dx} \right) \right) - \\
 & \left( \operatorname{a} d \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \operatorname{EllipticPi} \left[ \frac{(bc-ad)h}{b(-dg+ch)}, \operatorname{ArcSinh} \left[ \right. \right. \right. \\
 & \left. \left. \frac{\sqrt{-\frac{dg+ch}{h}}}{\sqrt{c+dx}} \right], \frac{(-de+cf)h}{f(-dg+ch)} \right] \right) / \left( b \sqrt{-\frac{dg+ch}{h}} \sqrt{\left( fh + \frac{d^2 eg}{(c+dx)^2} - \right. \right.} \\
 & \left. \left. \frac{cdfg}{(c+dx)^2} - \frac{cdeh}{(c+dx)^2} + \frac{c^2 fh}{(c+dx)^2} + \frac{dfg}{c+dx} + \frac{deh}{c+dx} - \frac{2cfh}{c+dx} \right) \right) \right) / \\
 & \left( \left( \operatorname{A} b f h - \operatorname{a} B f h + \frac{\operatorname{A} b d^2 e g}{(c+dx)^2} - \frac{\operatorname{a} B d^2 e g}{(c+dx)^2} - \frac{\operatorname{A} b c d f g}{(c+dx)^2} + \frac{\operatorname{a} B c d f g}{(c+dx)^2} - \frac{\operatorname{A} b c d e h}{(c+dx)^2} + \right. \right. \\
 & \frac{\operatorname{a} B c d e h}{(c+dx)^2} + \frac{\operatorname{A} b c^2 f h}{(c+dx)^2} - \\
 & \frac{\operatorname{a} B c^2 f h}{(c+dx)^2} - \frac{2 b B d e g}{c+dx} + \\
 & \frac{2 \operatorname{A} b d f g}{c+dx} + \frac{2 \operatorname{A} b d e h}{c+dx} - \frac{2 \operatorname{A} b c f h}{c+dx} + \\
 & \left. \left. \frac{2 \operatorname{a} B c f h}{c+dx} - \frac{2 \operatorname{a} A d f h}{c+dx} \right) \right) \\
 & \left( \sqrt{e + \frac{(c+dx) \left( f - \frac{cf}{c+dx} \right)}{d}} \sqrt{g + \frac{(c+dx) \left( h - \frac{ch}{c+dx} \right)}{d}} \right)
 \end{aligned}$$

Problem 6: Result more than twice size of optimal antiderivative.

$$\int \frac{(a+bx)^{3/2} (A+Bx)}{\sqrt{c+dx} \sqrt{e+fx} \sqrt{g+hx}} dx$$

Optimal (type 4, 981 leaves, 10 steps):

$$\begin{aligned} & \frac{1}{4d^2 f^2 h^2 \sqrt{c+dx}} (5aBdfh + b(4Adfh - 3B(dfh + de + cfh))) \sqrt{a+bx} \sqrt{e+fx} \sqrt{g+hx} + \\ & \frac{bB \sqrt{a+bx} \sqrt{c+dx} \sqrt{e+fx} \sqrt{g+hx}}{2dfh} - \\ & \left( \sqrt{dg - ch} \sqrt{fg - eh} (5aBdfh + b(4Adfh - 3B(dfh + de + cfh))) \sqrt{a+bx} \right. \\ & \left. \sqrt{-\frac{(de - cf)(g+hx)}{(fg - eh)(c+dx)}} \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{dg - ch} \sqrt{e+fx}}{\sqrt{fg - eh} \sqrt{c+dx}}\right], \frac{(bc - ad)(fg - eh)}{(be - af)(dg - ch)}\right] \right) / \\ & \left( 4d^2 f^2 h^2 \sqrt{\frac{(de - cf)(a+bx)}{(be - af)(c+dx)}} \sqrt{g+hx} \right) - \\ & \left( (be - af) \sqrt{bg - ah} (3aBdfh + b(4Adfh - B(cf + 3d(fg + eh)))) \sqrt{\frac{(be - af)(c+dx)}{(de - cf)(a+bx)}} \right. \\ & \left. \sqrt{g+hx} \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{bg - ah} \sqrt{e+fx}}{\sqrt{fg - eh} \sqrt{a+bx}}\right], -\frac{(bc - ad)(fg - eh)}{(de - cf)(bg - ah)}\right] \right) / \\ & \left( 4bd^2 f^2 h^2 \sqrt{fg - eh} \sqrt{c+dx} \sqrt{-\frac{(be - af)(g+hx)}{(fg - eh)(a+bx)}} \right) + \\ & \frac{1}{4bd^2 \sqrt{bc - ad} f^2 h^3 \sqrt{c+dx} \sqrt{e+fx}} \\ & \sqrt{-dg + ch} (4dfh(2a(2Ab + aB)dfh - bB(b(deg + cfg + ceh) + a(dfh + de + cfh))) - \\ & (adf + b(dfh + de + cfh))(5aBdfh + b(4Adfh - 3B(dfh + de + cfh)))) \\ & (a+bx) \sqrt{\frac{(bg - ah)(c+dx)}{(dg - ch)(a+bx)}} \sqrt{\frac{(bg - ah)(e+fx)}{(fg - eh)(a+bx)}} \\ & \operatorname{EllipticPi}\left[-\frac{b(dg - ch)}{(bc - ad)h}, \operatorname{ArcSin}\left[\frac{\sqrt{bc - ad} \sqrt{g+hx}}{\sqrt{-dg + ch} \sqrt{a+bx}}\right], \frac{(be - af)(dg - ch)}{(bc - ad)(fg - eh)}\right] \end{aligned}$$

Result (type 4, 21555 leaves): Display of huge result suppressed!

**Problem 7: Result more than twice size of optimal antiderivative.**

$$\int \frac{\sqrt{a+bx} (A+Bx)}{\sqrt{c+dx} \sqrt{e+fx} \sqrt{g+hx}} dx$$

Optimal (type 4, 736 leaves, 7 steps):

$$\frac{B \sqrt{a+bx} \sqrt{e+fx} \sqrt{g+hx}}{fh \sqrt{c+dx}} - \left( B \sqrt{dg-ch} \sqrt{fg-eh} \sqrt{a+bx} \sqrt{-\frac{(de-cf)(g+hx)}{(fg-eh)(c+dx)}} \right. \\ \left. \text{EllipticE}\left[\text{ArcSin}\left[\frac{\sqrt{dg-ch} \sqrt{e+fx}}{\sqrt{fg-eh} \sqrt{c+dx}}\right], \frac{(bc-ad)(fg-eh)}{(be-af)(dg-ch)}\right]\right) / \\ \left( dfh \sqrt{\frac{(de-cf)(a+bx)}{(be-af)(c+dx)}} \sqrt{g+hx} \right) - \left( B (be-af) \sqrt{bg-ah} \sqrt{\frac{(be-af)(c+dx)}{(de-cf)(a+bx)}} \right. \\ \left. \sqrt{g+hx} \text{EllipticF}\left[\text{ArcSin}\left[\frac{\sqrt{bg-ah} \sqrt{e+fx}}{\sqrt{fg-eh} \sqrt{a+bx}}\right], -\frac{(bc-ad)(fg-eh)}{(de-cf)(bg-ah)}\right]\right) / \\ \left( bfh \sqrt{fg-eh} \sqrt{c+dx} \sqrt{-\frac{(be-af)(g+hx)}{(fg-eh)(a+bx)}} \right) + \\ \left( \sqrt{-dg+ch} (2Abdfh + B(adfh - b(dfg+deh+cfh))) (a+bx) \sqrt{\frac{(bg-ah)(c+dx)}{(dg-ch)(a+bx)}} \right. \\ \left. \sqrt{\frac{(bg-ah)(e+fx)}{(fg-eh)(a+bx)}} \text{EllipticPi}\left[-\frac{b(dg-ch)}{(bc-ad)h}, \text{ArcSin}\left[\frac{\sqrt{bc-ad} \sqrt{g+hx}}{\sqrt{-dg+ch} \sqrt{a+bx}}\right], \right. \right. \\ \left. \left. \frac{(be-af)(dg-ch)}{(bc-ad)(fg-eh)} \right) \right] / (bd \sqrt{bc-ad} fh^2 \sqrt{c+dx} \sqrt{e+fx})$$

Result (type 4, 6648 leaves):

$$-\frac{1}{d^2} 2 \left( \left( \left( B (c+dx)^{3/2} \left( f + \frac{de}{c+dx} - \frac{cf}{c+dx} \right) \left( h + \frac{dg}{c+dx} - \frac{ch}{c+dx} \right) \sqrt{a + \frac{(c+dx)(b - \frac{bc}{c+dx})}{d}} \right) \right) / \right. \\ \left. \left( 2fh \sqrt{e + \frac{(c+dx)(f - \frac{cf}{c+dx})}{d}} \sqrt{g + \frac{(c+dx)(h - \frac{ch}{c+dx})}{d}} \right) \right) + \\ \left( d (bg-ah) (dg-ch) (Bfg + Beh - 2Afh) \sqrt{c+dx} \right. \\ \left. \sqrt{\left( \left( b - \frac{bc}{c+dx} + \frac{ad}{c+dx} \right) \left( f + \frac{de}{c+dx} - \frac{cf}{c+dx} \right) \left( h + \frac{dg}{c+dx} - \frac{ch}{c+dx} \right) \right)} \right)$$

$$\begin{aligned}
 & \sqrt{a + \frac{(c+dx)\left(b - \frac{bc}{c+dx}\right)}{d}} \left( \left( de \sqrt{\frac{(bc-ad)(-dg+ch)\left(-\frac{b}{bc-ad} + \frac{1}{c+dx}\right)}{-bdg+adh}} \right. \right. \\
 & \left. \left. \left(-\frac{f}{-de+cf} + \frac{1}{c+dx}\right) \sqrt{\frac{-\frac{h}{-dg+ch} + \frac{1}{c+dx}}{\frac{f}{-de+cf} - \frac{h}{-dg+ch}}} \right. \right. \\
 & \left. \left. \left( \left( (-bdg+adh) \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\sqrt{\frac{(de-cf)\left(h + \frac{dg}{c+dx} - \frac{ch}{c+dx}\right)}{d(-fg+eh)}}\right], \right. \right. \right. \right. \\
 & \left. \left. \left. \frac{(bc-ad)(-fg+eh)}{(-de+cf)(-bg+ah)} \right] \right) / \left( (bc-ad)(-dg+ch) \right) - \frac{1}{bc-ad} b \operatorname{EllipticF}\left[ \right. \right. \\
 & \left. \left. \operatorname{ArcSin}\left[\sqrt{\frac{(de-cf)\left(h + \frac{dg}{c+dx} - \frac{ch}{c+dx}\right)}{d(-fg+eh)}}\right], \frac{(bc-ad)(-fg+eh)}{(-de+cf)(-bg+ah)} \right] \right) \right) / \\
 & \left( \sqrt{\frac{-\frac{f}{-de+cf} + \frac{1}{c+dx}}{-\frac{f}{-de+cf} + \frac{h}{-dg+ch}}} \sqrt{\left(b + \frac{-bc+ad}{c+dx}\right)\left(f + \frac{de-cf}{c+dx}\right)\left(h + \frac{dg-ch}{c+dx}\right)} \right) - \\
 & \left( cf \sqrt{\frac{(bc-ad)(-dg+ch)\left(-\frac{b}{bc-ad} + \frac{1}{c+dx}\right)}{-bdg+adh}} \right. \\
 & \left. \left(-\frac{f}{-de+cf} + \frac{1}{c+dx}\right) \sqrt{\frac{-\frac{h}{-dg+ch} + \frac{1}{c+dx}}{\frac{f}{-de+cf} - \frac{h}{-dg+ch}}} \right. \\
 & \left. \left( \left( (-bdg+adh) \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\sqrt{\frac{(de-cf)\left(h + \frac{dg}{c+dx} - \frac{ch}{c+dx}\right)}{d(-fg+eh)}}\right], \right. \right. \right. \right. \\
 & \left. \left. \left. \frac{(bc-ad)(-fg+eh)}{(-de+cf)(-bg+ah)} \right] \right) / \left( (bc-ad)(-dg+ch) \right) - \frac{1}{bc-ad} b \operatorname{EllipticF}\left[ \right. \right. \\
 & \left. \left. \operatorname{ArcSin}\left[\sqrt{\frac{(de-cf)\left(h + \frac{dg}{c+dx} - \frac{ch}{c+dx}\right)}{d(-fg+eh)}}\right], \frac{(bc-ad)(-fg+eh)}{(-de+cf)(-bg+ah)} \right] \right) \right) /
 \end{aligned}$$

$$\begin{aligned}
 & \left( \sqrt{\frac{-\frac{f}{-de+cf} + \frac{1}{c+dx}}{-\frac{f}{-de+cf} + \frac{h}{-dg+ch}}} \sqrt{\left(b + \frac{-bc+ad}{c+dx}\right) \left(f + \frac{de-cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} \right) + \\
 & \left( f \sqrt{\frac{-\frac{b}{bc-ad} + \frac{1}{c+dx}}{-\frac{b}{bc-ad} + \frac{h}{-dg+ch}}} \sqrt{\frac{-\frac{f}{-de+cf} + \frac{1}{c+dx}}{-\frac{f}{-de+cf} + \frac{h}{-dg+ch}}} \left(-\frac{h}{-dg+ch} + \frac{1}{c+dx}\right) \right. \\
 & \quad \left. \text{EllipticF}\left[\text{ArcSin}\left[\sqrt{\frac{(-de+cf) \left(-h - \frac{dg}{c+dx} + \frac{ch}{c+dx}\right)}{d(-fg+eh)}}\right], \frac{(bc-ad)(-fg+eh)}{(-de+cf)(-bg+ah)}\right] \right) / \\
 & \left( \sqrt{\frac{-\frac{h}{-dg+ch} + \frac{1}{c+dx}}{\frac{f}{-de+cf} - \frac{h}{-dg+ch}}} \sqrt{\left(b + \frac{-bc+ad}{c+dx}\right) \left(f + \frac{de-cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} \right) / \\
 & \left( 2fh^2 (fg-eh) \left(b - \frac{bc}{c+dx} + \frac{ad}{c+dx}\right) \sqrt{e + \frac{(c+dx) \left(f - \frac{cf}{c+dx}\right)}{d}} \right. \\
 & \quad \left. \sqrt{g + \frac{(c+dx) \left(h - \frac{ch}{c+dx}\right)}{d}} \right) - \\
 & \left( d (be-af) (de-cf) (Bfg+Beh-2Afh) \sqrt{c+dx} \right. \\
 & \quad \sqrt{\left( \left(b - \frac{bc}{c+dx} + \frac{ad}{c+dx}\right) \left(f + \frac{de}{c+dx} - \frac{cf}{c+dx}\right) \left(h + \frac{dg}{c+dx} - \frac{ch}{c+dx}\right) \right)} \\
 & \quad \sqrt{a + \frac{(c+dx) \left(b - \frac{bc}{c+dx}\right)}{d}} \\
 & \quad \left( dg \sqrt{\frac{(bc-ad)(-dg+ch) \left(-\frac{b}{bc-ad} + \frac{1}{c+dx}\right)}{-bdg+adh}} \right. \\
 & \quad \left. \left(-\frac{f}{-de+cf} + \frac{1}{c+dx}\right) \sqrt{\frac{-\frac{h}{-dg+ch} + \frac{1}{c+dx}}{\frac{f}{-de+cf} - \frac{h}{-dg+ch}}} \right)
 \end{aligned}$$

$$\left( \left( (-bdg + adh) \operatorname{EllipticE} \left[ \operatorname{ArcSin} \left[ \sqrt{\frac{(de - cf) \left( h + \frac{dg}{c+dx} - \frac{ch}{c+dx} \right)}{d(-fg + eh)}} \right], \right. \right. \right.$$

$$\left. \left. \frac{(bc - ad)(-fg + eh)}{(-de + cf)(-bg + ah)} \right] \right) / \left( (bc - ad)(-dg + ch) \right) - \frac{1}{bc - ad} b \operatorname{EllipticF} \left[ \right.$$

$$\left. \operatorname{ArcSin} \left[ \sqrt{\frac{(de - cf) \left( h + \frac{dg}{c+dx} - \frac{ch}{c+dx} \right)}{d(-fg + eh)}} \right], \frac{(bc - ad)(-fg + eh)}{(-de + cf)(-bg + ah)} \right] \right) /$$

$$\left( \sqrt{\frac{-\frac{f}{-de+cf} + \frac{1}{c+dx}}{-\frac{f}{-de+cf} + \frac{h}{-dg+ch}}} \sqrt{\left( b + \frac{-bc+ad}{c+dx} \right) \left( f + \frac{de-cf}{c+dx} \right) \left( h + \frac{dg-ch}{c+dx} \right)} \right) -$$

$$\left( ch \sqrt{\frac{(bc - ad)(-dg + ch) \left( -\frac{b}{bc - ad} + \frac{1}{c + dx} \right)}{-bdg + adh}} \right.$$

$$\left. \left( -\frac{f}{-de + cf} + \frac{1}{c + dx} \right) \sqrt{\frac{-\frac{h}{-dg + ch} + \frac{1}{c + dx}}{\frac{f}{-de + cf} - \frac{h}{-dg + ch}}} \right)$$

$$\left( \left( (-bdg + adh) \operatorname{EllipticE} \left[ \operatorname{ArcSin} \left[ \sqrt{\frac{(de - cf) \left( h + \frac{dg}{c+dx} - \frac{ch}{c+dx} \right)}{d(-fg + eh)}} \right], \right. \right. \right.$$

$$\left. \left. \frac{(bc - ad)(-fg + eh)}{(-de + cf)(-bg + ah)} \right] \right) / \left( (bc - ad)(-dg + ch) \right) - \frac{1}{bc - ad} b \operatorname{EllipticF} \left[ \right.$$

$$\left. \operatorname{ArcSin} \left[ \sqrt{\frac{(de - cf) \left( h + \frac{dg}{c+dx} - \frac{ch}{c+dx} \right)}{d(-fg + eh)}} \right], \frac{(bc - ad)(-fg + eh)}{(-de + cf)(-bg + ah)} \right] \right) /$$

$$\left( \sqrt{\frac{-\frac{f}{-de+cf} + \frac{1}{c+dx}}{-\frac{f}{-de+cf} + \frac{h}{-dg+ch}}} \sqrt{\left( b + \frac{-bc+ad}{c+dx} \right) \left( f + \frac{de-cf}{c+dx} \right) \left( h + \frac{dg-ch}{c+dx} \right)} \right) +$$

$$\left( h \sqrt{\frac{-\frac{b}{bc-ad} + \frac{1}{c+dx}}{-\frac{b}{bc-ad} + \frac{h}{-dg+ch}}} \sqrt{\frac{-\frac{f}{-de+cf} + \frac{1}{c+dx}}{-\frac{f}{-de+cf} + \frac{h}{-dg+ch}}} \left( -\frac{h}{-dg + ch} + \frac{1}{c + dx} \right) \right)$$

$$\begin{aligned}
 & \left. \text{EllipticF}\left[\text{ArcSin}\left[\sqrt{\frac{(-de+cf)\left(-h-\frac{dg}{c+dx}+\frac{ch}{c+dx}\right)}{d(-fg+eh)}}\right], \frac{(bc-ad)(-fg+eh)}{(-de+cf)(-bg+ah)}\right]\right/ \\
 & \left(\sqrt{\left(\frac{-\frac{h}{-dg+ch}+\frac{1}{c+dx}}{\frac{f}{-de+cf}-\frac{h}{-dg+ch}}\sqrt{\left(b+\frac{-bc+ad}{c+dx}\right)\left(f+\frac{de-cf}{c+dx}\right)\left(h+\frac{dg-ch}{c+dx}\right)}\right)}\right) \\
 & \left(2f^2h(fg-eh)\left(b-\frac{bc}{c+dx}+\frac{ad}{c+dx}\right)\sqrt{e+\frac{(c+dx)\left(f-\frac{cf}{c+dx}\right)}{d}}\right. \\
 & \left.\sqrt{g+\frac{(c+dx)\left(h-\frac{ch}{c+dx}\right)}{d}}\right) - \\
 & \frac{1}{2f^2h^2\left(b-\frac{bc}{c+dx}+\frac{ad}{c+dx}\right)\sqrt{e+\frac{(c+dx)\left(f-\frac{cf}{c+dx}\right)}{d}}\sqrt{g+\frac{(c+dx)\left(h-\frac{ch}{c+dx}\right)}{d}}} \\
 & \frac{(bBdfg+bBdeh+bBcfh-2Abdfh-aBdfh)}{\sqrt{c+dx}} \\
 & \sqrt{\left(\left(b-\frac{bc}{c+dx}+\frac{ad}{c+dx}\right)\left(f+\frac{de}{c+dx}-\frac{cf}{c+dx}\right)\left(h+\frac{dg}{c+dx}-\frac{ch}{c+dx}\right)\right)} \\
 & \sqrt{a+\frac{(c+dx)\left(b-\frac{bc}{c+dx}\right)}{d}} \\
 & \left(\left(d^2eg\sqrt{-\frac{(bc-ad)(-dg+ch)\left(-\frac{b}{bc-ad}+\frac{1}{c+dx}\right)}{-bdg+adh}}\right.\right. \\
 & \left.\left(-\frac{f}{-de+cf}+\frac{1}{c+dx}\right)\sqrt{\frac{-\frac{h}{-dg+ch}+\frac{1}{c+dx}}{\frac{f}{-de+cf}-\frac{h}{-dg+ch}}}\right) \\
 & \left(\left(-bdg+adh\right)\text{EllipticE}\left[\text{ArcSin}\left[\sqrt{\frac{(de-cf)\left(h+\frac{dg}{c+dx}-\frac{ch}{c+dx}\right)}{d(-fg+eh)}}\right], \right. \right. \\
 & \left. \left.\frac{(bc-ad)(-fg+eh)}{(-de+cf)(-bg+ah)}\right]\right) / \left((bc-ad)(-dg+ch)\right) - \frac{1}{bc-ad}b\text{EllipticF}[
 \end{aligned}$$

$$\begin{aligned}
 & \left. \left( \text{ArcSin} \left[ \sqrt{\frac{(de - cf) \left( h + \frac{dg}{c+dx} - \frac{ch}{c+dx} \right)}{d(-fg + eh)}}, \frac{(bc - ad)(-fg + eh)}{(-de + cf)(-bg + ah)} \right] \right) \right) / \\
 & \left( \sqrt{\frac{-\frac{f}{-de+cf} + \frac{1}{c+dx}}{-\frac{f}{-de+cf} + \frac{h}{-dg+ch}}} \sqrt{\left( b + \frac{-bc+ad}{c+dx} \right) \left( f + \frac{de-cf}{c+dx} \right) \left( h + \frac{dg-ch}{c+dx} \right)} \right) - \\
 & \left( cd fg \sqrt{-\frac{(bc - ad)(-dg + ch) \left( -\frac{b}{bc-ad} + \frac{1}{c+dx} \right)}{-bdg + adh}} \right. \\
 & \left. \left( -\frac{f}{-de+cf} + \frac{1}{c+dx} \right) \sqrt{\frac{-\frac{h}{-dg+ch} + \frac{1}{c+dx}}{\frac{f}{-de+cf} - \frac{h}{-dg+ch}}} \right. \\
 & \left. \left( (-bdg + adh) \text{EllipticE} \left[ \text{ArcSin} \left[ \sqrt{\frac{(de - cf) \left( h + \frac{dg}{c+dx} - \frac{ch}{c+dx} \right)}{d(-fg + eh)}}, \right. \right. \right. \right. \\
 & \left. \left. \left. \frac{(bc - ad)(-fg + eh)}{(-de + cf)(-bg + ah)} \right] \right) \right) / \left( (bc - ad)(-dg + ch) - \frac{1}{bc - ad} b \text{EllipticF} \left[ \right. \right. \\
 & \left. \left. \text{ArcSin} \left[ \sqrt{\frac{(de - cf) \left( h + \frac{dg}{c+dx} - \frac{ch}{c+dx} \right)}{d(-fg + eh)}}, \frac{(bc - ad)(-fg + eh)}{(-de + cf)(-bg + ah)} \right] \right) \right) / \\
 & \left( \sqrt{\frac{-\frac{f}{-de+cf} + \frac{1}{c+dx}}{-\frac{f}{-de+cf} + \frac{h}{-dg+ch}}} \sqrt{\left( b + \frac{-bc+ad}{c+dx} \right) \left( f + \frac{de-cf}{c+dx} \right) \left( h + \frac{dg-ch}{c+dx} \right)} \right) - \\
 & \left( cde h \sqrt{-\frac{(bc - ad)(-dg + ch) \left( -\frac{b}{bc-ad} + \frac{1}{c+dx} \right)}{-bdg + adh}} \right. \\
 & \left. \left( -\frac{f}{-de+cf} + \frac{1}{c+dx} \right) \sqrt{\frac{-\frac{h}{-dg+ch} + \frac{1}{c+dx}}{\frac{f}{-de+cf} - \frac{h}{-dg+ch}}} \right. \\
 & \left. \left( (-bdg + adh) \text{EllipticE} \left[ \text{ArcSin} \left[ \sqrt{\frac{(de - cf) \left( h + \frac{dg}{c+dx} - \frac{ch}{c+dx} \right)}{d(-fg + eh)}}, \right. \right. \right. \right. \\
 & \left. \left. \left. \frac{(bc - ad)(-fg + eh)}{(-de + cf)(-bg + ah)} \right] \right) \right) /
 \end{aligned}$$

$$\left. \left. \left. \left. \frac{(bc-ad)(-fg+eh)}{(-de+cf)(-bg+ah)} \right] \right) / \left( (bc-ad)(-dg+ch) \right) - \frac{1}{bc-ad} b \text{EllipticF} \left[ \right. \right.$$

$$\left. \left. \left. \left. \text{ArcSin} \left[ \sqrt{\frac{(de-cf) \left( h + \frac{dg}{c+dx} - \frac{ch}{c+dx} \right)}{d(-fg+eh)}} \right], \frac{(bc-ad)(-fg+eh)}{(-de+cf)(-bg+ah)} \right] \right) \right) / \right.$$

$$\left( \sqrt{\frac{-\frac{f}{-de+cf} + \frac{1}{c+dx}}{-\frac{f}{-de+cf} + \frac{h}{-dg+ch}}} \sqrt{\left( b + \frac{-bc+ad}{c+dx} \right) \left( f + \frac{de-cf}{c+dx} \right) \left( h + \frac{dg-ch}{c+dx} \right)} \right) +$$

$$\left( c^2 f h \sqrt{-\frac{(bc-ad)(-dg+ch) \left( -\frac{b}{bc-ad} + \frac{1}{c+dx} \right)}{-bdg+adh}} \right.$$

$$\left. \left( -\frac{f}{-de+cf} + \frac{1}{c+dx} \right) \sqrt{\frac{-\frac{h}{-dg+ch} + \frac{1}{c+dx}}{\frac{f}{-de+cf} - \frac{h}{-dg+ch}}} \right.$$

$$\left. \left( \left( (-bdg+adh) \text{EllipticE} \left[ \text{ArcSin} \left[ \sqrt{\frac{(de-cf) \left( h + \frac{dg}{c+dx} - \frac{ch}{c+dx} \right)}{d(-fg+eh)}} \right], \right. \right. \right.$$

$$\left. \left. \left. \left. \frac{(bc-ad)(-fg+eh)}{(-de+cf)(-bg+ah)} \right] \right) / \left( (bc-ad)(-dg+ch) \right) - \frac{1}{bc-ad} b \text{EllipticF} \left[ \right. \right.$$

$$\left. \left. \left. \left. \text{ArcSin} \left[ \sqrt{\frac{(de-cf) \left( h + \frac{dg}{c+dx} - \frac{ch}{c+dx} \right)}{d(-fg+eh)}} \right], \frac{(bc-ad)(-fg+eh)}{(-de+cf)(-bg+ah)} \right] \right) \right) / \right.$$

$$\left( \sqrt{\frac{-\frac{f}{-de+cf} + \frac{1}{c+dx}}{-\frac{f}{-de+cf} + \frac{h}{-dg+ch}}} \sqrt{\left( b + \frac{-bc+ad}{c+dx} \right) \left( f + \frac{de-cf}{c+dx} \right) \left( h + \frac{dg-ch}{c+dx} \right)} \right) +$$

$$\left( d f g \sqrt{\frac{-\frac{b}{bc-ad} + \frac{1}{c+dx}}{-\frac{b}{bc-ad} + \frac{h}{-dg+ch}}} \sqrt{\frac{-\frac{f}{-de+cf} + \frac{1}{c+dx}}{-\frac{f}{-de+cf} + \frac{h}{-dg+ch}}} \left( -\frac{h}{-dg+ch} + \frac{1}{c+dx} \right) \right.$$

$$\left. \left. \left. \left. \text{EllipticF} \left[ \text{ArcSin} \left[ \sqrt{\frac{(-de+cf) \left( -h - \frac{dg}{c+dx} + \frac{ch}{c+dx} \right)}{d(-fg+eh)}} \right], \frac{(bc-ad)(-fg+eh)}{(-de+cf)(-bg+ah)} \right] \right) \right) / \right.$$

$$\begin{aligned}
 & \left( \sqrt{\frac{-\frac{h}{-dg+ch} + \frac{1}{c+dx}}{\frac{f}{-de+cf} - \frac{h}{-dg+ch}}} \sqrt{\left(b + \frac{-bc+ad}{c+dx}\right) \left(f + \frac{de-cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} \right) + \\
 & \left( de h \sqrt{\frac{-\frac{b}{bc-ad} + \frac{1}{c+dx}}{-\frac{b}{bc-ad} + \frac{h}{-dg+ch}}} \sqrt{\frac{-\frac{f}{-de+cf} + \frac{1}{c+dx}}{-\frac{f}{-de+cf} + \frac{h}{-dg+ch}}} \left(-\frac{h}{-dg+ch} + \frac{1}{c+dx}\right) \right. \\
 & \left. \text{EllipticF}\left[\text{ArcSin}\left[\sqrt{\frac{(-de+cf) \left(-h - \frac{dg}{c+dx} + \frac{ch}{c+dx}\right)}{d(-fg+eh)}}\right], \frac{(bc-ad)(-fg+eh)}{(-de+cf)(-bg+ah)}\right] \right) / \\
 & \left( \sqrt{\frac{-\frac{h}{-dg+ch} + \frac{1}{c+dx}}{\frac{f}{-de+cf} - \frac{h}{-dg+ch}}} \sqrt{\left(b + \frac{-bc+ad}{c+dx}\right) \left(f + \frac{de-cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} \right) - \\
 & \left( 2cfh \sqrt{\frac{-\frac{b}{bc-ad} + \frac{1}{c+dx}}{-\frac{b}{bc-ad} + \frac{h}{-dg+ch}}} \sqrt{\frac{-\frac{f}{-de+cf} + \frac{1}{c+dx}}{-\frac{f}{-de+cf} + \frac{h}{-dg+ch}}} \left(-\frac{h}{-dg+ch} + \frac{1}{c+dx}\right) \right. \\
 & \left. \text{EllipticF}\left[\text{ArcSin}\left[\sqrt{\frac{(-de+cf) \left(-h - \frac{dg}{c+dx} + \frac{ch}{c+dx}\right)}{d(-fg+eh)}}\right], \frac{(bc-ad)(-fg+eh)}{(-de+cf)(-bg+ah)}\right] \right) / \\
 & \left( \sqrt{\frac{-\frac{h}{-dg+ch} + \frac{1}{c+dx}}{\frac{f}{-de+cf} - \frac{h}{-dg+ch}}} \sqrt{\left(b + \frac{-bc+ad}{c+dx}\right) \left(f + \frac{de-cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} \right) - \\
 & \left( f(-dg+ch) \left(-\frac{f}{-de+cf} + \frac{h}{-dg+ch}\right) \sqrt{\frac{-\frac{b}{bc-ad} + \frac{1}{c+dx}}{-\frac{b}{bc-ad} + \frac{h}{-dg+ch}}} \right. \\
 & \left. \sqrt{\frac{\left(-\frac{f}{-de+cf} + \frac{1}{c+dx}\right) \left(-\frac{h}{-dg+ch} + \frac{1}{c+dx}\right)}{\left(-\frac{f}{-de+cf} + \frac{h}{-dg+ch}\right)^2}} \text{EllipticPi}\left[-\frac{-dfg+deh}{(-de+cf)h}, \right. \right. \\
 & \left. \left. \text{ArcSin}\left[\sqrt{\frac{(-de+cf) \left(-h - \frac{dg}{c+dx} + \frac{ch}{c+dx}\right)}{d(-fg+eh)}}\right], \frac{(bc-ad)(-fg+eh)}{(-de+cf)(-bg+ah)}\right] \right) /
 \end{aligned}$$

$$\left( \sqrt{\left( b + \frac{-bc+ad}{c+dx} \right) \left( f + \frac{de-cf}{c+dx} \right) \left( h + \frac{dg-ch}{c+dx} \right)} \right)$$

**Problem 9: Result more than twice size of optimal antiderivative.**

$$\int \frac{A+Bx}{(a+bx)^{3/2} \sqrt{c+dx} \sqrt{e+fx} \sqrt{g+hx}} dx$$

Optimal (type 4, 606 leaves, 7 steps):

$$\frac{2(Ab-aB)d\sqrt{a+bx}\sqrt{e+fx}\sqrt{g+hx}}{(bc-ad)(be-af)(bg-ah)\sqrt{c+dx}} - \frac{2b(Ab-aB)\sqrt{c+dx}\sqrt{e+fx}\sqrt{g+hx}}{(bc-ad)(be-af)(bg-ah)\sqrt{a+bx}}$$

$$\left( 2(Ab-aB)\sqrt{dg-ch}\sqrt{fg-eh}\sqrt{a+bx} \sqrt{-\frac{(de-cf)(g+hx)}{(fg-eh)(c+dx)}} \right)$$

$$\text{EllipticE}\left[\text{ArcSin}\left[\frac{\sqrt{dg-ch}\sqrt{e+fx}}{\sqrt{fg-eh}\sqrt{c+dx}}\right], \frac{(bc-ad)(fg-eh)}{(be-af)(dg-ch)}\right] /$$

$$\left( (bc-ad)(be-af)(bg-ah) \sqrt{\frac{(de-cf)(a+bx)}{(be-af)(c+dx)}} \sqrt{g+hx} \right) +$$

$$\left( 2(Bc-Ad) \sqrt{\frac{(be-af)(c+dx)}{(de-cf)(a+bx)}} \sqrt{g+hx} \right)$$

$$\text{EllipticF}\left[\text{ArcSin}\left[\frac{\sqrt{bg-ah}\sqrt{e+fx}}{\sqrt{fg-eh}\sqrt{a+bx}}\right], -\frac{(bc-ad)(fg-eh)}{(de-cf)(bg-ah)}\right] /$$

$$\left( (bc-ad)\sqrt{bg-ah}\sqrt{fg-eh}\sqrt{c+dx} \sqrt{-\frac{(be-af)(g+hx)}{(fg-eh)(a+bx)}} \right)$$

Result (type 4, 1749 leaves):

$$-\frac{2b(Ab-aB)\sqrt{c+dx}\sqrt{e+fx}\sqrt{g+hx}}{(bc-ad)(be-af)(bg-ah)\sqrt{a+bx}} + \frac{1}{b^2(-bc+ad)(-be+af)(-bg+ah)}$$

$$\left( \left( 2(Ab-aB)(a+bx)^{5/2} \left( d + \frac{bc}{a+bx} - \frac{ad}{a+bx} \right) \left( f + \frac{be}{a+bx} - \frac{af}{a+bx} \right) \left( h + \frac{bg}{a+bx} - \frac{ah}{a+bx} \right) \right) / \right)$$

$$\begin{aligned}
 & \left( \sqrt{c + \frac{(a+bx)(d - \frac{ad}{a+bx})}{b}} \sqrt{e + \frac{(a+bx)(f - \frac{af}{a+bx})}{b}} \sqrt{g + \frac{(a+bx)(h - \frac{ah}{a+bx})}{b}} \right) - \\
 & \frac{1}{\sqrt{c + \frac{(a+bx)(d - \frac{ad}{a+bx})}{b}} \sqrt{e + \frac{(a+bx)(f - \frac{af}{a+bx})}{b}} \sqrt{g + \frac{(a+bx)(h - \frac{ah}{a+bx})}{b}}} 2 (bc - ad) (be - af) \\
 & (bg - ah) (a+bx)^{3/2} \sqrt{\left( \left( d + \frac{bc}{a+bx} - \frac{ad}{a+bx} \right) \left( f + \frac{be}{a+bx} - \frac{af}{a+bx} \right) \left( h + \frac{bg}{a+bx} - \frac{ah}{a+bx} \right) \right)} \\
 & \left( - \left( \left( A b \sqrt{\frac{(bc - ad)(bg - ah) \left( -\frac{d}{-bc+ad} + \frac{1}{a+bx} \right)}{bdg - bch}} \left( -\frac{f}{-be+af} + \frac{1}{a+bx} \right) \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{\frac{f}{-be+af} - \frac{h}{-bg+ah}}} \right. \right. \right. \\
 & \left. \left. \left. - \left( (bdg - bch) \text{EllipticE} \left[ \text{ArcSin} \left[ \sqrt{\frac{(be - af) \left( h + \frac{bg}{a+bx} - \frac{ah}{a+bx} \right)}{b(-fg + eh)}} \right], \right. \right. \right. \right. \\
 & \left. \left. \left. \frac{(-bc + ad)(-fg + eh)}{(-be + af)(-dg + ch)} \right] \right) / ((bc - ad)(bg - ah)) \right) - \\
 & \frac{1}{-bc + ad} d \text{EllipticF} \left[ \text{ArcSin} \left[ \sqrt{\frac{(be - af) \left( h + \frac{bg}{a+bx} - \frac{ah}{a+bx} \right)}{b(-fg + eh)}} \right], \right. \\
 & \left. \left. \left. \frac{(-bc + ad)(-fg + eh)}{(-be + af)(-dg + ch)} \right] \right) \right] / \\
 & \left( \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \sqrt{\left( d + \frac{bc - ad}{a+bx} \right) \left( f + \frac{be - af}{a+bx} \right) \left( h + \frac{bg - ah}{a+bx} \right)} \right) + \\
 & \left( A B \sqrt{\frac{(bc - ad)(bg - ah) \left( -\frac{d}{-bc+ad} + \frac{1}{a+bx} \right)}{bdg - bch}} \left( -\frac{f}{-be+af} + \frac{1}{a+bx} \right) \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{\frac{f}{-be+af} - \frac{h}{-bg+ah}}} \right. \\
 & \left. \left( - \left( (bdg - bch) \text{EllipticE} \left[ \text{ArcSin} \left[ \sqrt{\frac{(be - af) \left( h + \frac{bg}{a+bx} - \frac{ah}{a+bx} \right)}{b(-fg + eh)}} \right], \right. \right. \right. \right. \right.
 \end{aligned}$$

$$\left. \left. \left. \left. \left. \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right/ \left( (bc-ad)(bg-ah) \right) \right) - \frac{1}{-bc+ad} \right. \\
 \left. d \operatorname{EllipticF} \left[ \operatorname{ArcSin} \left[ \sqrt{\frac{(be-af) \left( h + \frac{bg}{a+bx} - \frac{ah}{a+bx} \right)}{b(-fg+eh)}} \right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right] \right/ \\
 \left( \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \sqrt{\left( d + \frac{bc-ad}{a+bx} \right) \left( f + \frac{be-af}{a+bx} \right) \left( h + \frac{bg-ah}{a+bx} \right)} \right) - \\
 \left( B \sqrt{\frac{-\frac{d}{-bc+ad} + \frac{1}{a+bx}}{-\frac{d}{-bc+ad} + \frac{h}{-bg+ah}}} \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \left( -\frac{h}{-bg+ah} + \frac{1}{a+bx} \right) \right) \\
 \left. \operatorname{EllipticF} \left[ \operatorname{ArcSin} \left[ \sqrt{\frac{(-be+af) \left( -h - \frac{bg}{a+bx} + \frac{ah}{a+bx} \right)}{b(-fg+eh)}} \right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right] \right/ \\
 \left( \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{\frac{f}{-be+af} - \frac{h}{-bg+ah}}} \sqrt{\left( d + \frac{bc-ad}{a+bx} \right) \left( f + \frac{be-af}{a+bx} \right) \left( h + \frac{bg-ah}{a+bx} \right)} \right) \right)$$

**Problem 10: Result more than twice size of optimal antiderivative.**

$$\int \frac{A+Bx}{(a+bx)^{5/2} \sqrt{c+dx} \sqrt{e+fx} \sqrt{g+hx}} dx$$

Optimal (type 4, 1081 leaves, 8 steps):

$$\begin{aligned}
 & \left( 2d (3a^3 Bdfh + b^3 (3Bceg - 2A(deg + cfg + ceh))) - ab^2 \right. \\
 & \quad \left. (B(deg + cfg + ceh) - 4A(dfg + deh + cfh)) - a^2 b (6Adfh + B(dfg + deh + cfh))) \right) \\
 & \quad \sqrt{a+bx} \sqrt{e+fx} \sqrt{g+hx} \Big/ \left( 3(bc-ad)^2 (be-af)^2 (bg-ah)^2 \sqrt{c+dx} \right) - \\
 & \quad \frac{2b(Ab-aB) \sqrt{c+dx} \sqrt{e+fx} \sqrt{g+hx}}{3(bc-ad)(be-af)(bg-ah)(a+bx)^{3/2}} - \\
 & \left( 2b (3a^3 Bdfh + b^3 (3Bceg - 2A(deg + cfg + ceh))) - ab^2 \right. \\
 & \quad \left. (B(deg + cfg + ceh) - 4A(dfg + deh + cfh)) - a^2 b (6Adfh + B(dfg + deh + cfh))) \right) \\
 & \quad \sqrt{c+dx} \sqrt{e+fx} \sqrt{g+hx} \Big/ \left( 3(bc-ad)^2 (be-af)^2 (bg-ah)^2 \sqrt{a+bx} \right) - \\
 & \left( 2\sqrt{dg-ch} \sqrt{fg-eh} (3a^3 Bdfh + b^3 (3Bceg - 2A(deg + cfg + ceh))) - \right. \\
 & \quad \left. ab^2 (B(deg + cfg + ceh) - 4A(dfg + deh + cfh)) - \right. \\
 & \quad \left. a^2 b (6Adfh + B(dfg + deh + cfh))) \sqrt{a+bx} \sqrt{-\frac{(de-cf)(g+hx)}{(fg-eh)(c+dx)}} \right. \\
 & \quad \left. \text{EllipticE}\left[\text{ArcSin}\left[\frac{\sqrt{dg-ch} \sqrt{e+fx}}{\sqrt{fg-eh} \sqrt{c+dx}}\right], \frac{(bc-ad)(fg-eh)}{(be-af)(dg-ch)}\right] \right) \Big/ \\
 & \left( 3(bc-ad)^2 (be-af)^2 (bg-ah)^2 \sqrt{\frac{(de-cf)(a+bx)}{(be-af)(c+dx)}} \sqrt{g+hx} \right) - \\
 & \left( 2(3a^2 d (Bc-Ad) fh + b^2 (3Bcdeg - A(2d^2 eg - c^2 fh + cd(fg+eh)))) + \right. \\
 & \quad \left. ab(3Ad^2 (fg+eh) - B(d^2 eg + c^2 fh + 2cd(fg+eh))) \sqrt{\frac{(be-af)(c+dx)}{(de-cf)(a+bx)}} \right. \\
 & \quad \left. \sqrt{g+hx} \text{EllipticF}\left[\text{ArcSin}\left[\frac{\sqrt{bg-ah} \sqrt{e+fx}}{\sqrt{fg-eh} \sqrt{a+bx}}\right], -\frac{(bc-ad)(fg-eh)}{(de-cf)(bg-ah)}\right] \right) \Big/ \\
 & \left( 3(bc-ad)^2 (be-af)(bg-ah)^{3/2} \sqrt{fg-eh} \sqrt{c+dx} \sqrt{-\frac{(be-af)(g+hx)}{(fg-eh)(a+bx)}} \right)
 \end{aligned}$$

Result (type 4, 10637 leaves):

$$\begin{aligned}
 & \sqrt{a+bx} \sqrt{c+dx} \sqrt{e+fx} \sqrt{g+hx} \\
 & \left( -\frac{2b(Ab-aB)}{3(bc-ad)(be-af)(bg-ah)(a+bx)^2} - (2b(3b^3 Bceg - 2Ab^3 deg - ab^2 Bdeg - \right. \\
 & \quad 2Ab^3 cfg - ab^2 Bcfg + 4aAb^2 dfg - a^2 bBdfg - 2Ab^3 ceh - ab^2 Bceh + \\
 & \quad \left. 4aAb^2 deh - a^2 bBdeh + 4aAb^2 cfh - a^2 bBcfh - 6a^2 Abdfh + 3a^3 Bdfh)) \Big/
 \end{aligned}$$

$$\begin{aligned}
 & \left( 3 (bc - ad)^2 (be - af)^2 (bg - ah)^2 (a + bx) \right) + \\
 & \frac{1}{3b^2 (-bc + ad)^2 (-be + af)^2 (-bg + ah)^2} \\
 & 2 \left( \left( 3b^3 Bceg - 2Ab^3 deg - ab^2 Bdeg - 2Ab^3 cfg - ab^2 Bcfg + \right. \right. \\
 & \quad \left. \left. 4aAb^2 dfg - a^2 bBdfg - 2Ab^3 ceh - ab^2 Bceh + 4aAb^2 deh - \right. \right. \\
 & \quad \left. \left. a^2 bBdeh + 4aAb^2 cfh - a^2 bBcfh - 6a^2 Abd fh + 3a^3 Bdfh \right) \right) / \\
 & \left( (a + bx)^{5/2} \left( d + \frac{bc}{a + bx} - \frac{ad}{a + bx} \right) \left( f + \frac{be}{a + bx} - \frac{af}{a + bx} \right) \left( h + \frac{bg}{a + bx} - \frac{ah}{a + bx} \right) \right) / \\
 & \left( \sqrt{c + \frac{(a + bx) \left( d - \frac{ad}{a + bx} \right)}{b}} \sqrt{e + \frac{(a + bx) \left( f - \frac{af}{a + bx} \right)}{b}} \sqrt{g + \frac{(a + bx) \left( h - \frac{ah}{a + bx} \right)}{b}} \right) + \\
 & \frac{1}{\sqrt{c + \frac{(a + bx) \left( d - \frac{ad}{a + bx} \right)}{b}} \sqrt{e + \frac{(a + bx) \left( f - \frac{af}{a + bx} \right)}{b}} \sqrt{g + \frac{(a + bx) \left( h - \frac{ah}{a + bx} \right)}{b}}} (bc - ad) (be - af) \\
 & (bg - ah) (a + bx)^{3/2} \sqrt{\left( \left( d + \frac{bc}{a + bx} - \frac{ad}{a + bx} \right) \left( f + \frac{be}{a + bx} - \frac{af}{a + bx} \right) \left( h + \frac{bg}{a + bx} - \frac{ah}{a + bx} \right) \right)} \\
 & \left( - \left( \left( 3b^3 Bceg \sqrt{\frac{(bc - ad) (bg - ah) \left( -\frac{d}{-bc + ad} + \frac{1}{a + bx} \right)}{bdg - bch}} \right. \right. \right. \\
 & \quad \left. \left. \left( -\frac{f}{-be + af} + \frac{1}{a + bx} \right) \sqrt{\frac{-\frac{h}{-bg + ah} + \frac{1}{a + bx}}{\frac{f}{-be + af} - \frac{h}{-bg + ah}}} \left( - \left( \left( (bdg - bch) \text{EllipticE} \left[ \right. \right. \right. \right. \right. \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \text{ArcSin} \left[ \sqrt{\frac{(be - af) \left( h + \frac{bg}{a + bx} - \frac{ah}{a + bx} \right)}{b (-fg + eh)}} \right], \frac{(-bc + ad) (-fg + eh)}{(-be + af) (-dg + ch)} \right] \right) \right) \right) / \\
 & \left( (bc - ad) (bg - ah) \right) - \frac{1}{-bc + ad} d \text{EllipticF} \left[ \text{ArcSin} \left[ \right. \right. \\
 & \quad \left. \left. \sqrt{\frac{(be - af) \left( h + \frac{bg}{a + bx} - \frac{ah}{a + bx} \right)}{b (-fg + eh)}} \right], \frac{(-bc + ad) (-fg + eh)}{(-be + af) (-dg + ch)} \right] \right) /
 \end{aligned}$$

$$\begin{aligned}
 & \left( \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right) \left(h + \frac{bg-ah}{a+bx}\right)} \right) + \\
 & \left( 2Ab^3deg \sqrt{\frac{(bc-ad)(bg-ah)\left(-\frac{d}{-bc+ad} + \frac{1}{a+bx}\right)}{bdg-bch}} \left(-\frac{f}{-be+af} + \frac{1}{a+bx}\right) \right. \\
 & \left. \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{\frac{f}{-be+af} - \frac{h}{-bg+ah}}} \left( - \left( (bdg-bch) \text{EllipticE} \left[ \right. \right. \right. \right. \\
 & \left. \left. \left. \left. \text{ArcSin} \left[ \sqrt{\frac{(be-af)\left(h + \frac{bg}{a+bx} - \frac{ah}{a+bx}\right)}{b(-fg+eh)}} \right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right) \right) \right) / \\
 & \left( (bc-ad)(bg-ah) \right) - \frac{1}{-bc+ad} d \text{EllipticF} \left[ \text{ArcSin} \left[ \right. \right. \\
 & \left. \left. \sqrt{\frac{(be-af)\left(h + \frac{bg}{a+bx} - \frac{ah}{a+bx}\right)}{b(-fg+eh)}} \right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right) / \\
 & \left( \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right) \left(h + \frac{bg-ah}{a+bx}\right)} \right) + \\
 & \left( ab^2Bdeg \sqrt{\frac{(bc-ad)(bg-ah)\left(-\frac{d}{-bc+ad} + \frac{1}{a+bx}\right)}{bdg-bch}} \left(-\frac{f}{-be+af} + \frac{1}{a+bx}\right) \right. \\
 & \left. \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{\frac{f}{-be+af} - \frac{h}{-bg+ah}}} \left( - \left( (bdg-bch) \text{EllipticE} \left[ \right. \right. \right. \right. \\
 & \left. \left. \left. \left. \text{ArcSin} \left[ \sqrt{\frac{(be-af)\left(h + \frac{bg}{a+bx} - \frac{ah}{a+bx}\right)}{b(-fg+eh)}} \right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right) \right) \right) / \\
 & \left( (bc-ad)(bg-ah) \right) - \frac{1}{-bc+ad} d \text{EllipticF} \left[ \text{ArcSin} \left[ \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left. \left( \sqrt{\frac{(be-af) \left( h + \frac{bg}{a+bx} - \frac{ah}{a+bx} \right)}{b(-fg+eh)}} \right), \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \Bigg) / \\
 & \left( \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \sqrt{\left( d + \frac{bc-ad}{a+bx} \right) \left( f + \frac{be-af}{a+bx} \right) \left( h + \frac{bg-ah}{a+bx} \right)} \right) + \\
 & \left( 2Ab^3c f g \sqrt{\frac{(bc-ad)(bg-ah) \left( -\frac{d}{-bc+ad} + \frac{1}{a+bx} \right)}{bdg-bch}} \left( -\frac{f}{-be+af} + \frac{1}{a+bx} \right) \right. \\
 & \left. \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{\frac{f}{-be+af} - \frac{h}{-bg+ah}}} \left( \left( (bdg-bch) \text{EllipticE} \left[ \right. \right. \right. \right. \right. \\
 & \left. \left. \left. \left. \left. \text{ArcSin} \left[ \sqrt{\frac{(be-af) \left( h + \frac{bg}{a+bx} - \frac{ah}{a+bx} \right)}{b(-fg+eh)}} \right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right) \right) \right) / \\
 & \left. \left( (bc-ad)(bg-ah) \right) \right) - \frac{1}{-bc+ad} d \text{EllipticF} \left[ \text{ArcSin} \left[ \right. \right. \right. \right. \\
 & \left. \left. \left. \left. \left. \sqrt{\frac{(be-af) \left( h + \frac{bg}{a+bx} - \frac{ah}{a+bx} \right)}{b(-fg+eh)}} \right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right) \right] \Bigg) / \\
 & \left( \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \sqrt{\left( d + \frac{bc-ad}{a+bx} \right) \left( f + \frac{be-af}{a+bx} \right) \left( h + \frac{bg-ah}{a+bx} \right)} \right) + \\
 & \left( ab^2Bc f g \sqrt{\frac{(bc-ad)(bg-ah) \left( -\frac{d}{-bc+ad} + \frac{1}{a+bx} \right)}{bdg-bch}} \left( -\frac{f}{-be+af} + \frac{1}{a+bx} \right) \right. \\
 & \left. \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{\frac{f}{-be+af} - \frac{h}{-bg+ah}}} \left( \left( (bdg-bch) \text{EllipticE} \left[ \right. \right. \right. \right. \right. \\
 & \left. \left. \left. \left. \left. \text{ArcSin} \left[ \sqrt{\frac{(be-af) \left( h + \frac{bg}{a+bx} - \frac{ah}{a+bx} \right)}{b(-fg+eh)}} \right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right) \right) \right) /
 \end{aligned}$$

$$\begin{aligned}
 & \left( (bc - ad)(bg - ah) \right) - \frac{1}{-bc + ad} d \operatorname{EllipticF} \left[ \operatorname{ArcSin} \left[ \sqrt{\frac{(be - af) \left( h + \frac{bg}{a+bx} - \frac{ah}{a+bx} \right)}{b(-fg + eh)}}, \frac{(-bc + ad)(-fg + eh)}{(-be + af)(-dg + ch)} \right] \right] / \\
 & \left( \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \sqrt{\left( d + \frac{bc - ad}{a + bx} \right) \left( f + \frac{be - af}{a + bx} \right) \left( h + \frac{bg - ah}{a + bx} \right)} \right) - \\
 & \left( 4 a A b^2 d f g \sqrt{\frac{(bc - ad)(bg - ah) \left( -\frac{d}{-bc+ad} + \frac{1}{a+bx} \right)}{bdg - bch}} \left( -\frac{f}{-be + af} + \frac{1}{a + bx} \right) \right. \\
 & \left. \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{\frac{f}{-be+af} - \frac{h}{-bg+ah}}} \left( \left( (bdg - bch) \operatorname{EllipticE} \left[ \operatorname{ArcSin} \left[ \sqrt{\frac{(be - af) \left( h + \frac{bg}{a+bx} - \frac{ah}{a+bx} \right)}{b(-fg + eh)}}, \frac{(-bc + ad)(-fg + eh)}{(-be + af)(-dg + ch)} \right] \right) \right) / \right. \\
 & \left. \left( (bc - ad)(bg - ah) \right) - \frac{1}{-bc + ad} d \operatorname{EllipticF} \left[ \operatorname{ArcSin} \left[ \sqrt{\frac{(be - af) \left( h + \frac{bg}{a+bx} - \frac{ah}{a+bx} \right)}{b(-fg + eh)}}, \frac{(-bc + ad)(-fg + eh)}{(-be + af)(-dg + ch)} \right] \right] / \right. \\
 & \left. \left( \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \sqrt{\left( d + \frac{bc - ad}{a + bx} \right) \left( f + \frac{be - af}{a + bx} \right) \left( h + \frac{bg - ah}{a + bx} \right)} \right) + \\
 & \left( a^2 b B d f g \sqrt{\frac{(bc - ad)(bg - ah) \left( -\frac{d}{-bc+ad} + \frac{1}{a+bx} \right)}{bdg - bch}} \left( -\frac{f}{-be + af} + \frac{1}{a + bx} \right) \right. \\
 & \left. \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{\frac{f}{-be+af} - \frac{h}{-bg+ah}}} \left( \left( (bdg - bch) \operatorname{EllipticE} \left[ \right. \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left. \text{ArcSin} \left[ \sqrt{\frac{(be-af) \left( h + \frac{bg}{a+bx} - \frac{ah}{a+bx} \right)}{b(-fg+eh)}}, \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right/ \\
 & \left. \left( (bc-ad)(bg-ah) \right) - \frac{1}{-bc+ad} d \text{EllipticF} \left[ \text{ArcSin} \left[ \sqrt{\frac{(be-af) \left( h + \frac{bg}{a+bx} - \frac{ah}{a+bx} \right)}{b(-fg+eh)}}, \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right] \right/ \\
 & \left( \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \sqrt{\left( d + \frac{bc-ad}{a+bx} \right) \left( f + \frac{be-af}{a+bx} \right) \left( h + \frac{bg-ah}{a+bx} \right)} \right) + \\
 & \left( 2Ab^3ceh \sqrt{\frac{(bc-ad)(bg-ah) \left( -\frac{d}{-bc+ad} + \frac{1}{a+bx} \right)}{bdg-bch}} \left( -\frac{f}{-be+af} + \frac{1}{a+bx} \right) \right. \\
 & \left. \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{\frac{f}{-be+af} - \frac{h}{-bg+ah}}} \left( - \left( (bdg-bch) \text{EllipticE} \left[ \right. \right. \right. \right. \right. \\
 & \left. \left. \left. \left. \left. \text{ArcSin} \left[ \sqrt{\frac{(be-af) \left( h + \frac{bg}{a+bx} - \frac{ah}{a+bx} \right)}{b(-fg+eh)}}, \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right] \right) \right) \right/ \\
 & \left. \left( (bc-ad)(bg-ah) \right) - \frac{1}{-bc+ad} d \text{EllipticF} \left[ \text{ArcSin} \left[ \sqrt{\frac{(be-af) \left( h + \frac{bg}{a+bx} - \frac{ah}{a+bx} \right)}{b(-fg+eh)}}, \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right] \right) \\
 & \left. \left( \sqrt{\frac{(be-af) \left( h + \frac{bg}{a+bx} - \frac{ah}{a+bx} \right)}{b(-fg+eh)}}, \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right) \right/ \\
 & \left( \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \sqrt{\left( d + \frac{bc-ad}{a+bx} \right) \left( f + \frac{be-af}{a+bx} \right) \left( h + \frac{bg-ah}{a+bx} \right)} \right) + \\
 & \left( ab^2Bceh \sqrt{\frac{(bc-ad)(bg-ah) \left( -\frac{d}{-bc+ad} + \frac{1}{a+bx} \right)}{bdg-bch}} \left( -\frac{f}{-be+af} + \frac{1}{a+bx} \right) \right.
 \end{aligned}$$



$$\begin{aligned}
 & \left( a^2 b B d e h \sqrt{\frac{(bc-ad)(bg-ah)\left(-\frac{d}{-bc+ad} + \frac{1}{a+bx}\right)}{bdg-bch}} \left(-\frac{f}{-be+af} + \frac{1}{a+bx}\right) \right. \\
 & \left. \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{\frac{f}{-be+af} - \frac{h}{-bg+ah}}} \left( \left( (bdg-bch) \text{EllipticE} \left[ \right. \right. \right. \right. \\
 & \left. \left. \left. \left. \text{ArcSin} \left[ \sqrt{\frac{(be-af)\left(h + \frac{bg}{a+bx} - \frac{ah}{a+bx}\right)}{b(-fg+eh)}} \right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right) \right) \right) / \\
 & \left( (bc-ad)(bg-ah) \right) - \frac{1}{-bc+ad} d \text{EllipticF} \left[ \text{ArcSin} \left[ \right. \right. \\
 & \left. \left. \sqrt{\frac{(be-af)\left(h + \frac{bg}{a+bx} - \frac{ah}{a+bx}\right)}{b(-fg+eh)}} \right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right) / \\
 & \left( \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right) \left(h + \frac{bg-ah}{a+bx}\right)} \right) - \\
 & \left( 4 a A b^2 c f h \sqrt{\frac{(bc-ad)(bg-ah)\left(-\frac{d}{-bc+ad} + \frac{1}{a+bx}\right)}{bdg-bch}} \left(-\frac{f}{-be+af} + \frac{1}{a+bx}\right) \right. \\
 & \left. \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{\frac{f}{-be+af} - \frac{h}{-bg+ah}}} \left( \left( (bdg-bch) \text{EllipticE} \left[ \right. \right. \right. \right. \\
 & \left. \left. \left. \left. \text{ArcSin} \left[ \sqrt{\frac{(be-af)\left(h + \frac{bg}{a+bx} - \frac{ah}{a+bx}\right)}{b(-fg+eh)}} \right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right) \right) \right) / \\
 & \left( (bc-ad)(bg-ah) \right) - \frac{1}{-bc+ad} d \text{EllipticF} \left[ \text{ArcSin} \left[ \right. \right. \\
 & \left. \left. \sqrt{\frac{(be-af)\left(h + \frac{bg}{a+bx} - \frac{ah}{a+bx}\right)}{b(-fg+eh)}} \right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right) /
 \end{aligned}$$

$$\begin{aligned}
 & \left( \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right) \left(h + \frac{bg-ah}{a+bx}\right)} \right) + \\
 & \left( a^2 b B C f h \sqrt{\frac{(bc-ad)(bg-ah) \left(-\frac{d}{-bc+ad} + \frac{1}{a+bx}\right)}{bdg-bch}} \left(-\frac{f}{-be+af} + \frac{1}{a+bx}\right) \right. \\
 & \left. \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{-\frac{f}{-be+af} - \frac{h}{-bg+ah}}} \left( \left( (bdg-bch) \text{EllipticE} \left[ \right. \right. \right. \right. \\
 & \left. \left. \left. \left. \text{ArcSin} \left[ \sqrt{\frac{(be-af) \left(h + \frac{bg}{a+bx} - \frac{ah}{a+bx}\right)}{b(-fg+eh)}} \right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right) \right) \right) / \\
 & \left( (bc-ad)(bg-ah) \right) - \frac{1}{-bc+ad} d \text{EllipticF} \left[ \text{ArcSin} \left[ \right. \right. \\
 & \left. \left. \sqrt{\frac{(be-af) \left(h + \frac{bg}{a+bx} - \frac{ah}{a+bx}\right)}{b(-fg+eh)}} \right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right) / \\
 & \left( \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right) \left(h + \frac{bg-ah}{a+bx}\right)} \right) + \\
 & \left( 6 a^2 A b d f h \sqrt{\frac{(bc-ad)(bg-ah) \left(-\frac{d}{-bc+ad} + \frac{1}{a+bx}\right)}{bdg-bch}} \left(-\frac{f}{-be+af} + \frac{1}{a+bx}\right) \right. \\
 & \left. \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{-\frac{f}{-be+af} - \frac{h}{-bg+ah}}} \left( \left( (bdg-bch) \text{EllipticE} \left[ \right. \right. \right. \right. \\
 & \left. \left. \left. \left. \text{ArcSin} \left[ \sqrt{\frac{(be-af) \left(h + \frac{bg}{a+bx} - \frac{ah}{a+bx}\right)}{b(-fg+eh)}} \right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right) \right) \right) / \\
 & \left( (bc-ad)(bg-ah) \right) - \frac{1}{-bc+ad} d \text{EllipticF} \left[ \text{ArcSin} \left[ \right. \right.
 \end{aligned}$$

$$\left( \sqrt{\frac{(be-af) \left( h + \frac{bg}{a+bx} - \frac{ah}{a+bx} \right)}{b(-fg+eh)}} \right), \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \Bigg) /$$

$$\left( \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \sqrt{\left( d + \frac{bc-ad}{a+bx} \right) \left( f + \frac{be-af}{a+bx} \right) \left( h + \frac{bg-ah}{a+bx} \right)} \right) -$$

$$\left( 3a^3 B d f h \sqrt{\frac{(bc-ad)(bg-ah) \left( -\frac{d}{-bc+ad} + \frac{1}{a+bx} \right)}{bdg-bch}} \left( -\frac{f}{-be+af} + \frac{1}{a+bx} \right) \right.$$

$$\left. \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{\frac{f}{-be+af} - \frac{h}{-bg+ah}}} \left( - \left( (bdg-bch) \text{EllipticE} \left[ \right. \right. \right. \right.$$

$$\left. \left. \left. \left. \text{ArcSin} \left[ \sqrt{\frac{(be-af) \left( h + \frac{bg}{a+bx} - \frac{ah}{a+bx} \right)}{b(-fg+eh)}} \right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right) \right) \right) /$$

$$\left( (bc-ad)(bg-ah) \right) \Bigg) - \frac{1}{-bc+ad} d \text{EllipticF} \left[ \text{ArcSin} \left[ \right. \right.$$

$$\left. \left. \sqrt{\frac{(be-af) \left( h + \frac{bg}{a+bx} - \frac{ah}{a+bx} \right)}{b(-fg+eh)}} \right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right) /$$

$$\left( \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \sqrt{\left( d + \frac{bc-ad}{a+bx} \right) \left( f + \frac{be-af}{a+bx} \right) \left( h + \frac{bg-ah}{a+bx} \right)} \right) +$$

$$\left( A b^2 d f g \sqrt{\frac{-\frac{d}{-bc+ad} + \frac{1}{a+bx}}{-\frac{d}{-bc+ad} + \frac{h}{-bg+ah}}} \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \left( -\frac{h}{-bg+ah} + \frac{1}{a+bx} \right) \right.$$

$$\left. \text{EllipticF} \left[ \text{ArcSin} \left[ \sqrt{\frac{(-be+af) \left( -h - \frac{bg}{a+bx} + \frac{ah}{a+bx} \right)}{b(-fg+eh)}} \right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right) /$$

$$\left( \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{\frac{f}{-be+af} - \frac{h}{-bg+ah}}} \sqrt{\left( d + \frac{bc-ad}{a+bx} \right) \left( f + \frac{be-af}{a+bx} \right) \left( h + \frac{bg-ah}{a+bx} \right)} \right) -$$

$$\left( a b B d f g \sqrt{\frac{-\frac{d}{-bc+ad} + \frac{1}{a+bx}}{-\frac{d}{-bc+ad} + \frac{h}{-bg+ah}}} \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \left( -\frac{h}{-bg+ah} + \frac{1}{a+bx} \right) \right. \\ \left. \text{EllipticF}\left[\text{ArcSin}\left[\sqrt{\frac{(-be+af)\left(-h - \frac{bg}{a+bx} + \frac{ah}{a+bx}\right)}{b(-fg+eh)}}\right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)}\right] \right) /$$

$$\left( \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{\frac{f}{-be+af} - \frac{h}{-bg+ah}}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right) \left(h + \frac{bg-ah}{a+bx}\right)} \right) +$$

$$\left( A b^2 d e h \sqrt{\frac{-\frac{d}{-bc+ad} + \frac{1}{a+bx}}{-\frac{d}{-bc+ad} + \frac{h}{-bg+ah}}} \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \left( -\frac{h}{-bg+ah} + \frac{1}{a+bx} \right) \right.$$

$$\left. \text{EllipticF}\left[\text{ArcSin}\left[\sqrt{\frac{(-be+af)\left(-h - \frac{bg}{a+bx} + \frac{ah}{a+bx}\right)}{b(-fg+eh)}}\right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)}\right] \right) /$$

$$\left( \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{\frac{f}{-be+af} - \frac{h}{-bg+ah}}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right) \left(h + \frac{bg-ah}{a+bx}\right)} \right) -$$

$$\left( a b B d e h \sqrt{\frac{-\frac{d}{-bc+ad} + \frac{1}{a+bx}}{-\frac{d}{-bc+ad} + \frac{h}{-bg+ah}}} \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \left( -\frac{h}{-bg+ah} + \frac{1}{a+bx} \right) \right.$$

$$\left. \text{EllipticF}\left[\text{ArcSin}\left[\sqrt{\frac{(-be+af)\left(-h - \frac{bg}{a+bx} + \frac{ah}{a+bx}\right)}{b(-fg+eh)}}\right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)}\right] \right) /$$

$$\left( \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{\frac{f}{-be+af} - \frac{h}{-bg+ah}}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right) \left(h + \frac{bg-ah}{a+bx}\right)} \right) +$$

$$\left( A b^2 c f h \sqrt{\frac{-\frac{d}{-bc+ad} + \frac{1}{a+bx}}{-\frac{d}{-bc+ad} + \frac{h}{-bg+ah}}} \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \left( -\frac{h}{-bg+ah} + \frac{1}{a+bx} \right) \right.$$

$$\left. \text{EllipticF}\left[\text{ArcSin}\left[\sqrt{\frac{(-be+af)\left(-h - \frac{bg}{a+bx} + \frac{ah}{a+bx}\right)}{b(-fg+eh)}}\right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)}\right] \right) /$$

$$\left( \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{\frac{f}{-be+af} - \frac{h}{-bg+ah}}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right) \left(h + \frac{bg-ah}{a+bx}\right)} \right) -$$

$$\left( ab B c f h \sqrt{\frac{-\frac{d}{-bc+ad} + \frac{1}{a+bx}}{-\frac{d}{-bc+ad} + \frac{h}{-bg+ah}}} \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \left(-\frac{h}{-bg+ah} + \frac{1}{a+bx}\right) \right)$$

$$\left. \text{EllipticF}\left[\text{ArcSin}\left[\sqrt{\frac{(-be+af)\left(-h - \frac{bg}{a+bx} + \frac{ah}{a+bx}\right)}{b(-fg+eh)}}\right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)}\right] \right) /$$

$$\left( \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{\frac{f}{-be+af} - \frac{h}{-bg+ah}}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right) \left(h + \frac{bg-ah}{a+bx}\right)} \right) -$$

$$\left( 3 a A b d f h \sqrt{\frac{-\frac{d}{-bc+ad} + \frac{1}{a+bx}}{-\frac{d}{-bc+ad} + \frac{h}{-bg+ah}}} \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \left(-\frac{h}{-bg+ah} + \frac{1}{a+bx}\right) \right)$$

$$\left. \text{EllipticF}\left[\text{ArcSin}\left[\sqrt{\frac{(-be+af)\left(-h - \frac{bg}{a+bx} + \frac{ah}{a+bx}\right)}{b(-fg+eh)}}\right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)}\right] \right) /$$

$$\left( \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{\frac{f}{-be+af} - \frac{h}{-bg+ah}}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right) \left(h + \frac{bg-ah}{a+bx}\right)} \right) +$$

$$\left( 3 a^2 B d f h \sqrt{\frac{-\frac{d}{-bc+ad} + \frac{1}{a+bx}}{-\frac{d}{-bc+ad} + \frac{h}{-bg+ah}}} \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \left(-\frac{h}{-bg+ah} + \frac{1}{a+bx}\right) \right)$$

$$\left. \text{EllipticF}\left[\text{ArcSin}\left[\sqrt{\frac{(-be+af)\left(-h - \frac{bg}{a+bx} + \frac{ah}{a+bx}\right)}{b(-fg+eh)}}\right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)}\right] \right) /$$

$$\left( \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{\frac{f}{-be+af} - \frac{h}{-bg+ah}}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right) \left(h + \frac{bg-ah}{a+bx}\right)} \right)$$

Problem 11: Result more than twice size of optimal antiderivative.

$$\int \frac{(a+bx)^{3/2} (de+cf+2dfx)}{\sqrt{c+dx} \sqrt{e+fx} \sqrt{g+hx}} dx$$

Optimal (type 4, 898 leaves, 10 steps):

$$\begin{aligned} & \frac{(5adf h - b(3dfg + deh + cfh)) \sqrt{a+bx} \sqrt{e+fx} \sqrt{g+hx}}{2fh^2 \sqrt{c+dx}} + \\ & \frac{b \sqrt{a+bx} \sqrt{c+dx} \sqrt{e+fx} \sqrt{g+hx}}{h} - \\ & \left( \sqrt{dg - ch} \sqrt{fg - eh} (5adf h - b(3dfg + deh + cfh)) \sqrt{a+bx} \sqrt{-\frac{(de - cf)(g + hx)}{(fg - eh)(c + dx)}} \right. \\ & \quad \left. \text{EllipticE} \left[ \text{ArcSin} \left[ \frac{\sqrt{dg - ch} \sqrt{e+fx}}{\sqrt{fg - eh} \sqrt{c+dx}} \right], \frac{(bc - ad)(fg - eh)}{(be - af)(dg - ch)} \right] \right) / \\ & \left( 2dfh^2 \sqrt{\frac{(de - cf)(a + bx)}{(be - af)(c + dx)}} \sqrt{g + hx} \right) - \\ & \left( (be - af) \sqrt{bg - ah} (3adf h + b(cf h - d(3fg + eh))) \sqrt{\frac{(be - af)(c + dx)}{(de - cf)(a + bx)}} \right. \\ & \quad \left. \sqrt{g + hx} \text{EllipticF} \left[ \text{ArcSin} \left[ \frac{\sqrt{bg - ah} \sqrt{e+fx}}{\sqrt{fg - eh} \sqrt{a+bx}} \right], -\frac{(bc - ad)(fg - eh)}{(de - cf)(bg - ah)} \right] \right) / \\ & \left( 2bfh^2 \sqrt{fg - eh} \sqrt{c + dx} \sqrt{-\frac{(be - af)(g + hx)}{(fg - eh)(a + bx)}} \right) - \\ & \left( \sqrt{-dg + ch} (6abd^2 f^2 gh - 3a^2 d^2 f^2 h^2 + b^2 (2cdefh^2 - c^2 f^2 h^2 - d^2 (3f^2 g^2 + e^2 h^2))) \right. \\ & \quad \left. (a + bx) \sqrt{\frac{(bg - ah)(c + dx)}{(dg - ch)(a + bx)}} \sqrt{\frac{(bg - ah)(e + fx)}{(fg - eh)(a + bx)}} \right. \\ & \quad \left. \text{EllipticPi} \left[ -\frac{b(dg - ch)}{(bc - ad)h}, \text{ArcSin} \left[ \frac{\sqrt{bc - ad} \sqrt{g + hx}}{\sqrt{-dg + ch} \sqrt{a + bx}} \right], \frac{(be - af)(dg - ch)}{(bc - ad)(fg - eh)} \right] \right) / \\ & (2bd \sqrt{bc - ad} fh^3 \sqrt{c + dx} \sqrt{e + fx}) \end{aligned}$$

Result (type 4, 14853 leaves):

$$\frac{b \sqrt{a+bx} \sqrt{c+dx} \sqrt{e+fx} \sqrt{g+hx}}{h} +$$

$$\begin{aligned}
 & \frac{1}{b^2 h} \left( \left( (-3 b d f g - b d e h - b c f h + 5 a d f h) (a + b x)^{5/2} \left( d + \frac{b c}{a + b x} - \frac{a d}{a + b x} \right) \right. \right. \\
 & \quad \left. \left. \left( f + \frac{b e}{a + b x} - \frac{a f}{a + b x} \right) \left( h + \frac{b g}{a + b x} - \frac{a h}{a + b x} \right) \right) \right) / \\
 & \left( 2 d f h \sqrt{c + \frac{(a + b x) \left( d - \frac{a d}{a + b x} \right)}{b}} \sqrt{e + \frac{(a + b x) \left( f - \frac{a f}{a + b x} \right)}{b}} \sqrt{g + \frac{(a + b x) \left( h - \frac{a h}{a + b x} \right)}{b}} \right) + \\
 & \left( 1 / \left( 2 d f h \sqrt{c + \frac{(a + b x) \left( d - \frac{a d}{a + b x} \right)}{b}} \sqrt{e + \frac{(a + b x) \left( f - \frac{a f}{a + b x} \right)}{b}} \sqrt{g + \frac{(a + b x) \left( h - \frac{a h}{a + b x} \right)}{b}} \right) \right) \\
 & (a + b x)^{3/2} \sqrt{\left( \left( d + \frac{b c}{a + b x} - \frac{a d}{a + b x} \right) \left( f + \frac{b e}{a + b x} - \frac{a f}{a + b x} \right) \left( h + \frac{b g}{a + b x} - \frac{a h}{a + b x} \right) \right)} \left( \left( 3 b^4 c d e f \right. \right. \\
 & \quad \left. \left. g^2 \sqrt{\frac{(b c - a d) (b g - a h) \left( -\frac{d}{-b c + a d} + \frac{1}{a + b x} \right)}{b d g - b c h}} \left( -\frac{f}{-b e + a f} + \frac{1}{a + b x} \right) \sqrt{\frac{-\frac{h}{-b g + a h} + \frac{1}{a + b x}}{\frac{f}{-b e + a f} - \frac{h}{-b g + a h}}} \right. \right. \\
 & \quad \left. \left. - \left( (b d g - b c h) \text{EllipticE}\left[ \text{ArcSin}\left[ \sqrt{\frac{(b e - a f) \left( h + \frac{b g}{a + b x} - \frac{a h}{a + b x} \right)}{b (-f g + e h)}} \right] \right), \right. \right. \\
 & \quad \left. \left. \frac{(-b c + a d) (-f g + e h)}{(-b e + a f) (-d g + c h)} \right) \right) / \left( (b c - a d) (b g - a h) \right) - \frac{1}{-b c + a d} \\
 & \quad \left. \left. d \text{EllipticF}\left[ \text{ArcSin}\left[ \sqrt{\frac{(b e - a f) \left( h + \frac{b g}{a + b x} - \frac{a h}{a + b x} \right)}{b (-f g + e h)}} \right] \right], \frac{(-b c + a d) (-f g + e h)}{(-b e + a f) (-d g + c h)} \right] \right) \right) / \\
 & \left( \sqrt{\frac{-\frac{f}{-b e + a f} + \frac{1}{a + b x}}{-\frac{f}{-b e + a f} + \frac{h}{-b g + a h}}} \sqrt{\left( d + \frac{b c - a d}{a + b x} \right) \left( f + \frac{b e - a f}{a + b x} \right) \left( h + \frac{b g - a h}{a + b x} \right)} - \left( 3 a b^3 d^2 e f \right. \right. \\
 & \quad \left. \left. g^2 \sqrt{\frac{(b c - a d) (b g - a h) \left( -\frac{d}{-b c + a d} + \frac{1}{a + b x} \right)}{b d g - b c h}} \left( -\frac{f}{-b e + a f} + \frac{1}{a + b x} \right) \sqrt{\frac{-\frac{h}{-b g + a h} + \frac{1}{a + b x}}{\frac{f}{-b e + a f} - \frac{h}{-b g + a h}}} \right. \right.
 \end{aligned}$$

$$\left( - \left( \left( (bdg - bch) \operatorname{EllipticE} \left[ \operatorname{ArcSin} \left[ \sqrt{\frac{(be - af) \left( h + \frac{bg}{a+bx} - \frac{ah}{a+bx} \right)}{b(-fg + eh)}} \right] \right), \right. \right. \right.$$

$$\left. \left. \left. \frac{(-bc + ad)(-fg + eh)}{(-be + af)(-dg + ch)} \right] \right) / \left( (bc - ad)(bg - ah) \right) - \frac{1}{-bc + ad} \right.$$

$$\left. \left. \left. d \operatorname{EllipticF} \left[ \operatorname{ArcSin} \left[ \sqrt{\frac{(be - af) \left( h + \frac{bg}{a+bx} - \frac{ah}{a+bx} \right)}{b(-fg + eh)}} \right] \right], \frac{(-bc + ad)(-fg + eh)}{(-be + af)(-dg + ch)} \right] \right) \right) /$$

$$\left( \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \sqrt{\left( d + \frac{bc - ad}{a + bx} \right) \left( f + \frac{be - af}{a + bx} \right) \left( h + \frac{bg - ah}{a + bx} \right)} \right) -$$

$$\left( 3ab^3cd f^2 g^2 \sqrt{\frac{(bc - ad)(bg - ah) \left( -\frac{d}{-bc+ad} + \frac{1}{a+bx} \right)}{bdg - bch}} \right.$$

$$\left. \left( -\frac{f}{-be + af} + \frac{1}{a + bx} \right) \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{\frac{f}{-be+af} - \frac{h}{-bg+ah}}} \right.$$

$$\left( - \left( \left( (bdg - bch) \operatorname{EllipticE} \left[ \operatorname{ArcSin} \left[ \sqrt{\frac{(be - af) \left( h + \frac{bg}{a+bx} - \frac{ah}{a+bx} \right)}{b(-fg + eh)}} \right] \right), \right. \right. \right.$$

$$\left. \left. \left. \frac{(-bc + ad)(-fg + eh)}{(-be + af)(-dg + ch)} \right] \right) / \left( (bc - ad)(bg - ah) \right) - \frac{1}{-bc + ad} \right.$$

$$\left. \left. \left. d \operatorname{EllipticF} \left[ \operatorname{ArcSin} \left[ \sqrt{\frac{(be - af) \left( h + \frac{bg}{a+bx} - \frac{ah}{a+bx} \right)}{b(-fg + eh)}} \right] \right], \frac{(-bc + ad)(-fg + eh)}{(-be + af)(-dg + ch)} \right] \right) \right) /$$

$$\left( \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \sqrt{\left( d + \frac{bc - ad}{a + bx} \right) \left( f + \frac{be - af}{a + bx} \right) \left( h + \frac{bg - ah}{a + bx} \right)} \right) +$$

$$\left( 3a^2b^2d^2 f^2 g^2 \sqrt{\frac{(bc - ad)(bg - ah) \left( -\frac{d}{-bc+ad} + \frac{1}{a+bx} \right)}{bdg - bch}} \right)$$

$$\begin{aligned}
 & \left( -\frac{f}{-be+af} + \frac{1}{a+bx} \right) \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{\frac{f}{-be+af} - \frac{h}{-bg+ah}}} \\
 & \left( -\left( (bdg-bch) \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\sqrt{\frac{(be-af)\left(h+\frac{bg}{a+bx}-\frac{ah}{a+bx}\right)}{b(-fg+eh)}}\right], \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right) / \left( (bc-ad)(bg-ah) \right) - \frac{1}{-bc+ad} \right. \\
 & \quad \left. \left. \left. d \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\sqrt{\frac{(be-af)\left(h+\frac{bg}{a+bx}-\frac{ah}{a+bx}\right)}{b(-fg+eh)}}\right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right) \right) \right) / \\
 & \left( \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right) \left(h + \frac{bg-ah}{a+bx}\right)} \right) + \\
 & \left( b^4 c d e^2 g h \sqrt{\frac{(bc-ad)(bg-ah)\left(-\frac{d}{-bc+ad} + \frac{1}{a+bx}\right)}{bdg-bch}} \right. \\
 & \left. \left( -\frac{f}{-be+af} + \frac{1}{a+bx} \right) \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{\frac{f}{-be+af} - \frac{h}{-bg+ah}}} \right. \\
 & \left. \left( -\left( (bdg-bch) \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\sqrt{\frac{(be-af)\left(h+\frac{bg}{a+bx}-\frac{ah}{a+bx}\right)}{b(-fg+eh)}}\right], \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right) / \left( (bc-ad)(bg-ah) \right) - \frac{1}{-bc+ad} \right. \\
 & \quad \left. \left. \left. d \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\sqrt{\frac{(be-af)\left(h+\frac{bg}{a+bx}-\frac{ah}{a+bx}\right)}{b(-fg+eh)}}\right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right) \right) \right) / \\
 & \left( \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right) \left(h + \frac{bg-ah}{a+bx}\right)} \right) -
 \end{aligned}$$

$$\begin{aligned}
 & \left( ab^3 d^2 e^2 g h \sqrt{\frac{(bc-ad)(bg-ah) \left(-\frac{d}{-bc+ad} + \frac{1}{a+bx}\right)}{bdg-bch}} \right. \\
 & \left. \left(-\frac{f}{-be+af} + \frac{1}{a+bx}\right) \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{\frac{f}{-be+af} - \frac{h}{-bg+ah}}} \right. \\
 & \left. \left( - \left( (bdg-bch) \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\sqrt{\frac{(be-af)\left(h + \frac{bg}{a+bx} - \frac{ah}{a+bx}\right)}{b(-fg+eh)}}\right], \right. \right. \right. \\
 & \left. \left. \left. \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right) / \left( (bc-ad)(bg-ah) \right) - \frac{1}{-bc+ad} \right. \\
 & \left. \left. \left. d \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\sqrt{\frac{(be-af)\left(h + \frac{bg}{a+bx} - \frac{ah}{a+bx}\right)}{b(-fg+eh)}}\right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)}\right] \right) \right) \right) / \\
 & \left( \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right) \left(h + \frac{bg-ah}{a+bx}\right)} \right) + \\
 & \left( b^4 c^2 e f g h \sqrt{\frac{(bc-ad)(bg-ah) \left(-\frac{d}{-bc+ad} + \frac{1}{a+bx}\right)}{bdg-bch}} \right. \\
 & \left. \left(-\frac{f}{-be+af} + \frac{1}{a+bx}\right) \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{\frac{f}{-be+af} - \frac{h}{-bg+ah}}} \right. \\
 & \left. \left( - \left( (bdg-bch) \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\sqrt{\frac{(be-af)\left(h + \frac{bg}{a+bx} - \frac{ah}{a+bx}\right)}{b(-fg+eh)}}\right], \right. \right. \right. \\
 & \left. \left. \left. \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right) / \left( (bc-ad)(bg-ah) \right) - \frac{1}{-bc+ad} \right. \\
 & \left. \left. \left. d \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\sqrt{\frac{(be-af)\left(h + \frac{bg}{a+bx} - \frac{ah}{a+bx}\right)}{b(-fg+eh)}}\right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)}\right] \right) \right) \right) /
 \end{aligned}$$

$$\begin{aligned}
 & \left( \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right) \left(h + \frac{bg-ah}{a+bx}\right)} \right) - \\
 & \left( 10ab^3cdefgh \sqrt{\frac{(bc-ad)(bg-ah)\left(-\frac{d}{-bc+ad} + \frac{1}{a+bx}\right)}{bdg-bch}} \right. \\
 & \left. \left(-\frac{f}{-be+af} + \frac{1}{a+bx}\right) \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{\frac{f}{-be+af} - \frac{h}{-bg+ah}}} \right. \\
 & \left. \left. - \left( (bdg-bch) \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\sqrt{\frac{(be-af)\left(h + \frac{bg}{a+bx} - \frac{ah}{a+bx}\right)}{b(-fg+eh)}}\right], \right. \right. \right. \\
 & \left. \left. \left. \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right) / \left( (bc-ad)(bg-ah) \right) - \frac{1}{-bc+ad} \right. \\
 & \left. \left. \left. d \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\sqrt{\frac{(be-af)\left(h + \frac{bg}{a+bx} - \frac{ah}{a+bx}\right)}{b(-fg+eh)}}\right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right) \right) \right) / \\
 & \left( \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right) \left(h + \frac{bg-ah}{a+bx}\right)} \right) + \\
 & \left( 9a^2b^2d^2efgh \sqrt{\frac{(bc-ad)(bg-ah)\left(-\frac{d}{-bc+ad} + \frac{1}{a+bx}\right)}{bdg-bch}} \right. \\
 & \left. \left(-\frac{f}{-be+af} + \frac{1}{a+bx}\right) \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{\frac{f}{-be+af} - \frac{h}{-bg+ah}}} \right. \\
 & \left. \left. - \left( (bdg-bch) \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\sqrt{\frac{(be-af)\left(h + \frac{bg}{a+bx} - \frac{ah}{a+bx}\right)}{b(-fg+eh)}}\right], \right. \right. \right. \\
 & \left. \left. \left. \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right) / \left( (bc-ad)(bg-ah) \right) - \frac{1}{-bc+ad} \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left. d \operatorname{EllipticF} \left[ \operatorname{ArcSin} \left[ \sqrt{\frac{(be-af) \left( h + \frac{bg}{a+bx} - \frac{ah}{a+bx} \right)}{b(-fg+eh)}} \right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right) / \\
 & \left( \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \sqrt{\left( d + \frac{bc-ad}{a+bx} \right) \left( f + \frac{be-af}{a+bx} \right) \left( h + \frac{bg-ah}{a+bx} \right)} \right) - \\
 & \left( ab^3 c^2 f^2 gh \sqrt{\frac{(bc-ad)(bg-ah) \left( -\frac{d}{-bc+ad} + \frac{1}{a+bx} \right)}{bdg-bch}} \right. \\
 & \left. \left( -\frac{f}{-be+af} + \frac{1}{a+bx} \right) \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{\frac{f}{-be+af} - \frac{h}{-bg+ah}}} \right. \\
 & \left. \left( - \left( (bdg-bch) \operatorname{EllipticE} \left[ \operatorname{ArcSin} \left[ \sqrt{\frac{(be-af) \left( h + \frac{bg}{a+bx} - \frac{ah}{a+bx} \right)}{b(-fg+eh)}} \right], \right. \right. \right. \\
 & \left. \left. \left. \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right) / ((bc-ad)(bg-ah)) \right) - \frac{1}{-bc+ad} \\
 & \left. d \operatorname{EllipticF} \left[ \operatorname{ArcSin} \left[ \sqrt{\frac{(be-af) \left( h + \frac{bg}{a+bx} - \frac{ah}{a+bx} \right)}{b(-fg+eh)}} \right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right) / \\
 & \left( \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \sqrt{\left( d + \frac{bc-ad}{a+bx} \right) \left( f + \frac{be-af}{a+bx} \right) \left( h + \frac{bg-ah}{a+bx} \right)} \right) + \\
 & \left( 9a^2 b^2 c d f^2 gh \sqrt{\frac{(bc-ad)(bg-ah) \left( -\frac{d}{-bc+ad} + \frac{1}{a+bx} \right)}{bdg-bch}} \right. \\
 & \left. \left( -\frac{f}{-be+af} + \frac{1}{a+bx} \right) \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{\frac{f}{-be+af} - \frac{h}{-bg+ah}}} \right. \\
 & \left. \left( - \left( (bdg-bch) \operatorname{EllipticE} \left[ \operatorname{ArcSin} \left[ \sqrt{\frac{(be-af) \left( h + \frac{bg}{a+bx} - \frac{ah}{a+bx} \right)}{b(-fg+eh)}} \right], \right. \right. \right. \right.
 \end{aligned}$$

$$\left. \left( \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right) / \left( (bc-ad)(bg-ah) \right) - \frac{1}{-bc+ad} \right.$$

$$\left. \left. d \operatorname{EllipticF} \left[ \operatorname{ArcSin} \left[ \sqrt{\frac{(be-af) \left( h + \frac{bg}{a+bx} - \frac{ah}{a+bx} \right)}{b(-fg+eh)}} \right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right) \right/$$

$$\left( \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \sqrt{\left( d + \frac{bc-ad}{a+bx} \right) \left( f + \frac{be-af}{a+bx} \right) \left( h + \frac{bg-ah}{a+bx} \right)} \right) -$$

$$\left( 8a^3 b d^2 f^2 g h \sqrt{\frac{(bc-ad)(bg-ah) \left( -\frac{d}{-bc+ad} + \frac{1}{a+bx} \right)}{bdg-bch}} \right.$$

$$\left. \left( -\frac{f}{-be+af} + \frac{1}{a+bx} \right) \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{\frac{f}{-be+af} - \frac{h}{-bg+ah}}} \right.$$

$$\left. \left( (bdg-bch) \operatorname{EllipticE} \left[ \operatorname{ArcSin} \left[ \sqrt{\frac{(be-af) \left( h + \frac{bg}{a+bx} - \frac{ah}{a+bx} \right)}{b(-fg+eh)}} \right], \right. \right.$$

$$\left. \left. \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right) / \left( (bc-ad)(bg-ah) \right) - \frac{1}{-bc+ad}$$

$$\left. \left. d \operatorname{EllipticF} \left[ \operatorname{ArcSin} \left[ \sqrt{\frac{(be-af) \left( h + \frac{bg}{a+bx} - \frac{ah}{a+bx} \right)}{b(-fg+eh)}} \right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right) \right/$$

$$\left( \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \sqrt{\left( d + \frac{bc-ad}{a+bx} \right) \left( f + \frac{be-af}{a+bx} \right) \left( h + \frac{bg-ah}{a+bx} \right)} \right) -$$

$$\left( ab^3 c d e^2 h^2 \sqrt{\frac{(bc-ad)(bg-ah) \left( -\frac{d}{-bc+ad} + \frac{1}{a+bx} \right)}{bdg-bch}} \right.$$

$$\left. \left( -\frac{f}{-be+af} + \frac{1}{a+bx} \right) \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{\frac{f}{-be+af} - \frac{h}{-bg+ah}}} \right.$$

$$\begin{aligned}
 & \left( - \left( \left( (bdg - bch) \operatorname{EllipticE} \left[ \operatorname{ArcSin} \left[ \sqrt{\frac{(be - af) \left( h + \frac{bg}{a+bx} - \frac{ah}{a+bx} \right)}{b(-fg + eh)}} \right] \right), \right. \right. \\
 & \left. \left. \frac{(-bc + ad)(-fg + eh)}{(-be + af)(-dg + ch)} \right) \right) / \left( (bc - ad)(bg - ah) \right) - \frac{1}{-bc + ad} \\
 & \left. d \operatorname{EllipticF} \left[ \operatorname{ArcSin} \left[ \sqrt{\frac{(be - af) \left( h + \frac{bg}{a+bx} - \frac{ah}{a+bx} \right)}{b(-fg + eh)}} \right] \right], \frac{(-bc + ad)(-fg + eh)}{(-be + af)(-dg + ch)} \right] \right) / \\
 & \left( \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \sqrt{\left( d + \frac{bc - ad}{a + bx} \right) \left( f + \frac{be - af}{a + bx} \right) \left( h + \frac{bg - ah}{a + bx} \right)} \right) + \\
 & \left( a^2 b^2 d^2 e^2 h^2 \sqrt{\frac{(bc - ad)(bg - ah) \left( -\frac{d}{-bc+ad} + \frac{1}{a+bx} \right)}{bdg - bch}} \right. \\
 & \left. \left( -\frac{f}{-be + af} + \frac{1}{a + bx} \right) \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{\frac{f}{-be+af} - \frac{h}{-bg+ah}}} \right. \\
 & \left. \left( - \left( \left( (bdg - bch) \operatorname{EllipticE} \left[ \operatorname{ArcSin} \left[ \sqrt{\frac{(be - af) \left( h + \frac{bg}{a+bx} - \frac{ah}{a+bx} \right)}{b(-fg + eh)}} \right] \right), \right. \right. \right. \\
 & \left. \left. \frac{(-bc + ad)(-fg + eh)}{(-be + af)(-dg + ch)} \right) \right) / \left( (bc - ad)(bg - ah) \right) - \frac{1}{-bc + ad} \right. \\
 & \left. \left. d \operatorname{EllipticF} \left[ \operatorname{ArcSin} \left[ \sqrt{\frac{(be - af) \left( h + \frac{bg}{a+bx} - \frac{ah}{a+bx} \right)}{b(-fg + eh)}} \right] \right], \frac{(-bc + ad)(-fg + eh)}{(-be + af)(-dg + ch)} \right] \right) / \\
 & \left( \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \sqrt{\left( d + \frac{bc - ad}{a + bx} \right) \left( f + \frac{be - af}{a + bx} \right) \left( h + \frac{bg - ah}{a + bx} \right)} \right) - \\
 & \left( a b^3 c^2 e f h^2 \sqrt{\frac{(bc - ad)(bg - ah) \left( -\frac{d}{-bc+ad} + \frac{1}{a+bx} \right)}{bdg - bch}} \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left( -\frac{f}{-be+af} + \frac{1}{a+bx} \right) \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{\frac{f}{-be+af} - \frac{h}{-bg+ah}}} \\
 & \left( -\left( (bdg-bch) \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\sqrt{\frac{(be-af)\left(h+\frac{bg}{a+bx}-\frac{ah}{a+bx}\right)}{b(-fg+eh)}}\right], \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)}\right] \right) / \left( (bc-ad)(bg-ah) \right) - \frac{1}{-bc+ad} \right. \\
 & \quad \left. \left. \left. d \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\sqrt{\frac{(be-af)\left(h+\frac{bg}{a+bx}-\frac{ah}{a+bx}\right)}{b(-fg+eh)}}\right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)}\right] \right) \right) \right) / \\
 & \left( \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right) \left(h + \frac{bg-ah}{a+bx}\right)} \right) + \\
 & \left( 7a^2b^2cdefh^2 \sqrt{\frac{(bc-ad)(bg-ah)\left(-\frac{d}{-bc+ad} + \frac{1}{a+bx}\right)}{bdg-bch}} \right. \\
 & \left. \left( -\frac{f}{-be+af} + \frac{1}{a+bx} \right) \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{\frac{f}{-be+af} - \frac{h}{-bg+ah}}} \right. \\
 & \left. \left( -\left( (bdg-bch) \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\sqrt{\frac{(be-af)\left(h+\frac{bg}{a+bx}-\frac{ah}{a+bx}\right)}{b(-fg+eh)}}\right], \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)}\right] \right) / \left( (bc-ad)(bg-ah) \right) - \frac{1}{-bc+ad} \right. \right. \\
 & \quad \left. \left. \left. d \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\sqrt{\frac{(be-af)\left(h+\frac{bg}{a+bx}-\frac{ah}{a+bx}\right)}{b(-fg+eh)}}\right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)}\right] \right) \right) \right) / \\
 & \left( \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right) \left(h + \frac{bg-ah}{a+bx}\right)} \right) -
 \end{aligned}$$

$$\left( 6 a^3 b d^2 e f h^2 \sqrt{\frac{(bc-ad)(bg-ah)\left(-\frac{d}{-bc+ad} + \frac{1}{a+bx}\right)}{bdg-bch}} \right.$$

$$\left. \left( -\frac{f}{-be+af} + \frac{1}{a+bx} \right) \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{\frac{f}{-be+af} - \frac{h}{-bg+ah}}} \right.$$

$$\left. \left( -\left( (bdg-bch) \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\sqrt{\frac{(be-af)\left(h + \frac{bg}{a+bx} - \frac{ah}{a+bx}\right)}{b(-fg+eh)}}\right], \right. \right. \right.$$

$$\left. \left. \left. \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right) / \left( (bc-ad)(bg-ah) \right) - \frac{1}{-bc+ad} \right.$$

$$\left. \left. \left. d \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\sqrt{\frac{(be-af)\left(h + \frac{bg}{a+bx} - \frac{ah}{a+bx}\right)}{b(-fg+eh)}}\right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right) \right) \right) /$$

$$\left( \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right) \left(h + \frac{bg-ah}{a+bx}\right)} \right) +$$

$$\left( a^2 b^2 c^2 f^2 h^2 \sqrt{\frac{(bc-ad)(bg-ah)\left(-\frac{d}{-bc+ad} + \frac{1}{a+bx}\right)}{bdg-bch}} \right.$$

$$\left. \left( -\frac{f}{-be+af} + \frac{1}{a+bx} \right) \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{\frac{f}{-be+af} - \frac{h}{-bg+ah}}} \right.$$

$$\left. \left( -\left( (bdg-bch) \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\sqrt{\frac{(be-af)\left(h + \frac{bg}{a+bx} - \frac{ah}{a+bx}\right)}{b(-fg+eh)}}\right], \right. \right. \right.$$

$$\left. \left. \left. \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right) / \left( (bc-ad)(bg-ah) \right) - \frac{1}{-bc+ad} \right.$$

$$\left. \left. \left. d \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\sqrt{\frac{(be-af)\left(h + \frac{bg}{a+bx} - \frac{ah}{a+bx}\right)}{b(-fg+eh)}}\right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right) \right) \right) /$$

$$\begin{aligned}
 & \left( \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right) \left(h + \frac{bg-ah}{a+bx}\right)} \right) - \\
 & \left( 6a^3 bcd f^2 h^2 \sqrt{\frac{(bc-ad)(bg-ah) \left(-\frac{d}{-bc+ad} + \frac{1}{a+bx}\right)}{bdg-bch}} \right. \\
 & \left. \left(-\frac{f}{-be+af} + \frac{1}{a+bx}\right) \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{\frac{f}{-be+af} - \frac{h}{-bg+ah}}} \right. \\
 & \left. - \left( \left( (bdg-bch) \text{EllipticE}\left[\text{ArcSin}\left[\sqrt{\frac{(be-af)\left(h + \frac{bg}{a+bx} - \frac{ah}{a+bx}\right)}{b(-fg+eh)}}\right], \right. \right. \right. \\
 & \left. \left. \left. \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right) / \left( (bc-ad)(bg-ah) \right) - \frac{1}{-bc+ad} \right. \\
 & \left. \left. \left. d \text{EllipticF}\left[\text{ArcSin}\left[\sqrt{\frac{(be-af)\left(h + \frac{bg}{a+bx} - \frac{ah}{a+bx}\right)}{b(-fg+eh)}}\right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right) \right) \right) / \\
 & \left( \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right) \left(h + \frac{bg-ah}{a+bx}\right)} \right) + \\
 & \left( 5a^4 d^2 f^2 h^2 \sqrt{\frac{(bc-ad)(bg-ah) \left(-\frac{d}{-bc+ad} + \frac{1}{a+bx}\right)}{bdg-bch}} \right. \\
 & \left. \left(-\frac{f}{-be+af} + \frac{1}{a+bx}\right) \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{\frac{f}{-be+af} - \frac{h}{-bg+ah}}} \right. \\
 & \left. - \left( \left( (bdg-bch) \text{EllipticE}\left[\text{ArcSin}\left[\sqrt{\frac{(be-af)\left(h + \frac{bg}{a+bx} - \frac{ah}{a+bx}\right)}{b(-fg+eh)}}\right], \right. \right. \right. \\
 & \left. \left. \left. \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right) / \left( (bc-ad)(bg-ah) \right) - \frac{1}{-bc+ad} \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left. d \operatorname{EllipticF} \left[ \operatorname{ArcSin} \left[ \sqrt{\frac{(be-af) \left( h + \frac{bg}{a+bx} - \frac{ah}{a+bx} \right)}{b(-fg+eh)}} \right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right) / \\
 & \left( \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \sqrt{\left( d + \frac{bc-ad}{a+bx} \right) \left( f + \frac{be-af}{a+bx} \right) \left( h + \frac{bg-ah}{a+bx} \right)} \right) + \\
 & \left( 2b^3 c d e f g h \sqrt{\frac{-\frac{d}{-bc+ad} + \frac{1}{a+bx}}{-\frac{d}{-bc+ad} + \frac{h}{-bg+ah}}} \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \left( -\frac{h}{-bg+ah} + \frac{1}{a+bx} \right) \right) \\
 & \left. \operatorname{EllipticF} \left[ \operatorname{ArcSin} \left[ \sqrt{\frac{(-be+af) \left( -h - \frac{bg}{a+bx} + \frac{ah}{a+bx} \right)}{b(-fg+eh)}} \right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right) / \\
 & \left( \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{\frac{f}{-be+af} - \frac{h}{-bg+ah}}} \sqrt{\left( d + \frac{bc-ad}{a+bx} \right) \left( f + \frac{be-af}{a+bx} \right) \left( h + \frac{bg-ah}{a+bx} \right)} \right) - \\
 & \left( 2a b^2 d^2 e f g h \sqrt{\frac{-\frac{d}{-bc+ad} + \frac{1}{a+bx}}{-\frac{d}{-bc+ad} + \frac{h}{-bg+ah}}} \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \left( -\frac{h}{-bg+ah} + \frac{1}{a+bx} \right) \right) \\
 & \left. \operatorname{EllipticF} \left[ \operatorname{ArcSin} \left[ \sqrt{\frac{(-be+af) \left( -h - \frac{bg}{a+bx} + \frac{ah}{a+bx} \right)}{b(-fg+eh)}} \right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right) / \\
 & \left( \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{\frac{f}{-be+af} - \frac{h}{-bg+ah}}} \sqrt{\left( d + \frac{bc-ad}{a+bx} \right) \left( f + \frac{be-af}{a+bx} \right) \left( h + \frac{bg-ah}{a+bx} \right)} \right) - \\
 & \left( 2a b^2 c d f^2 g h \sqrt{\frac{-\frac{d}{-bc+ad} + \frac{1}{a+bx}}{-\frac{d}{-bc+ad} + \frac{h}{-bg+ah}}} \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \left( -\frac{h}{-bg+ah} + \frac{1}{a+bx} \right) \right) \\
 & \left. \operatorname{EllipticF} \left[ \operatorname{ArcSin} \left[ \sqrt{\frac{(-be+af) \left( -h - \frac{bg}{a+bx} + \frac{ah}{a+bx} \right)}{b(-fg+eh)}} \right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right) / \\
 & \left( \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{\frac{f}{-be+af} - \frac{h}{-bg+ah}}} \sqrt{\left( d + \frac{bc-ad}{a+bx} \right) \left( f + \frac{be-af}{a+bx} \right) \left( h + \frac{bg-ah}{a+bx} \right)} \right) +
 \end{aligned}$$

$$\left( 2 a^2 b d^2 f^2 g h \sqrt{\frac{-\frac{d}{-bc+ad} + \frac{1}{a+bx}}{-\frac{d}{-bc+ad} + \frac{h}{-bg+ah}}} \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \left( -\frac{h}{-bg+ah} + \frac{1}{a+bx} \right) \right. \\ \left. \text{EllipticF}\left[\text{ArcSin}\left[\sqrt{\frac{(-be+af)\left(-h - \frac{bg}{a+bx} + \frac{ah}{a+bx}\right)}{b(-fg+eh)}}\right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)}\right] \right) /$$

$$\left( \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{\frac{f}{-be+af} - \frac{h}{-bg+ah}}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right)\left(f + \frac{be-af}{a+bx}\right)\left(h + \frac{bg-ah}{a+bx}\right)} \right) -$$

$$\left( 2 a b^2 c d e f h^2 \sqrt{\frac{-\frac{d}{-bc+ad} + \frac{1}{a+bx}}{-\frac{d}{-bc+ad} + \frac{h}{-bg+ah}}} \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \left( -\frac{h}{-bg+ah} + \frac{1}{a+bx} \right) \right. \\ \left. \text{EllipticF}\left[\text{ArcSin}\left[\sqrt{\frac{(-be+af)\left(-h - \frac{bg}{a+bx} + \frac{ah}{a+bx}\right)}{b(-fg+eh)}}\right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)}\right] \right) /$$

$$\left( \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{\frac{f}{-be+af} - \frac{h}{-bg+ah}}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right)\left(f + \frac{be-af}{a+bx}\right)\left(h + \frac{bg-ah}{a+bx}\right)} \right) +$$

$$\left( 2 a^2 b d^2 e f h^2 \sqrt{\frac{-\frac{d}{-bc+ad} + \frac{1}{a+bx}}{-\frac{d}{-bc+ad} + \frac{h}{-bg+ah}}} \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \left( -\frac{h}{-bg+ah} + \frac{1}{a+bx} \right) \right. \\ \left. \text{EllipticF}\left[\text{ArcSin}\left[\sqrt{\frac{(-be+af)\left(-h - \frac{bg}{a+bx} + \frac{ah}{a+bx}\right)}{b(-fg+eh)}}\right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)}\right] \right) /$$

$$\left( \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{\frac{f}{-be+af} - \frac{h}{-bg+ah}}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right)\left(f + \frac{be-af}{a+bx}\right)\left(h + \frac{bg-ah}{a+bx}\right)} \right) +$$

$$\left( 2 a^2 b c d f^2 h^2 \sqrt{\frac{-\frac{d}{-bc+ad} + \frac{1}{a+bx}}{-\frac{d}{-bc+ad} + \frac{h}{-bg+ah}}} \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \left( -\frac{h}{-bg+ah} + \frac{1}{a+bx} \right) \right. \\ \left. \text{EllipticF}\left[\text{ArcSin}\left[\sqrt{\frac{(-be+af)\left(-h - \frac{bg}{a+bx} + \frac{ah}{a+bx}\right)}{b(-fg+eh)}}\right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)}\right] \right) /$$

$$\left( \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{\frac{f}{-be+af} - \frac{h}{-bg+ah}}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right) \left(h + \frac{bg-ah}{a+bx}\right)} \right) -$$

$$\left( 2 a^3 d^2 f^2 h^2 \sqrt{\frac{-\frac{d}{-bc+ad} + \frac{1}{a+bx}}{-\frac{d}{-bc+ad} + \frac{h}{-bg+ah}}} \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \left(-\frac{h}{-bg+ah} + \frac{1}{a+bx}\right) \right.$$

$$\left. \text{EllipticF}\left[\text{ArcSin}\left[\sqrt{\frac{(-be+af) \left(-h - \frac{bg}{a+bx} + \frac{ah}{a+bx}\right)}{b(-fg+eh)}}\right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)}\right] \right) /$$

$$\left( \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{\frac{f}{-be+af} - \frac{h}{-bg+ah}}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right) \left(h + \frac{bg-ah}{a+bx}\right)} \right) -$$

$$\left( 6 a b d^2 f^2 g (-bg+ah) \left(-\frac{f}{-be+af} + \frac{h}{-bg+ah}\right) \sqrt{\frac{-\frac{d}{-bc+ad} + \frac{1}{a+bx}}{-\frac{d}{-bc+ad} + \frac{h}{-bg+ah}}} \right.$$

$$\left. \sqrt{-\frac{\left(-\frac{f}{-be+af} + \frac{1}{a+bx}\right) \left(-\frac{h}{-bg+ah} + \frac{1}{a+bx}\right)}{\left(-\frac{f}{-be+af} + \frac{h}{-bg+ah}\right)^2}} \text{EllipticPi}\left[-\frac{-bfg+beh}{(-be+af)h}, \right. \right.$$

$$\left. \left. \text{ArcSin}\left[\sqrt{\frac{(-be+af) \left(-h - \frac{bg}{a+bx} + \frac{ah}{a+bx}\right)}{b(-fg+eh)}}\right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)}\right] \right) /$$

$$\left( \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right) \left(h + \frac{bg-ah}{a+bx}\right)} \right) +$$

$$\left( 3 b^2 d^2 f^2 g^2 (-bg+ah) \left(-\frac{f}{-be+af} + \frac{h}{-bg+ah}\right) \sqrt{\frac{-\frac{d}{-bc+ad} + \frac{1}{a+bx}}{-\frac{d}{-bc+ad} + \frac{h}{-bg+ah}}} \right.$$

$$\left. \sqrt{-\frac{\left(-\frac{f}{-be+af} + \frac{1}{a+bx}\right) \left(-\frac{h}{-bg+ah} + \frac{1}{a+bx}\right)}{\left(-\frac{f}{-be+af} + \frac{h}{-bg+ah}\right)^2}} \text{EllipticPi}\left[-\frac{-bfg+beh}{(-be+af)h}, \right. \right.$$

$$\left. \left. \text{ArcSin}\left[\sqrt{\frac{(-be+af) \left(-h - \frac{bg}{a+bx} + \frac{ah}{a+bx}\right)}{b(-fg+eh)}}\right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)}\right] \right) /$$

$$\begin{aligned}
 & \left( h \sqrt{\left( d + \frac{bc-ad}{a+bx} \right) \left( f + \frac{be-af}{a+bx} \right) \left( h + \frac{bg-ah}{a+bx} \right)} \right) + \\
 & \left( b^2 d^2 e^2 h (-bg+ah) \left( -\frac{f}{-be+af} + \frac{h}{-bg+ah} \right) \sqrt{\frac{-\frac{d}{-bc+ad} + \frac{1}{a+bx}}{-\frac{d}{-bc+ad} + \frac{h}{-bg+ah}}} \right. \\
 & \quad \sqrt{-\frac{\left( -\frac{f}{-be+af} + \frac{1}{a+bx} \right) \left( -\frac{h}{-bg+ah} + \frac{1}{a+bx} \right)}{\left( -\frac{f}{-be+af} + \frac{h}{-bg+ah} \right)^2}} \text{EllipticPi} \left[ -\frac{-bfg+beh}{(-be+af)h}, \right. \\
 & \quad \left. \left. \text{ArcSin} \left[ \sqrt{\frac{(-be+af) \left( -h - \frac{bg}{a+bx} + \frac{ah}{a+bx} \right)}{b(-fg+eh)}}, \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right) \right] / \\
 & \left( \sqrt{\left( d + \frac{bc-ad}{a+bx} \right) \left( f + \frac{be-af}{a+bx} \right) \left( h + \frac{bg-ah}{a+bx} \right)} \right) - \\
 & \left( 2b^2 c d e f h (-bg+ah) \left( -\frac{f}{-be+af} + \frac{h}{-bg+ah} \right) \sqrt{\frac{-\frac{d}{-bc+ad} + \frac{1}{a+bx}}{-\frac{d}{-bc+ad} + \frac{h}{-bg+ah}}} \right. \\
 & \quad \sqrt{-\frac{\left( -\frac{f}{-be+af} + \frac{1}{a+bx} \right) \left( -\frac{h}{-bg+ah} + \frac{1}{a+bx} \right)}{\left( -\frac{f}{-be+af} + \frac{h}{-bg+ah} \right)^2}} \text{EllipticPi} \left[ -\frac{-bfg+beh}{(-be+af)h}, \right. \\
 & \quad \left. \left. \text{ArcSin} \left[ \sqrt{\frac{(-be+af) \left( -h - \frac{bg}{a+bx} + \frac{ah}{a+bx} \right)}{b(-fg+eh)}}, \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right) \right] / \\
 & \left( \sqrt{\left( d + \frac{bc-ad}{a+bx} \right) \left( f + \frac{be-af}{a+bx} \right) \left( h + \frac{bg-ah}{a+bx} \right)} \right) + \\
 & \left( b^2 c^2 f^2 h (-bg+ah) \left( -\frac{f}{-be+af} + \frac{h}{-bg+ah} \right) \sqrt{\frac{-\frac{d}{-bc+ad} + \frac{1}{a+bx}}{-\frac{d}{-bc+ad} + \frac{h}{-bg+ah}}} \right. \\
 & \quad \sqrt{-\frac{\left( -\frac{f}{-be+af} + \frac{1}{a+bx} \right) \left( -\frac{h}{-bg+ah} + \frac{1}{a+bx} \right)}{\left( -\frac{f}{-be+af} + \frac{h}{-bg+ah} \right)^2}} \text{EllipticPi} \left[ -\frac{-bfg+beh}{(-be+af)h}, \right.
 \end{aligned}$$

$$\begin{aligned} & \left. \text{ArcSin} \left[ \sqrt{\frac{(-be+af) \left(-h - \frac{bg}{a+bx} + \frac{ah}{a+bx}\right)}{b(-fg+eh)}} \right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] / \\ & \left( \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right) \left(h + \frac{bg-ah}{a+bx}\right)} \right) + \\ & \left( 3a^2 d^2 f^2 h (-bg+ah) \left(-\frac{f}{-be+af} + \frac{h}{-bg+ah}\right) \sqrt{\frac{-\frac{d}{-bc+ad} + \frac{1}{a+bx}}{-\frac{d}{-bc+ad} + \frac{h}{-bg+ah}}} \right. \\ & \left. \sqrt{-\frac{\left(-\frac{f}{-be+af} + \frac{1}{a+bx}\right) \left(-\frac{h}{-bg+ah} + \frac{1}{a+bx}\right)}{\left(-\frac{f}{-be+af} + \frac{h}{-bg+ah}\right)^2}} \text{EllipticPi} \left[-\frac{-bfg+beh}{(-be+af)h}, \right. \right. \\ & \left. \left. \text{ArcSin} \left[ \sqrt{\frac{(-be+af) \left(-h - \frac{bg}{a+bx} + \frac{ah}{a+bx}\right)}{b(-fg+eh)}} \right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] / \right. \\ & \left. \left. \left( \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right) \left(h + \frac{bg-ah}{a+bx}\right)} \right) \right) \right) \end{aligned}$$

**Problem 12: Result more than twice size of optimal antiderivative.**

$$\int \frac{\sqrt{a+bx} (de+cf+2dfx)}{\sqrt{c+dx} \sqrt{e+fx} \sqrt{g+hx}} dx$$

Optimal (type 4, 472 leaves, 5 steps):

$$\frac{2b\sqrt{c+dx}\sqrt{e+fx}\sqrt{g+hx}}{h\sqrt{a+bx}} - \left( 2\sqrt{bg-ah}\sqrt{fg-eh}\sqrt{c+dx}\sqrt{-\frac{(be-af)(g+hx)}{(fg-eh)(a+bx)}} \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{bg-ah}\sqrt{e+fx}}{\sqrt{fg-eh}\sqrt{a+bx}}\right], -\frac{(bc-ad)(fg-eh)}{(de-cf)(bg-ah)}\right] \right) / \left( h\sqrt{\frac{(be-af)(c+dx)}{(de-cf)(a+bx)}}\sqrt{g+hx} \right) - \left( 2d(bg-ah)^{3/2}\sqrt{\frac{(fg-eh)(a+bx)}{(bg-ah)(e+fx)}}\sqrt{\frac{(fg-eh)(c+dx)}{(dg-ch)(e+fx)}}(e+fx)\operatorname{EllipticPi}\left[\frac{f(bg-ah)}{(be-af)h}, \operatorname{ArcSin}\left[\frac{\sqrt{be-af}\sqrt{g+hx}}{\sqrt{bg-ah}\sqrt{e+fx}}\right], \frac{(de-cf)(bg-ah)}{(be-af)(dg-ch)}\right] \right) / (\sqrt{be-af}h^2\sqrt{a+bx}\sqrt{c+dx})$$

Result (type 4, 6583 leaves):

$$-\frac{1}{d} 2 \left( \left( (c+dx)^{3/2} \left( f + \frac{de}{c+dx} - \frac{cf}{c+dx} \right) \left( h + \frac{dg}{c+dx} - \frac{ch}{c+dx} \right) \sqrt{a + \frac{(c+dx)(b - \frac{bc}{c+dx})}{d}} \right) / \left( h\sqrt{e + \frac{(c+dx)(f - \frac{cf}{c+dx})}{d}}\sqrt{g + \frac{(c+dx)(h - \frac{ch}{c+dx})}{d}} \right) \right) - \left( f(bg-ah)(dg-ch)^2 \sqrt{c+dx} \sqrt{\left( \left( b - \frac{bc}{c+dx} + \frac{ad}{c+dx} \right) \left( f + \frac{de}{c+dx} - \frac{cf}{c+dx} \right) \left( h + \frac{dg}{c+dx} - \frac{ch}{c+dx} \right) \right)} \sqrt{a + \frac{(c+dx)(b - \frac{bc}{c+dx})}{d}} \left( \left( de\sqrt{-\frac{(bc-ad)(-dg+ch)(-\frac{b}{bc-ad} + \frac{1}{c+dx})}{-bdg+adh}} \left( -\frac{f}{-de+cf} + \frac{1}{c+dx} \right) \sqrt{\frac{-\frac{h}{-dg+ch} + \frac{1}{c+dx}}{\frac{f}{-de+cf} - \frac{h}{-dg+ch}}} \right) \right) \left( (-bdg+adh)\operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\sqrt{\frac{(de-cf)(h + \frac{dg}{c+dx} - \frac{ch}{c+dx})}{d(-fg+eh)}}\right], \frac{(bc-ad)(-fg+eh)}{(-de+cf)(-bg+ah)}\right] \right) / \left( (bc-ad)(-dg+ch) - \frac{1}{bc-ad}b\operatorname{EllipticF}\left[ \right. \right.$$

$$\begin{aligned}
 & \left. \left. \left. \text{ArcSin} \left[ \sqrt{\frac{(de - cf) \left( h + \frac{dg}{c+dx} - \frac{ch}{c+dx} \right)}{d(-fg + eh)}} \right], \frac{(bc - ad)(-fg + eh)}{(-de + cf)(-bg + ah)} \right] \right) \right) / \\
 & \left( \sqrt{\frac{-\frac{f}{-de+cf} + \frac{1}{c+dx}}{-\frac{f}{-de+cf} + \frac{h}{-dg+ch}}} \sqrt{\left( b + \frac{-bc+ad}{c+dx} \right) \left( f + \frac{de-cf}{c+dx} \right) \left( h + \frac{dg-ch}{c+dx} \right)} \right) - \\
 & \left( cf \sqrt{-\frac{(bc - ad)(-dg + ch) \left( -\frac{b}{bc-ad} + \frac{1}{c+dx} \right)}{-bdg + adh}} \right. \\
 & \left. \left( -\frac{f}{-de + cf} + \frac{1}{c + dx} \right) \sqrt{\frac{-\frac{h}{-dg+ch} + \frac{1}{c+dx}}{\frac{f}{-de+cf} - \frac{h}{-dg+ch}}} \right. \\
 & \left. \left( (-bdg + adh) \text{EllipticE} \left[ \text{ArcSin} \left[ \sqrt{\frac{(de - cf) \left( h + \frac{dg}{c+dx} - \frac{ch}{c+dx} \right)}{d(-fg + eh)}} \right], \right. \right. \right. \\
 & \left. \left. \left. \frac{(bc - ad)(-fg + eh)}{(-de + cf)(-bg + ah)} \right] \right) \right) / \left( (bc - ad)(-dg + ch) \right) - \frac{1}{bc - ad} b \text{EllipticF} \left[ \right. \\
 & \left. \left. \left. \text{ArcSin} \left[ \sqrt{\frac{(de - cf) \left( h + \frac{dg}{c+dx} - \frac{ch}{c+dx} \right)}{d(-fg + eh)}} \right], \frac{(bc - ad)(-fg + eh)}{(-de + cf)(-bg + ah)} \right] \right) \right) / \\
 & \left( \sqrt{\frac{-\frac{f}{-de+cf} + \frac{1}{c+dx}}{-\frac{f}{-de+cf} + \frac{h}{-dg+ch}}} \sqrt{\left( b + \frac{-bc+ad}{c+dx} \right) \left( f + \frac{de-cf}{c+dx} \right) \left( h + \frac{dg-ch}{c+dx} \right)} \right) + \\
 & \left( f \sqrt{\frac{-\frac{b}{bc-ad} + \frac{1}{c+dx}}{-\frac{b}{bc-ad} + \frac{h}{-dg+ch}}} \sqrt{\frac{-\frac{f}{-de+cf} + \frac{1}{c+dx}}{-\frac{f}{-de+cf} + \frac{h}{-dg+ch}}} \left( -\frac{h}{-dg + ch} + \frac{1}{c + dx} \right) \right. \\
 & \left. \left. \left. \text{EllipticF} \left[ \text{ArcSin} \left[ \sqrt{\frac{(-de + cf) \left( -h - \frac{dg}{c+dx} + \frac{ch}{c+dx} \right)}{d(-fg + eh)}} \right], \frac{(bc - ad)(-fg + eh)}{(-de + cf)(-bg + ah)} \right] \right) \right) \right) / \\
 & \left( \sqrt{\frac{-\frac{h}{-dg+ch} + \frac{1}{c+dx}}{\frac{f}{-de+cf} - \frac{h}{-dg+ch}}} \sqrt{\left( b + \frac{-bc+ad}{c+dx} \right) \left( f + \frac{de-cf}{c+dx} \right) \left( h + \frac{dg-ch}{c+dx} \right)} \right) \right) \right) /
 \end{aligned}$$

$$\begin{aligned}
 & \left( h^2 (-fg+eh) \left( b - \frac{bc}{c+dx} + \frac{ad}{c+dx} \right) \sqrt{e + \frac{(c+dx) \left( f - \frac{cf}{c+dx} \right)}{d}} \right. \\
 & \left. \sqrt{g + \frac{(c+dx) \left( h - \frac{ch}{c+dx} \right)}{d}} \right) + \\
 & \left( (be-af) (de-cf) (dg-ch) \sqrt{c+dx} \right. \\
 & \left. \sqrt{\left( \left( b - \frac{bc}{c+dx} + \frac{ad}{c+dx} \right) \left( f + \frac{de}{c+dx} - \frac{cf}{c+dx} \right) \left( h + \frac{dg}{c+dx} - \frac{ch}{c+dx} \right) \right)} \right. \\
 & \left. \sqrt{a + \frac{(c+dx) \left( b - \frac{bc}{c+dx} \right)}{d}} \right. \\
 & \left. \left( dg \sqrt{-\frac{(bc-ad) (-dg+ch) \left( -\frac{b}{bc-ad} + \frac{1}{c+dx} \right)}{-bdg+adh}} \right. \right. \\
 & \left. \left. \left( -\frac{f}{-de+cf} + \frac{1}{c+dx} \right) \sqrt{\frac{-\frac{h}{-dg+ch} + \frac{1}{c+dx}}{\frac{f}{-de+cf} - \frac{h}{-dg+ch}}} \right. \right. \\
 & \left. \left. \left( (-bdg+adh) \text{EllipticE} \left[ \text{ArcSin} \left[ \sqrt{\frac{(de-cf) \left( h + \frac{dg}{c+dx} - \frac{ch}{c+dx} \right)}{d(-fg+eh)}} \right] \right], \right. \right. \\
 & \left. \left. \frac{(bc-ad) (-fg+eh)}{(-de+cf) (-bg+ah)} \right] \right) / \left( (bc-ad) (-dg+ch) - \frac{1}{bc-ad} b \text{EllipticF} \left[ \right. \right. \\
 & \left. \left. \text{ArcSin} \left[ \sqrt{\frac{(de-cf) \left( h + \frac{dg}{c+dx} - \frac{ch}{c+dx} \right)}{d(-fg+eh)}} \right] \right], \frac{(bc-ad) (-fg+eh)}{(-de+cf) (-bg+ah)} \right] \right) / \\
 & \left( \sqrt{\frac{-\frac{f}{-de+cf} + \frac{1}{c+dx}}{-\frac{f}{-de+cf} + \frac{h}{-dg+ch}}} \sqrt{\left( b + \frac{-bc+ad}{c+dx} \right) \left( f + \frac{de-cf}{c+dx} \right) \left( h + \frac{dg-ch}{c+dx} \right)} \right) -
 \end{aligned}$$

$$\begin{aligned}
 & \left( ch \sqrt{-\frac{(bc-ad)(-dg+ch)\left(-\frac{b}{bc-ad} + \frac{1}{c+dx}\right)}{-bdg+adh}} \right. \\
 & \left. \left(-\frac{f}{-de+cf} + \frac{1}{c+dx}\right) \sqrt{\frac{-\frac{h}{-dg+ch} + \frac{1}{c+dx}}{\frac{f}{-de+cf} - \frac{h}{-dg+ch}}} \right. \\
 & \left. \left( \left( (-bdg+adh) \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\sqrt{\frac{(de-cf)\left(h + \frac{dg}{c+dx} - \frac{ch}{c+dx}\right)}{d(-fg+eh)}}\right], \right. \right. \right. \\
 & \left. \left. \frac{(bc-ad)(-fg+eh)}{(-de+cf)(-bg+ah)} \right] \right) / \left( (bc-ad)(-dg+ch) - \frac{1}{bc-ad} b \operatorname{EllipticF}\left[ \right. \right. \\
 & \left. \left. \operatorname{ArcSin}\left[\sqrt{\frac{(de-cf)\left(h + \frac{dg}{c+dx} - \frac{ch}{c+dx}\right)}{d(-fg+eh)}}\right], \frac{(bc-ad)(-fg+eh)}{(-de+cf)(-bg+ah)} \right] \right) \right) / \\
 & \left( \sqrt{\frac{-\frac{f}{-de+cf} + \frac{1}{c+dx}}{-\frac{f}{-de+cf} + \frac{h}{-dg+ch}}} \sqrt{\left(b + \frac{-bc+ad}{c+dx}\right)\left(f + \frac{de-cf}{c+dx}\right)\left(h + \frac{dg-ch}{c+dx}\right)} \right) + \\
 & \left( h \sqrt{\frac{-\frac{b}{bc-ad} + \frac{1}{c+dx}}{-\frac{b}{bc-ad} + \frac{h}{-dg+ch}}} \sqrt{\frac{-\frac{f}{-de+cf} + \frac{1}{c+dx}}{-\frac{f}{-de+cf} + \frac{h}{-dg+ch}}} \left(-\frac{h}{-dg+ch} + \frac{1}{c+dx}\right) \right. \\
 & \left. \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\sqrt{\frac{(-de+cf)\left(-h - \frac{dg}{c+dx} + \frac{ch}{c+dx}\right)}{d(-fg+eh)}}\right], \frac{(bc-ad)(-fg+eh)}{(-de+cf)(-bg+ah)} \right] \right) / \\
 & \left( \sqrt{\frac{-\frac{h}{-dg+ch} + \frac{1}{c+dx}}{\frac{f}{-de+cf} - \frac{h}{-dg+ch}}} \sqrt{\left(b + \frac{-bc+ad}{c+dx}\right)\left(f + \frac{de-cf}{c+dx}\right)\left(h + \frac{dg-ch}{c+dx}\right)} \right) \right) / \\
 & \left( h(-fg+eh) \left(b - \frac{bc}{c+dx} + \frac{ad}{c+dx}\right) \sqrt{e + \frac{(c+dx)\left(f - \frac{cf}{c+dx}\right)}{d}} \right. \\
 & \left. \sqrt{g + \frac{(c+dx)\left(h - \frac{ch}{c+dx}\right)}{d}} \right) -
 \end{aligned}$$

$$\begin{aligned}
 & \frac{1}{h^2 \left( b - \frac{bc}{c+dx} + \frac{ad}{c+dx} \right) \sqrt{e + \frac{(c+dx) \left( f - \frac{cf}{c+dx} \right)}{d}} \sqrt{g + \frac{(c+dx) \left( h - \frac{ch}{c+dx} \right)}{d}}} \\
 & d \\
 & \frac{(bg - ah)}{\sqrt{c+dx}} \\
 & \sqrt{\left( \left( b - \frac{bc}{c+dx} + \frac{ad}{c+dx} \right) \left( f + \frac{de}{c+dx} - \frac{cf}{c+dx} \right) \left( h + \frac{dg}{c+dx} - \frac{ch}{c+dx} \right) \right)} \\
 & \sqrt{a + \frac{(c+dx) \left( b - \frac{bc}{c+dx} \right)}{d}} \\
 & \left( \left( d^2 e g \sqrt{-\frac{(bc-ad)(-dg+ch) \left( -\frac{b}{bc-ad} + \frac{1}{c+dx} \right)}{-bdg+adh}} \right. \right. \\
 & \left. \left( -\frac{f}{-de+cf} + \frac{1}{c+dx} \right) \sqrt{\frac{-\frac{h}{-dg+ch} + \frac{1}{c+dx}}{\frac{f}{-de+cf} - \frac{h}{-dg+ch}}} \right. \\
 & \left. \left( \left( (-bdg+adh) \operatorname{EllipticE} \left[ \operatorname{ArcSin} \left[ \sqrt{\frac{(de-cf) \left( h + \frac{dg}{c+dx} - \frac{ch}{c+dx} \right)}{d(-fg+eh)}} \right], \right. \right. \right. \\
 & \left. \left. \frac{(bc-ad)(-fg+eh)}{(-de+cf)(-bg+ah)} \right] \right) / \left( (bc-ad)(-dg+ch) - \frac{1}{bc-ad} b \operatorname{EllipticF} \left[ \right. \right. \\
 & \left. \left. \operatorname{ArcSin} \left[ \sqrt{\frac{(de-cf) \left( h + \frac{dg}{c+dx} - \frac{ch}{c+dx} \right)}{d(-fg+eh)}} \right], \frac{(bc-ad)(-fg+eh)}{(-de+cf)(-bg+ah)} \right] \right) \right) / \\
 & \left( \sqrt{\frac{-\frac{f}{-de+cf} + \frac{1}{c+dx}}{-\frac{f}{-de+cf} + \frac{h}{-dg+ch}}} \sqrt{\left( b + \frac{-bc+ad}{c+dx} \right) \left( f + \frac{de-cf}{c+dx} \right) \left( h + \frac{dg-ch}{c+dx} \right)} \right) - \\
 & \left( c d f g \sqrt{-\frac{(bc-ad)(-dg+ch) \left( -\frac{b}{bc-ad} + \frac{1}{c+dx} \right)}{-bdg+adh}} \right. \\
 & \left. \left( -\frac{f}{-de+cf} + \frac{1}{c+dx} \right) \sqrt{\frac{-\frac{h}{-dg+ch} + \frac{1}{c+dx}}{-\frac{f}{-de+cf} - \frac{h}{-dg+ch}}} \right)
 \end{aligned}$$

$$\left( \left( (-bdg + adh) \operatorname{EllipticE} \left[ \operatorname{ArcSin} \left[ \sqrt{\frac{(de - cf) \left( h + \frac{dg}{c+dx} - \frac{ch}{c+dx} \right)}{d(-fg + eh)}} \right], \right. \right. \right. \\
 \left. \left. \frac{(bc - ad)(-fg + eh)}{(-de + cf)(-bg + ah)} \right] \right) / \left( (bc - ad)(-dg + ch) - \frac{1}{bc - ad} b \operatorname{EllipticF} \left[ \right. \right. \\
 \left. \left. \operatorname{ArcSin} \left[ \sqrt{\frac{(de - cf) \left( h + \frac{dg}{c+dx} - \frac{ch}{c+dx} \right)}{d(-fg + eh)}} \right], \frac{(bc - ad)(-fg + eh)}{(-de + cf)(-bg + ah)} \right] \right) \right) / \\
 \left( \sqrt{\frac{-\frac{f}{-de+cf} + \frac{1}{c+dx}}{-\frac{f}{-de+cf} + \frac{h}{-dg+ch}}} \sqrt{\left( b + \frac{-bc+ad}{c+dx} \right) \left( f + \frac{de-cf}{c+dx} \right) \left( h + \frac{dg-ch}{c+dx} \right)} \right) - \\
 \left( cde h \sqrt{-\frac{(bc - ad)(-dg + ch) \left( -\frac{b}{bc - ad} + \frac{1}{c+dx} \right)}{-bdg + adh}} \right. \\
 \left. \left( -\frac{f}{-de + cf} + \frac{1}{c + dx} \right) \sqrt{\frac{-\frac{h}{-dg+ch} + \frac{1}{c+dx}}{\frac{f}{-de+cf} - \frac{h}{-dg+ch}}} \right) \\
 \left( \left( (-bdg + adh) \operatorname{EllipticE} \left[ \operatorname{ArcSin} \left[ \sqrt{\frac{(de - cf) \left( h + \frac{dg}{c+dx} - \frac{ch}{c+dx} \right)}{d(-fg + eh)}} \right], \right. \right. \right. \\
 \left. \left. \frac{(bc - ad)(-fg + eh)}{(-de + cf)(-bg + ah)} \right] \right) / \left( (bc - ad)(-dg + ch) - \frac{1}{bc - ad} b \operatorname{EllipticF} \left[ \right. \right. \\
 \left. \left. \operatorname{ArcSin} \left[ \sqrt{\frac{(de - cf) \left( h + \frac{dg}{c+dx} - \frac{ch}{c+dx} \right)}{d(-fg + eh)}} \right], \frac{(bc - ad)(-fg + eh)}{(-de + cf)(-bg + ah)} \right] \right) \right) / \\
 \left( \sqrt{\frac{-\frac{f}{-de+cf} + \frac{1}{c+dx}}{-\frac{f}{-de+cf} + \frac{h}{-dg+ch}}} \sqrt{\left( b + \frac{-bc+ad}{c+dx} \right) \left( f + \frac{de-cf}{c+dx} \right) \left( h + \frac{dg-ch}{c+dx} \right)} \right) + \\
 \left( c^2 f h \sqrt{-\frac{(bc - ad)(-dg + ch) \left( -\frac{b}{bc - ad} + \frac{1}{c+dx} \right)}{-bdg + adh}} \right)$$

$$\begin{aligned}
 & \left( -\frac{f}{-de+cf} + \frac{1}{c+dx} \right) \sqrt{\frac{-\frac{h}{-dg+ch} + \frac{1}{c+dx}}{\frac{f}{-de+cf} - \frac{h}{-dg+ch}}} \\
 & \left( \left( (-bdg+adh) \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\sqrt{\frac{(de-cf)\left(h+\frac{dg}{c+dx}-\frac{ch}{c+dx}\right)}{d(-fg+eh)}}\right], \right. \right. \\
 & \quad \left. \left. \frac{(bc-ad)(-fg+eh)}{(-de+cf)(-bg+ah)} \right] \right) / \left( (bc-ad)(-dg+ch) - \frac{1}{bc-ad} b \operatorname{EllipticF}\left[ \right. \right. \\
 & \quad \left. \left. \operatorname{ArcSin}\left[\sqrt{\frac{(de-cf)\left(h+\frac{dg}{c+dx}-\frac{ch}{c+dx}\right)}{d(-fg+eh)}}\right], \frac{(bc-ad)(-fg+eh)}{(-de+cf)(-bg+ah)} \right] \right) / \\
 & \left( \sqrt{\frac{-\frac{f}{-de+cf} + \frac{1}{c+dx}}{-\frac{f}{-de+cf} + \frac{h}{-dg+ch}}} \sqrt{\left(b + \frac{-bc+ad}{c+dx}\right) \left(f + \frac{de-cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} \right) + \\
 & \left( dfg \sqrt{\frac{-\frac{b}{bc-ad} + \frac{1}{c+dx}}{-\frac{b}{bc-ad} + \frac{h}{-dg+ch}}} \sqrt{\frac{-\frac{f}{-de+cf} + \frac{1}{c+dx}}{-\frac{f}{-de+cf} + \frac{h}{-dg+ch}}} \left( -\frac{h}{-dg+ch} + \frac{1}{c+dx} \right) \right. \\
 & \quad \left. \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\sqrt{\frac{(-de+cf)\left(-h-\frac{dg}{c+dx}+\frac{ch}{c+dx}\right)}{d(-fg+eh)}}\right], \frac{(bc-ad)(-fg+eh)}{(-de+cf)(-bg+ah)} \right] \right) / \\
 & \left( \sqrt{\frac{-\frac{h}{-dg+ch} + \frac{1}{c+dx}}{\frac{f}{-de+cf} - \frac{h}{-dg+ch}}} \sqrt{\left(b + \frac{-bc+ad}{c+dx}\right) \left(f + \frac{de-cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} \right) + \\
 & \left( de h \sqrt{\frac{-\frac{b}{bc-ad} + \frac{1}{c+dx}}{-\frac{b}{bc-ad} + \frac{h}{-dg+ch}}} \sqrt{\frac{-\frac{f}{-de+cf} + \frac{1}{c+dx}}{-\frac{f}{-de+cf} + \frac{h}{-dg+ch}}} \left( -\frac{h}{-dg+ch} + \frac{1}{c+dx} \right) \right. \\
 & \quad \left. \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\sqrt{\frac{(-de+cf)\left(-h-\frac{dg}{c+dx}+\frac{ch}{c+dx}\right)}{d(-fg+eh)}}\right], \frac{(bc-ad)(-fg+eh)}{(-de+cf)(-bg+ah)} \right] \right) / \\
 & \left( \sqrt{\frac{-\frac{h}{-dg+ch} + \frac{1}{c+dx}}{\frac{f}{-de+cf} - \frac{h}{-dg+ch}}} \sqrt{\left(b + \frac{-bc+ad}{c+dx}\right) \left(f + \frac{de-cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} \right) -
 \end{aligned}$$

$$\left( 2 c f h \sqrt{\frac{-\frac{b}{bc-ad} + \frac{1}{c+dx}}{-\frac{b}{bc-ad} + \frac{h}{-dg+ch}}} \sqrt{\frac{-\frac{f}{-de+cf} + \frac{1}{c+dx}}{-\frac{f}{-de+cf} + \frac{h}{-dg+ch}}} \left( -\frac{h}{-dg+ch} + \frac{1}{c+dx} \right) \right. \\ \left. \text{EllipticF}\left[\text{ArcSin}\left[\sqrt{\frac{(-de+cf)\left(-h - \frac{dg}{c+dx} + \frac{ch}{c+dx}\right)}{d(-fg+eh)}}\right], \frac{(bc-ad)(-fg+eh)}{(-de+cf)(-bg+ah)}\right] \right) / \\ \left( \sqrt{\frac{-\frac{h}{-dg+ch} + \frac{1}{c+dx}}{\frac{f}{-de+cf} - \frac{h}{-dg+ch}}} \sqrt{\left(b + \frac{-bc+ad}{c+dx}\right) \left(f + \frac{de-cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} \right) - \\ \left( f(-dg+ch) \left( -\frac{f}{-de+cf} + \frac{h}{-dg+ch} \right) \sqrt{\frac{-\frac{b}{bc-ad} + \frac{1}{c+dx}}{-\frac{b}{bc-ad} + \frac{h}{-dg+ch}}} \right. \\ \left. \sqrt{-\frac{\left(-\frac{f}{-de+cf} + \frac{1}{c+dx}\right) \left(-\frac{h}{-dg+ch} + \frac{1}{c+dx}\right)}{\left(-\frac{f}{-de+cf} + \frac{h}{-dg+ch}\right)^2}} \text{EllipticPi}\left[-\frac{-dfg+deh}{(-de+cf)h}, \right. \right. \\ \left. \left. \text{ArcSin}\left[\sqrt{\frac{(-de+cf)\left(-h - \frac{dg}{c+dx} + \frac{ch}{c+dx}\right)}{d(-fg+eh)}}\right], \frac{(bc-ad)(-fg+eh)}{(-de+cf)(-bg+ah)}\right] \right) / \\ \left( \sqrt{\left(b + \frac{-bc+ad}{c+dx}\right) \left(f + \frac{de-cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} \right) \right)$$

**Problem 13: Result more than twice size of optimal antiderivative.**

$$\int \frac{de+cf+2dfx}{\sqrt{a+bx} \sqrt{c+dx} \sqrt{e+fx} \sqrt{g+hx}} dx$$

Optimal (type 4, 449 leaves, 5 steps):

$$\left( 2 (bde + bcf - 2adf) \sqrt{\frac{(be - af)(c + dx)}{(de - cf)(a + bx)}} \sqrt{g + hx} \right. \\ \left. \text{EllipticF}\left[\text{ArcSin}\left[\frac{\sqrt{bg - ah} \sqrt{e + fx}}{\sqrt{fg - eh} \sqrt{a + bx}}\right], -\frac{(bc - ad)(fg - eh)}{(de - cf)(bg - ah)}\right] \right) / \\ \left( b \sqrt{bg - ah} \sqrt{fg - eh} \sqrt{c + dx} \sqrt{-\frac{(be - af)(g + hx)}{(fg - eh)(a + bx)}} \right) + \\ \left( 4df \sqrt{-dg + ch} (a + bx) \sqrt{\frac{(bg - ah)(c + dx)}{(dg - ch)(a + bx)}} \sqrt{\frac{(bg - ah)(e + fx)}{(fg - eh)(a + bx)}} \right. \\ \left. \text{EllipticPi}\left[-\frac{b(dg - ch)}{(bc - ad)h}, \text{ArcSin}\left[\frac{\sqrt{bc - ad} \sqrt{g + hx}}{\sqrt{-dg + ch} \sqrt{a + bx}}\right], \frac{(be - af)(dg - ch)}{(bc - ad)(fg - eh)}\right] \right) / \\ \left( b \sqrt{bc - ad} h \sqrt{c + dx} \sqrt{e + fx} \right)$$

Result (type 4, 1529 leaves):

$$\frac{1}{b^2 \sqrt{c + \frac{(a+bx)(d - \frac{ad}{a+bx})}{b}} \sqrt{e + \frac{(a+bx)(f - \frac{af}{a+bx})}{b}} \sqrt{g + \frac{(a+bx)(h - \frac{ah}{a+bx})}{b}}} \\ 2(a+bx)^{3/2} \sqrt{\left(d + \frac{bc}{a+bx} - \frac{ad}{a+bx}\right) \left(f + \frac{be}{a+bx} - \frac{af}{a+bx}\right) \left(h + \frac{bg}{a+bx} - \frac{ah}{a+bx}\right)} \\ \left( - \left( \left( bde \sqrt{\frac{-\frac{d}{-bc+ad} + \frac{1}{a+bx}}{-\frac{d}{-bc+ad} + \frac{h}{-bg+ah}}} \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \left(-\frac{h}{-bg+ah} + \frac{1}{a+bx}\right) \right. \right. \right. \\ \left. \left. \left. \text{EllipticF}\left[\text{ArcSin}\left[\sqrt{\frac{(-be+af)\left(-h - \frac{bg}{a+bx} + \frac{ah}{a+bx}\right)}{b(-fg+eh)}}\right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)}\right] \right) \right) / \\ \left( \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{-\frac{f}{-be+af} - \frac{h}{-bg+ah}}} \sqrt{\left(d + \frac{bc - ad}{a+bx}\right) \left(f + \frac{be - af}{a+bx}\right) \left(h + \frac{bg - ah}{a+bx}\right)} \right) - \\ \left( bcf \sqrt{\frac{-\frac{d}{-bc+ad} + \frac{1}{a+bx}}{-\frac{d}{-bc+ad} + \frac{h}{-bg+ah}}} \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \left(-\frac{h}{-bg+ah} + \frac{1}{a+bx}\right) \right)$$

$$\begin{aligned}
 & \text{EllipticF}\left[\text{ArcSin}\left[\sqrt{\frac{(-be+af)\left(-h-\frac{bg}{a+bx}+\frac{ah}{a+bx}\right)}{b(-fg+eh)}}\right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)}\right] / \\
 & \left( \sqrt{\frac{-\frac{h}{-bg+ah}+\frac{1}{a+bx}}{\frac{f}{-be+af}-\frac{h}{-bg+ah}}} \sqrt{\left(d+\frac{bc-ad}{a+bx}\right)\left(f+\frac{be-af}{a+bx}\right)\left(h+\frac{bg-ah}{a+bx}\right)} \right) + \\
 & \left( 2adf \sqrt{\frac{-\frac{d}{-bc+ad}+\frac{1}{a+bx}}{\frac{d}{-bc+ad}+\frac{h}{-bg+ah}}} \sqrt{\frac{-\frac{f}{-be+af}+\frac{1}{a+bx}}{\frac{f}{-be+af}+\frac{h}{-bg+ah}}} \left(-\frac{h}{-bg+ah}+\frac{1}{a+bx}\right) \right) \\
 & \text{EllipticF}\left[\text{ArcSin}\left[\sqrt{\frac{(-be+af)\left(-h-\frac{bg}{a+bx}+\frac{ah}{a+bx}\right)}{b(-fg+eh)}}\right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)}\right] / \\
 & \left( \sqrt{\frac{-\frac{h}{-bg+ah}+\frac{1}{a+bx}}{\frac{f}{-be+af}-\frac{h}{-bg+ah}}} \sqrt{\left(d+\frac{bc-ad}{a+bx}\right)\left(f+\frac{be-af}{a+bx}\right)\left(h+\frac{bg-ah}{a+bx}\right)} \right) + \\
 & \left( 2df(-bg+ah) \left(-\frac{f}{-be+af}+\frac{h}{-bg+ah}\right) \sqrt{\frac{-\frac{d}{-bc+ad}+\frac{1}{a+bx}}{\frac{d}{-bc+ad}+\frac{h}{-bg+ah}}} \right) \\
 & \sqrt{-\frac{\left(-\frac{f}{-be+af}+\frac{1}{a+bx}\right)\left(-\frac{h}{-bg+ah}+\frac{1}{a+bx}\right)}{\left(-\frac{f}{-be+af}+\frac{h}{-bg+ah}\right)^2}} \text{EllipticPi}\left[-\frac{-bfg+beh}{(-be+af)h}, \right. \\
 & \left. \text{ArcSin}\left[\sqrt{\frac{(-be+af)\left(-h-\frac{bg}{a+bx}+\frac{ah}{a+bx}\right)}{b(-fg+eh)}}\right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)}\right] / \\
 & \left( h \sqrt{\left(d+\frac{bc-ad}{a+bx}\right)\left(f+\frac{be-af}{a+bx}\right)\left(h+\frac{bg-ah}{a+bx}\right)} \right)
 \end{aligned}$$

**Problem 14: Result more than twice size of optimal antiderivative.**

$$\int \frac{de+cf+2dfx}{(a+bx)^{3/2} \sqrt{c+dx} \sqrt{e+fx} \sqrt{g+hx}} dx$$

Optimal (type 4, 625 leaves, 7 steps):

$$\begin{aligned}
 & \frac{2d (bde+bcf-2adf) \sqrt{a+bx} \sqrt{e+fx} \sqrt{g+hx}}{(bc-ad) (be-af) (bg-ah) \sqrt{c+dx}} - \\
 & \frac{2b (bde+bcf-2adf) \sqrt{c+dx} \sqrt{e+fx} \sqrt{g+hx}}{(bc-ad) (be-af) (bg-ah) \sqrt{a+bx}} - \\
 & \left( 2 (bde+bcf-2adf) \sqrt{dg-ch} \sqrt{fg-eh} \sqrt{a+bx} \sqrt{-\frac{(de-cf)(g+hx)}{(fg-eh)(c+dx)}} \right. \\
 & \quad \left. \text{EllipticE}\left[\text{ArcSin}\left[\frac{\sqrt{dg-ch} \sqrt{e+fx}}{\sqrt{fg-eh} \sqrt{c+dx}}\right], \frac{(bc-ad)(fg-eh)}{(be-af)(dg-ch)}\right] \right) / \\
 & \left( (bc-ad) (be-af) (bg-ah) \sqrt{\frac{(de-cf)(a+bx)}{(be-af)(c+dx)}} \sqrt{g+hx} \right) - \\
 & \left( 2d (de-cf) \sqrt{\frac{(be-af)(c+dx)}{(de-cf)(a+bx)}} \sqrt{g+hx} \right. \\
 & \quad \left. \text{EllipticF}\left[\text{ArcSin}\left[\frac{\sqrt{bg-ah} \sqrt{e+fx}}{\sqrt{fg-eh} \sqrt{a+bx}}\right], -\frac{(bc-ad)(fg-eh)}{(de-cf)(bg-ah)}\right] \right) / \\
 & \left( (bc-ad) \sqrt{bg-ah} \sqrt{fg-eh} \sqrt{c+dx} \sqrt{-\frac{(be-af)(g+hx)}{(fg-eh)(a+bx)}} \right)
 \end{aligned}$$

Result (type 4, 2236 leaves):

$$\begin{aligned}
 & -\frac{2b (bde+bcf-2adf) \sqrt{c+dx} \sqrt{e+fx} \sqrt{g+hx}}{(bc-ad) (be-af) (bg-ah) \sqrt{a+bx}} + \\
 & \frac{1}{b^2 (-bc+ad) (-be+af) (-bg+ah)} 2 \left( (-bde-bcf+2adf) (a+bx)^{5/2} \right. \\
 & \quad \left. \left( d + \frac{bc}{a+bx} - \frac{ad}{a+bx} \right) \left( f + \frac{be}{a+bx} - \frac{af}{a+bx} \right) \left( h + \frac{bg}{a+bx} - \frac{ah}{a+bx} \right) \right) / \\
 & \left( \sqrt{c + \frac{(a+bx) \left( d - \frac{ad}{a+bx} \right)}{b}} \sqrt{e + \frac{(a+bx) \left( f - \frac{af}{a+bx} \right)}{b}} \sqrt{g + \frac{(a+bx) \left( h - \frac{ah}{a+bx} \right)}{b}} \right) - \\
 & \frac{1}{\sqrt{c + \frac{(a+bx) \left( d - \frac{ad}{a+bx} \right)}{b}} \sqrt{e + \frac{(a+bx) \left( f - \frac{af}{a+bx} \right)}{b}} \sqrt{g + \frac{(a+bx) \left( h - \frac{ah}{a+bx} \right)}{b}}} (bc-ad) (be-af)
 \end{aligned}$$

$$\begin{aligned}
 & (bg - ah) (a + bx)^{3/2} \sqrt{\left( \left( d + \frac{bc}{a+bx} - \frac{ad}{a+bx} \right) \left( f + \frac{be}{a+bx} - \frac{af}{a+bx} \right) \left( h + \frac{bg}{a+bx} - \frac{ah}{a+bx} \right) \right)} \\
 & \left( - \left( \left( bde \sqrt{\frac{(bc - ad)(bg - ah) \left( -\frac{d}{-bc+ad} + \frac{1}{a+bx} \right)}{bdg - bch} \right) \left( -\frac{f}{-be+af} + \frac{1}{a+bx} \right)} \right. \right. \\
 & \quad \left. \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{-be+af} - \frac{h}{-bg+ah}} \left( - \left( \left( bdg - bch \right) \text{EllipticE} \left[ \right. \right. \right. \right. \\
 & \quad \quad \left. \left. \left. \text{ArcSin} \left[ \sqrt{\frac{(be - af) \left( h + \frac{bg}{a+bx} - \frac{ah}{a+bx} \right)}{b(-fg + eh)}} \right], \frac{(-bc + ad)(-fg + eh)}{(-be + af)(-dg + ch)} \right] \right) \right) / \right. \\
 & \quad \left. \left( (bc - ad)(bg - ah) \right) - \frac{1}{-bc + ad} d \text{EllipticF} \left[ \text{ArcSin} \left[ \right. \right. \right. \right. \\
 & \quad \quad \left. \left. \left. \sqrt{\frac{(be - af) \left( h + \frac{bg}{a+bx} - \frac{ah}{a+bx} \right)}{b(-fg + eh)}} \right], \frac{(-bc + ad)(-fg + eh)}{(-be + af)(-dg + ch)} \right] \right) \right) / \\
 & \quad \left( \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-be+af} - \frac{h}{-bg+ah}} \sqrt{\left( d + \frac{bc - ad}{a+bx} \right) \left( f + \frac{be - af}{a+bx} \right) \left( h + \frac{bg - ah}{a+bx} \right)} \right) - \\
 & \quad \left( bcf \sqrt{\frac{(bc - ad)(bg - ah) \left( -\frac{d}{-bc+ad} + \frac{1}{a+bx} \right)}{bdg - bch} \right) \left( -\frac{f}{-be+af} + \frac{1}{a+bx} \right) \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{-be+af} - \frac{h}{-bg+ah}} \right. \\
 & \quad \left. - \left( \left( (bdg - bch) \text{EllipticE} \left[ \text{ArcSin} \left[ \sqrt{\frac{(be - af) \left( h + \frac{bg}{a+bx} - \frac{ah}{a+bx} \right)}{b(-fg + eh)}} \right], \right. \right. \right. \right. \\
 & \quad \quad \left. \left. \left. \frac{(-bc + ad)(-fg + eh)}{(-be + af)(-dg + ch)} \right] \right) \right) / \left( (bc - ad)(bg - ah) \right) - \right. \\
 & \quad \left. \frac{1}{-bc + ad} d \text{EllipticF} \left[ \text{ArcSin} \left[ \sqrt{\frac{(be - af) \left( h + \frac{bg}{a+bx} - \frac{ah}{a+bx} \right)}{b(-fg + eh)}} \right], \right. \right. \\
 \end{aligned}$$

$$\left. \left. \left. \left. \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right) \right) \right) /$$

$$\left( \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right) \left(h + \frac{bg-ah}{a+bx}\right)} \right) +$$

$$\left( 2adf \sqrt{\frac{(bc-ad)(bg-ah) \left(-\frac{d}{-bc+ad} + \frac{1}{a+bx}\right)}{bdg-bch}} \left(-\frac{f}{-be+af} + \frac{1}{a+bx}\right) \right.$$

$$\left. \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{\frac{f}{-be+af} - \frac{h}{-bg+ah}}} \left( - \left( (bdg-bch) \text{EllipticE} \left[ \right. \right. \right. \right.$$

$$\left. \left. \left. \text{ArcSin} \left[ \sqrt{\frac{(be-af) \left(h + \frac{bg}{a+bx} - \frac{ah}{a+bx}\right)}{b(-fg+eh)}} \right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right) \right) /$$

$$\left( (bc-ad)(bg-ah) \right) - \frac{1}{-bc+ad} d \text{EllipticF} \left[ \text{ArcSin} \left[ \right. \right. \right.$$

$$\left. \left. \left. \sqrt{\frac{(be-af) \left(h + \frac{bg}{a+bx} - \frac{ah}{a+bx}\right)}{b(-fg+eh)}} \right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right) \right) /$$

$$\left( \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right) \left(h + \frac{bg-ah}{a+bx}\right)} \right) -$$

$$\left( 2df \sqrt{\frac{-\frac{d}{-bc+ad} + \frac{1}{a+bx}}{-\frac{d}{-bc+ad} + \frac{h}{-bg+ah}}} \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \left(-\frac{h}{-bg+ah} + \frac{1}{a+bx}\right) \right.$$

$$\left. \text{EllipticF} \left[ \text{ArcSin} \left[ \sqrt{\frac{(-be+af) \left(-h - \frac{bg}{a+bx} + \frac{ah}{a+bx}\right)}{b(-fg+eh)}} \right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right) /$$

$$\left( \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{\frac{f}{-be+af} - \frac{h}{-bg+ah}}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right) \left(h + \frac{bg-ah}{a+bx}\right)} \right) \right)$$

**Problem 15: Result more than twice size of optimal antiderivative.**

$$\int \frac{d e + c f + 2 d f x}{(a + b x)^{5/2} \sqrt{c + d x} \sqrt{e + f x} \sqrt{g + h x}} dx$$

Optimal (type 4, 1090 leaves, 8 steps):

$$\begin{aligned} & \left( 4 d \left( 3 a^3 d^2 f^2 h - a^2 b d f (d f g + 4 d e h + 4 c f h) - b^3 (d^2 e^2 g - c d e (f g - e h) + c^2 f (f g + e h)) \right) + \right. \\ & \quad \left. a b^2 (2 c^2 f^2 h + d^2 e (f g + 2 e h) + c d f (f g + 3 e h)) \right) \sqrt{a + b x} \sqrt{e + f x} \sqrt{g + h x} \Big/ \\ & \left( 3 (b c - a d)^2 (b e - a f)^2 (b g - a h)^2 \sqrt{c + d x} \right) - \\ & \frac{2 b (b d e + b c f - 2 a d f) \sqrt{c + d x} \sqrt{e + f x} \sqrt{g + h x}}{3 (b c - a d) (b e - a f) (b g - a h) (a + b x)^{3/2}} - \\ & \left( 4 b \left( 3 a^3 d^2 f^2 h - a^2 b d f (d f g + 4 d e h + 4 c f h) - b^3 (d^2 e^2 g - c d e (f g - e h) + c^2 f (f g + e h)) \right) + \right. \\ & \quad \left. a b^2 (2 c^2 f^2 h + d^2 e (f g + 2 e h) + c d f (f g + 3 e h)) \right) \sqrt{c + d x} \sqrt{e + f x} \sqrt{g + h x} \Big/ \\ & \left( 3 (b c - a d)^2 (b e - a f)^2 (b g - a h)^2 \sqrt{a + b x} \right) - \left( 4 \sqrt{d g - c h} \sqrt{f g - e h} \right. \\ & \quad \left. (3 a^3 d^2 f^2 h - a^2 b d f (d f g + 4 d e h + 4 c f h) - b^3 (d^2 e^2 g - c d e (f g - e h) + c^2 f (f g + e h)) + \right. \\ & \quad \left. a b^2 (2 c^2 f^2 h + d^2 e (f g + 2 e h) + c d f (f g + 3 e h)) \right) \sqrt{a + b x} \sqrt{-\frac{(d e - c f) (g + h x)}{(f g - e h) (c + d x)}} \\ & \left. \text{EllipticE} \left[ \text{ArcSin} \left[ \frac{\sqrt{d g - c h} \sqrt{e + f x}}{\sqrt{f g - e h} \sqrt{c + d x}} \right], \frac{(b c - a d) (f g - e h)}{(b e - a f) (d g - c h)} \right] \right) \Big/ \\ & \left( 3 (b c - a d)^2 (b e - a f)^2 (b g - a h)^2 \sqrt{\frac{(d e - c f) (a + b x)}{(b e - a f) (c + d x)}} \sqrt{g + h x} \right) + \\ & \left( 2 (d e - c f) (3 a^2 d^2 f h - a b d (d f g + 3 d e h + 2 c f h) + b^2 (2 d^2 e g - c d f g + c d e h + c^2 f h)) \right. \\ & \quad \left. \sqrt{\frac{(b e - a f) (c + d x)}{(d e - c f) (a + b x)}} \sqrt{g + h x} \right) \\ & \left. \text{EllipticF} \left[ \text{ArcSin} \left[ \frac{\sqrt{b g - a h} \sqrt{e + f x}}{\sqrt{f g - e h} \sqrt{a + b x}} \right], -\frac{(b c - a d) (f g - e h)}{(d e - c f) (b g - a h)} \right] \right) \Big/ \\ & \left( 3 (b c - a d)^2 (b e - a f) (b g - a h)^{3/2} \sqrt{f g - e h} \sqrt{c + d x} \sqrt{-\frac{(b e - a f) (g + h x)}{(f g - e h) (a + b x)}} \right) \end{aligned}$$

Result (type 4, 10601 leaves):

$$\sqrt{a + b x} \sqrt{c + d x} \sqrt{e + f x} \sqrt{g + h x} \left( -\frac{2 b (b d e + b c f - 2 a d f)}{3 (b c - a d) (b e - a f) (b g - a h) (a + b x)^2} + (4 b (b^3 d^2 e^2 g - b^3 c d e f g - a b^2 d^2 e f g + \right.$$

$$\begin{aligned}
 & \left( b^3 c^2 f^2 g - a b^2 c d f^2 g + a^2 b d^2 f^2 g + b^3 c d e^2 h - 2 a b^2 d^2 e^2 h + b^3 c^2 e f h - \right. \\
 & \left. 3 a b^2 c d e f h + 4 a^2 b d^2 e f h - 2 a b^2 c^2 f^2 h + 4 a^2 b c d f^2 h - 3 a^3 d^2 f^2 h \right) / \\
 & \left( 3 (bc - ad)^2 (be - af)^2 (bg - ah)^2 (a + bx) \right) + \\
 & \frac{1}{3 b^2 (-bc + ad)^2 (-be + af)^2 (-bg + ah)^2} \\
 & 2 \left( - \left( 2 (b^3 d^2 e^2 g - b^3 c d e f g - a b^2 d^2 e f g + b^3 c^2 f^2 g - a b^2 c d f^2 g + a^2 b d^2 f^2 g + b^3 c d e^2 h - 2 a b^2 \right. \right. \\
 & \left. \left. d^2 e^2 h + b^3 c^2 e f h - 3 a b^2 c d e f h + 4 a^2 b d^2 e f h - 2 a b^2 c^2 f^2 h + 4 a^2 b c d f^2 h - 3 a^3 d^2 \right. \right. \\
 & \left. \left. f^2 h) (a + bx)^{5/2} \left( d + \frac{bc}{a + bx} - \frac{ad}{a + bx} \right) \left( f + \frac{be}{a + bx} - \frac{af}{a + bx} \right) \left( h + \frac{bg}{a + bx} - \frac{ah}{a + bx} \right) \right) / \\
 & \left( \sqrt{c + \frac{(a + bx) \left( d - \frac{ad}{a + bx} \right)}{b}} \sqrt{e + \frac{(a + bx) \left( f - \frac{af}{a + bx} \right)}{b}} \sqrt{g + \frac{(a + bx) \left( h - \frac{ah}{a + bx} \right)}{b}} \right) + \\
 & \frac{1}{\sqrt{c + \frac{(a + bx) \left( d - \frac{ad}{a + bx} \right)}{b}} \sqrt{e + \frac{(a + bx) \left( f - \frac{af}{a + bx} \right)}{b}} \sqrt{g + \frac{(a + bx) \left( h - \frac{ah}{a + bx} \right)}{b}}} (bc - ad) (be - af) \\
 & (bg - ah) (a + bx)^{3/2} \sqrt{\left( \left( d + \frac{bc}{a + bx} - \frac{ad}{a + bx} \right) \left( f + \frac{be}{a + bx} - \frac{af}{a + bx} \right) \left( h + \frac{bg}{a + bx} - \frac{ah}{a + bx} \right) \right)} \\
 & \left( \left( 2 b^3 d^2 e^2 g \sqrt{\frac{(bc - ad) (bg - ah) \left( -\frac{d}{-bc + ad} + \frac{1}{a + bx} \right)}{bdg - bch}} \right. \right. \\
 & \left. \left( -\frac{f}{-be + af} + \frac{1}{a + bx} \right) \sqrt{\frac{-\frac{h}{-bg + ah} + \frac{1}{a + bx}}{\frac{f}{-be + af} - \frac{h}{-bg + ah}}} \right) - \left( \left( (bdg - bch) \text{EllipticE} \left[ \right. \right. \right. \\
 & \left. \left. \left. \text{ArcSin} \left[ \sqrt{\frac{(be - af) \left( h + \frac{bg}{a + bx} - \frac{ah}{a + bx} \right)}{b (-fg + eh)}} \right], \frac{(-bc + ad) (-fg + eh)}{(-be + af) (-dg + ch)} \right] \right) / \right. \\
 & \left. \left. \left. (bc - ad) (bg - ah) \right) \right) - \frac{1}{-bc + ad} d \text{EllipticF} \left[ \text{ArcSin} \left[ \right. \right. \right.
 \end{aligned}$$

$$\left( \sqrt{\frac{(be-af) \left( h + \frac{bg}{a+bx} - \frac{ah}{a+bx} \right)}{b(-fg+eh)}} \right), \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \Bigg) /$$

$$\left( \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \sqrt{\left( d + \frac{bc-ad}{a+bx} \right) \left( f + \frac{be-af}{a+bx} \right) \left( h + \frac{bg-ah}{a+bx} \right)} \right) -$$

$$\left( 2b^3 c d e f g \sqrt{\frac{(bc-ad)(bg-ah) \left( -\frac{d}{-bc+ad} + \frac{1}{a+bx} \right)}{bdg-bch}} \left( -\frac{f}{-be+af} + \frac{1}{a+bx} \right) \right.$$

$$\left. \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{\frac{f}{-be+af} - \frac{h}{-bg+ah}}} \left( \left( (bdg-bch) \text{EllipticE} \left[ \right. \right. \right. \right.$$

$$\left. \left. \left. \text{ArcSin} \left[ \sqrt{\frac{(be-af) \left( h + \frac{bg}{a+bx} - \frac{ah}{a+bx} \right)}{b(-fg+eh)}} \right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right) \right. /$$

$$\left. \left( (bc-ad)(bg-ah) \right) \right) - \frac{1}{-bc+ad} d \text{EllipticF} \left[ \text{ArcSin} \left[ \right. \right. \right.$$

$$\left. \left. \left. \sqrt{\frac{(be-af) \left( h + \frac{bg}{a+bx} - \frac{ah}{a+bx} \right)}{b(-fg+eh)}} \right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right) /$$

$$\left( \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \sqrt{\left( d + \frac{bc-ad}{a+bx} \right) \left( f + \frac{be-af}{a+bx} \right) \left( h + \frac{bg-ah}{a+bx} \right)} \right) -$$

$$\left( 2ab^2 d^2 e f g \sqrt{\frac{(bc-ad)(bg-ah) \left( -\frac{d}{-bc+ad} + \frac{1}{a+bx} \right)}{bdg-bch}} \left( -\frac{f}{-be+af} + \frac{1}{a+bx} \right) \right.$$

$$\left. \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{\frac{f}{-be+af} - \frac{h}{-bg+ah}}} \left( \left( (bdg-bch) \text{EllipticE} \left[ \right. \right. \right. \right.$$

$$\left. \left. \left. \text{ArcSin} \left[ \sqrt{\frac{(be-af) \left( h + \frac{bg}{a+bx} - \frac{ah}{a+bx} \right)}{b(-fg+eh)}} \right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right) \right) /$$

$$\begin{aligned}
 & \left( (bc-ad)(bg-ah) \right) - \frac{1}{-bc+ad} d \operatorname{EllipticF} \left[ \operatorname{ArcSin} \left[ \sqrt{\frac{(be-af) \left( h + \frac{bg}{a+bx} - \frac{ah}{a+bx} \right)}{b(-fg+eh)}}, \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right] / \\
 & \left( \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \sqrt{\left( d + \frac{bc-ad}{a+bx} \right) \left( f + \frac{be-af}{a+bx} \right) \left( h + \frac{bg-ah}{a+bx} \right)} \right) + \\
 & \left( 2b^3 c^2 f^2 g \sqrt{\frac{(bc-ad)(bg-ah) \left( -\frac{d}{-bc+ad} + \frac{1}{a+bx} \right)}{bdg-bch}} \left( -\frac{f}{-be+af} + \frac{1}{a+bx} \right) \right. \\
 & \left. \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{\frac{f}{-be+af} - \frac{h}{-bg+ah}}} \left( \left( (bdg-bch) \operatorname{EllipticE} \left[ \operatorname{ArcSin} \left[ \sqrt{\frac{(be-af) \left( h + \frac{bg}{a+bx} - \frac{ah}{a+bx} \right)}{b(-fg+eh)}}, \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right) \right) \right) / \\
 & \left( (bc-ad)(bg-ah) \right) - \frac{1}{-bc+ad} d \operatorname{EllipticF} \left[ \operatorname{ArcSin} \left[ \sqrt{\frac{(be-af) \left( h + \frac{bg}{a+bx} - \frac{ah}{a+bx} \right)}{b(-fg+eh)}}, \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right] / \\
 & \left( \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \sqrt{\left( d + \frac{bc-ad}{a+bx} \right) \left( f + \frac{be-af}{a+bx} \right) \left( h + \frac{bg-ah}{a+bx} \right)} \right) - \\
 & \left( 2ab^2 c d f^2 g \sqrt{\frac{(bc-ad)(bg-ah) \left( -\frac{d}{-bc+ad} + \frac{1}{a+bx} \right)}{bdg-bch}} \left( -\frac{f}{-be+af} + \frac{1}{a+bx} \right) \right. \\
 & \left. \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{\frac{f}{-be+af} - \frac{h}{-bg+ah}}} \left( \left( (bdg-bch) \operatorname{EllipticE} \left[ \right. \right. \right) \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left. \text{ArcSin} \left[ \sqrt{\frac{(be-af) \left( h + \frac{bg}{a+bx} - \frac{ah}{a+bx} \right)}{b(-fg+eh)}}, \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right/ \\
 & \left. \left( (bc-ad)(bg-ah) \right) - \frac{1}{-bc+ad} d \text{EllipticF} \left[ \text{ArcSin} \left[ \sqrt{\frac{(be-af) \left( h + \frac{bg}{a+bx} - \frac{ah}{a+bx} \right)}{b(-fg+eh)}}, \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right] \right/ \\
 & \left( \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \sqrt{\left( d + \frac{bc-ad}{a+bx} \right) \left( f + \frac{be-af}{a+bx} \right) \left( h + \frac{bg-ah}{a+bx} \right)} \right) + \\
 & \left( 2a^2 b d^2 f^2 g \sqrt{\frac{(bc-ad)(bg-ah) \left( -\frac{d}{-bc+ad} + \frac{1}{a+bx} \right)}{bdg-bch}} \left( -\frac{f}{-be+af} + \frac{1}{a+bx} \right) \right. \\
 & \left. \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{\frac{f}{-be+af} - \frac{h}{-bg+ah}}} \left( - \left( (bdg-bch) \text{EllipticE} \left[ \right. \right. \right. \right. \right. \\
 & \left. \left. \left. \left. \left. \text{ArcSin} \left[ \sqrt{\frac{(be-af) \left( h + \frac{bg}{a+bx} - \frac{ah}{a+bx} \right)}{b(-fg+eh)}}, \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right] \right) \right) \right) \right/ \\
 & \left. \left( (bc-ad)(bg-ah) \right) - \frac{1}{-bc+ad} d \text{EllipticF} \left[ \text{ArcSin} \left[ \sqrt{\frac{(be-af) \left( h + \frac{bg}{a+bx} - \frac{ah}{a+bx} \right)}{b(-fg+eh)}}, \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right] \right) \right/ \\
 & \left( \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \sqrt{\left( d + \frac{bc-ad}{a+bx} \right) \left( f + \frac{be-af}{a+bx} \right) \left( h + \frac{bg-ah}{a+bx} \right)} \right) + \\
 & \left( 2b^3 c d e^2 h \sqrt{\frac{(bc-ad)(bg-ah) \left( -\frac{d}{-bc+ad} + \frac{1}{a+bx} \right)}{bdg-bch}} \left( -\frac{f}{-be+af} + \frac{1}{a+bx} \right) \right)
 \end{aligned}$$

$$\begin{aligned}
 & \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{-be+af} - \frac{h}{-bg+ah}} \left( - \left( (bdg - bch) \text{EllipticE} \left[ \right. \right. \right. \\
 & \quad \left. \left. \left. \text{ArcSin} \left[ \sqrt{\frac{(be-af) \left( h + \frac{bg}{a+bx} - \frac{ah}{a+bx} \right)}{b(-fg+eh)}} \right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right) / \right. \\
 & \quad \left. \left( (bc-ad)(bg-ah) \right) \right) - \frac{1}{-bc+ad} d \text{EllipticF} \left[ \text{ArcSin} \left[ \right. \right. \\
 & \quad \left. \left. \sqrt{\frac{(be-af) \left( h + \frac{bg}{a+bx} - \frac{ah}{a+bx} \right)}{b(-fg+eh)}} \right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right) / \\
 & \left( \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-be+af} + \frac{h}{-bg+ah}} \sqrt{\left( d + \frac{bc-ad}{a+bx} \right) \left( f + \frac{be-af}{a+bx} \right) \left( h + \frac{bg-ah}{a+bx} \right)} \right) - \\
 & \left( 4ab^2d^2e^2h \sqrt{\frac{(bc-ad)(bg-ah) \left( -\frac{d}{-bc+ad} + \frac{1}{a+bx} \right)}{bdg-bch}} \left( -\frac{f}{-be+af} + \frac{1}{a+bx} \right) \right) \\
 & \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{-be+af} - \frac{h}{-bg+ah}} \left( - \left( (bdg - bch) \text{EllipticE} \left[ \right. \right. \right. \\
 & \quad \left. \left. \left. \text{ArcSin} \left[ \sqrt{\frac{(be-af) \left( h + \frac{bg}{a+bx} - \frac{ah}{a+bx} \right)}{b(-fg+eh)}} \right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right) / \right. \\
 & \quad \left. \left( (bc-ad)(bg-ah) \right) \right) - \frac{1}{-bc+ad} d \text{EllipticF} \left[ \text{ArcSin} \left[ \right. \right. \\
 & \quad \left. \left. \sqrt{\frac{(be-af) \left( h + \frac{bg}{a+bx} - \frac{ah}{a+bx} \right)}{b(-fg+eh)}} \right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right) / \\
 & \left( \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-be+af} + \frac{h}{-bg+ah}} \sqrt{\left( d + \frac{bc-ad}{a+bx} \right) \left( f + \frac{be-af}{a+bx} \right) \left( h + \frac{bg-ah}{a+bx} \right)} \right) +
 \end{aligned}$$

$$\begin{aligned}
 & \left( 2b^3 c^2 e f h \sqrt{\frac{(bc-ad)(bg-ah)\left(-\frac{d}{-bc+ad} + \frac{1}{a+bx}\right)}{bdg-bch}} \left(-\frac{f}{-be+af} + \frac{1}{a+bx}\right) \right. \\
 & \quad \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{\frac{f}{-be+af} - \frac{h}{-bg+ah}}} \left( \left( (bdg-bch) \text{EllipticE} \left[ \right. \right. \right. \\
 & \quad \left. \left. \left. \text{ArcSin} \left[ \sqrt{\frac{(be-af)\left(h + \frac{bg}{a+bx} - \frac{ah}{a+bx}\right)}{b(-fg+eh)}} \right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right) \right) / \\
 & \quad \left. \left( (bc-ad)(bg-ah) \right) - \frac{1}{-bc+ad} d \text{EllipticF} \left[ \text{ArcSin} \left[ \right. \right. \right. \\
 & \quad \left. \left. \left. \sqrt{\frac{(be-af)\left(h + \frac{bg}{a+bx} - \frac{ah}{a+bx}\right)}{b(-fg+eh)}} \right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right) \right) / \\
 & \quad \left( \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right) \left(h + \frac{bg-ah}{a+bx}\right)} \right) - \\
 & \left( 6ab^2 c d e f h \sqrt{\frac{(bc-ad)(bg-ah)\left(-\frac{d}{-bc+ad} + \frac{1}{a+bx}\right)}{bdg-bch}} \left(-\frac{f}{-be+af} + \frac{1}{a+bx}\right) \right. \\
 & \quad \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{\frac{f}{-be+af} - \frac{h}{-bg+ah}}} \left( \left( (bdg-bch) \text{EllipticE} \left[ \right. \right. \right. \\
 & \quad \left. \left. \left. \text{ArcSin} \left[ \sqrt{\frac{(be-af)\left(h + \frac{bg}{a+bx} - \frac{ah}{a+bx}\right)}{b(-fg+eh)}} \right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right) \right) / \\
 & \quad \left. \left( (bc-ad)(bg-ah) \right) - \frac{1}{-bc+ad} d \text{EllipticF} \left[ \text{ArcSin} \left[ \right. \right. \right. \\
 & \quad \left. \left. \left. \sqrt{\frac{(be-af)\left(h + \frac{bg}{a+bx} - \frac{ah}{a+bx}\right)}{b(-fg+eh)}} \right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right) \right) /
 \end{aligned}$$

$$\begin{aligned}
 & \left( \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right) \left(h + \frac{bg-ah}{a+bx}\right)} \right) + \\
 & \left( 8a^2bd^2efh \sqrt{\frac{(bc-ad)(bg-ah)\left(-\frac{d}{-bc+ad} + \frac{1}{a+bx}\right)}{bdg-bch}} \left(-\frac{f}{-be+af} + \frac{1}{a+bx}\right) \right. \\
 & \left. \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{-\frac{f}{-be+af} - \frac{h}{-bg+ah}}} \left( \left( (bdg-bch) \text{EllipticE} \left[ \right. \right. \right. \right. \\
 & \left. \left. \left. \left. \text{ArcSin} \left[ \sqrt{\frac{(be-af)\left(h + \frac{bg}{a+bx} - \frac{ah}{a+bx}\right)}{b(-fg+eh)}} \right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right) / \right. \right. \\
 & \left. \left. \left( (bc-ad)(bg-ah) \right) \right) - \frac{1}{-bc+ad} d \text{EllipticF} \left[ \text{ArcSin} \left[ \right. \right. \right. \right. \\
 & \left. \left. \left. \left. \sqrt{\frac{(be-af)\left(h + \frac{bg}{a+bx} - \frac{ah}{a+bx}\right)}{b(-fg+eh)}} \right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right) / \right. \\
 & \left. \left( \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right) \left(h + \frac{bg-ah}{a+bx}\right)} \right) - \\
 & \left( 4a^2b^2c^2f^2h \sqrt{\frac{(bc-ad)(bg-ah)\left(-\frac{d}{-bc+ad} + \frac{1}{a+bx}\right)}{bdg-bch}} \left(-\frac{f}{-be+af} + \frac{1}{a+bx}\right) \right. \\
 & \left. \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{-\frac{f}{-be+af} - \frac{h}{-bg+ah}}} \left( \left( (bdg-bch) \text{EllipticE} \left[ \right. \right. \right. \right. \right. \\
 & \left. \left. \left. \left. \text{ArcSin} \left[ \sqrt{\frac{(be-af)\left(h + \frac{bg}{a+bx} - \frac{ah}{a+bx}\right)}{b(-fg+eh)}} \right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right) / \right. \\
 & \left. \left. \left( (bc-ad)(bg-ah) \right) \right) - \frac{1}{-bc+ad} d \text{EllipticF} \left[ \text{ArcSin} \left[ \right. \right. \right. \right.
 \end{aligned}$$

$$\left( \sqrt{\frac{(be-af) \left( h + \frac{bg}{a+bx} - \frac{ah}{a+bx} \right)}{b(-fg+eh)}}, \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right) /$$

$$\left( \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \sqrt{\left( d + \frac{bc-ad}{a+bx} \right) \left( f + \frac{be-af}{a+bx} \right) \left( h + \frac{bg-ah}{a+bx} \right)} \right) +$$

$$\left( 8a^2 b c d f^2 h \sqrt{\frac{(bc-ad)(bg-ah) \left( -\frac{d}{-bc+ad} + \frac{1}{a+bx} \right)}{bdg-bch}} \left( -\frac{f}{-be+af} + \frac{1}{a+bx} \right) \right.$$

$$\left. \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{\frac{f}{-be+af} - \frac{h}{-bg+ah}}} \left( \left( (bdg-bch) \text{EllipticE} \left[ \right. \right. \right. \right.$$

$$\left. \left. \left. \left. \text{ArcSin} \left[ \sqrt{\frac{(be-af) \left( h + \frac{bg}{a+bx} - \frac{ah}{a+bx} \right)}{b(-fg+eh)}}, \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right) \right. \right. \right.$$

$$\left. \left. \left. \left. \left( (bc-ad)(bg-ah) \right) \right) - \frac{1}{-bc+ad} d \text{EllipticF} \left[ \text{ArcSin} \left[ \right. \right. \right. \right.$$

$$\left. \left. \left. \left. \sqrt{\frac{(be-af) \left( h + \frac{bg}{a+bx} - \frac{ah}{a+bx} \right)}{b(-fg+eh)}}, \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right) \right) \right) \right) /$$

$$\left( \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \sqrt{\left( d + \frac{bc-ad}{a+bx} \right) \left( f + \frac{be-af}{a+bx} \right) \left( h + \frac{bg-ah}{a+bx} \right)} \right) -$$

$$\left( 6a^3 d^2 f^2 h \sqrt{\frac{(bc-ad)(bg-ah) \left( -\frac{d}{-bc+ad} + \frac{1}{a+bx} \right)}{bdg-bch}} \left( -\frac{f}{-be+af} + \frac{1}{a+bx} \right) \right.$$

$$\left. \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{\frac{f}{-be+af} - \frac{h}{-bg+ah}}} \left( \left( (bdg-bch) \text{EllipticE} \left[ \right. \right. \right. \right.$$

$$\left. \left. \left. \left. \text{ArcSin} \left[ \sqrt{\frac{(be-af) \left( h + \frac{bg}{a+bx} - \frac{ah}{a+bx} \right)}{b(-fg+eh)}}, \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right) \right) \right) \right) /$$

$$\begin{aligned}
 & \left. \left( (bc-ad)(bg-ah) \right) - \frac{1}{-bc+ad} d \operatorname{EllipticF} \left[ \operatorname{ArcSin} \left[ \sqrt{\frac{(be-af) \left( h + \frac{bg}{a+bx} - \frac{ah}{a+bx} \right)}{b(-fg+eh)}}, \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right] \right) / \\
 & \left( \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \sqrt{\left( d + \frac{bc-ad}{a+bx} \right) \left( f + \frac{be-af}{a+bx} \right) \left( h + \frac{bg-ah}{a+bx} \right)} \right) + \\
 & \left( b^2 d^2 e f g \sqrt{\frac{-\frac{d}{-bc+ad} + \frac{1}{a+bx}}{-\frac{d}{-bc+ad} + \frac{h}{-bg+ah}}} \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \left( -\frac{h}{-bg+ah} + \frac{1}{a+bx} \right) \right) \\
 & \operatorname{EllipticF} \left[ \operatorname{ArcSin} \left[ \sqrt{\frac{(-be+af) \left( -h - \frac{bg}{a+bx} + \frac{ah}{a+bx} \right)}{b(-fg+eh)}}, \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right) / \\
 & \left( \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{\frac{f}{-be+af} - \frac{h}{-bg+ah}}} \sqrt{\left( d + \frac{bc-ad}{a+bx} \right) \left( f + \frac{be-af}{a+bx} \right) \left( h + \frac{bg-ah}{a+bx} \right)} \right) + \\
 & \left( b^2 c d f^2 g \sqrt{\frac{-\frac{d}{-bc+ad} + \frac{1}{a+bx}}{-\frac{d}{-bc+ad} + \frac{h}{-bg+ah}}} \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \left( -\frac{h}{-bg+ah} + \frac{1}{a+bx} \right) \right) \\
 & \operatorname{EllipticF} \left[ \operatorname{ArcSin} \left[ \sqrt{\frac{(-be+af) \left( -h - \frac{bg}{a+bx} + \frac{ah}{a+bx} \right)}{b(-fg+eh)}}, \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right) / \\
 & \left( \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{\frac{f}{-be+af} - \frac{h}{-bg+ah}}} \sqrt{\left( d + \frac{bc-ad}{a+bx} \right) \left( f + \frac{be-af}{a+bx} \right) \left( h + \frac{bg-ah}{a+bx} \right)} \right) - \\
 & \left( 2 a b d^2 f^2 g \sqrt{\frac{-\frac{d}{-bc+ad} + \frac{1}{a+bx}}{-\frac{d}{-bc+ad} + \frac{h}{-bg+ah}}} \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \left( -\frac{h}{-bg+ah} + \frac{1}{a+bx} \right) \right) \\
 & \operatorname{EllipticF} \left[ \operatorname{ArcSin} \left[ \sqrt{\frac{(-be+af) \left( -h - \frac{bg}{a+bx} + \frac{ah}{a+bx} \right)}{b(-fg+eh)}}, \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right) /
 \end{aligned}$$

$$\left( \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{\frac{f}{-be+af} - \frac{h}{-bg+ah}}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right) \left(h + \frac{bg-ah}{a+bx}\right)} \right) +$$

$$\left( b^2 d^2 e^2 h \sqrt{\frac{-\frac{d}{-bc+ad} + \frac{1}{a+bx}}{-\frac{d}{-bc+ad} + \frac{h}{-bg+ah}}} \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \left(-\frac{h}{-bg+ah} + \frac{1}{a+bx}\right) \right.$$

$$\left. \text{EllipticF}\left[\text{ArcSin}\left[\sqrt{\frac{(-be+af) \left(-h - \frac{bg}{a+bx} + \frac{ah}{a+bx}\right)}{b(-fg+eh)}}\right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)}\right] \right) /$$

$$\left( \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{\frac{f}{-be+af} - \frac{h}{-bg+ah}}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right) \left(h + \frac{bg-ah}{a+bx}\right)} \right) +$$

$$\left( 2 b^2 c d e f h \sqrt{\frac{-\frac{d}{-bc+ad} + \frac{1}{a+bx}}{-\frac{d}{-bc+ad} + \frac{h}{-bg+ah}}} \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \left(-\frac{h}{-bg+ah} + \frac{1}{a+bx}\right) \right.$$

$$\left. \text{EllipticF}\left[\text{ArcSin}\left[\sqrt{\frac{(-be+af) \left(-h - \frac{bg}{a+bx} + \frac{ah}{a+bx}\right)}{b(-fg+eh)}}\right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)}\right] \right) /$$

$$\left( \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{\frac{f}{-be+af} - \frac{h}{-bg+ah}}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right) \left(h + \frac{bg-ah}{a+bx}\right)} \right) -$$

$$\left( 5 a b d^2 e f h \sqrt{\frac{-\frac{d}{-bc+ad} + \frac{1}{a+bx}}{-\frac{d}{-bc+ad} + \frac{h}{-bg+ah}}} \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \left(-\frac{h}{-bg+ah} + \frac{1}{a+bx}\right) \right.$$

$$\left. \text{EllipticF}\left[\text{ArcSin}\left[\sqrt{\frac{(-be+af) \left(-h - \frac{bg}{a+bx} + \frac{ah}{a+bx}\right)}{b(-fg+eh)}}\right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)}\right] \right) /$$

$$\left( \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{\frac{f}{-be+af} - \frac{h}{-bg+ah}}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right) \left(h + \frac{bg-ah}{a+bx}\right)} \right) +$$

$$\left( b^2 c^2 f^2 h \sqrt{\frac{-\frac{d}{-bc+ad} + \frac{1}{a+bx}}{-\frac{d}{-bc+ad} + \frac{h}{-bg+ah}}} \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \left(-\frac{h}{-bg+ah} + \frac{1}{a+bx}\right) \right)$$

$$\begin{aligned}
 & \left. \text{EllipticF}\left[\text{ArcSin}\left[\sqrt{\frac{(-be+af)\left(-h-\frac{bg}{a+bx}+\frac{ah}{a+bx}\right)}{b(-fg+eh)}}\right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)}\right]\right/ \\
 & \left(\sqrt{\frac{-\frac{h}{-bg+ah}+\frac{1}{a+bx}}{\frac{f}{-be+af}-\frac{h}{-bg+ah}}}\sqrt{\left(d+\frac{bc-ad}{a+bx}\right)\left(f+\frac{be-af}{a+bx}\right)\left(h+\frac{bg-ah}{a+bx}\right)}\right) - \\
 & \left(5abcd f^2 h \sqrt{\frac{-\frac{d}{-bc+ad}+\frac{1}{a+bx}}{-\frac{d}{-bc+ad}+\frac{h}{-bg+ah}}}\sqrt{\frac{-\frac{f}{-be+af}+\frac{1}{a+bx}}{-\frac{f}{-be+af}+\frac{h}{-bg+ah}}}\left(-\frac{h}{-bg+ah}+\frac{1}{a+bx}\right)\right) \\
 & \left. \text{EllipticF}\left[\text{ArcSin}\left[\sqrt{\frac{(-be+af)\left(-h-\frac{bg}{a+bx}+\frac{ah}{a+bx}\right)}{b(-fg+eh)}}\right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)}\right]\right/ \\
 & \left(\sqrt{\frac{-\frac{h}{-bg+ah}+\frac{1}{a+bx}}{\frac{f}{-be+af}-\frac{h}{-bg+ah}}}\sqrt{\left(d+\frac{bc-ad}{a+bx}\right)\left(f+\frac{be-af}{a+bx}\right)\left(h+\frac{bg-ah}{a+bx}\right)}\right) + \\
 & \left(6a^2 d^2 f^2 h \sqrt{\frac{-\frac{d}{-bc+ad}+\frac{1}{a+bx}}{-\frac{d}{-bc+ad}+\frac{h}{-bg+ah}}}\sqrt{\frac{-\frac{f}{-be+af}+\frac{1}{a+bx}}{-\frac{f}{-be+af}+\frac{h}{-bg+ah}}}\left(-\frac{h}{-bg+ah}+\frac{1}{a+bx}\right)\right) \\
 & \left. \text{EllipticF}\left[\text{ArcSin}\left[\sqrt{\frac{(-be+af)\left(-h-\frac{bg}{a+bx}+\frac{ah}{a+bx}\right)}{b(-fg+eh)}}\right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)}\right]\right/ \\
 & \left(\sqrt{\frac{-\frac{h}{-bg+ah}+\frac{1}{a+bx}}{\frac{f}{-be+af}-\frac{h}{-bg+ah}}}\sqrt{\left(d+\frac{bc-ad}{a+bx}\right)\left(f+\frac{be-af}{a+bx}\right)\left(h+\frac{bg-ah}{a+bx}\right)}\right)
 \end{aligned}$$

**Problem 16: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{(a+bx)(abB - a^2C + b^2Bx + b^2Cx^2)}{\sqrt{c+dx}\sqrt{e+fx}\sqrt{g+hx}} dx$$

Optimal (type 4, 721 leaves, 8 steps):

$$\frac{1}{15 d^2 f^2 h^2} 2 b^2 (5 b B d f h + 2 C (a d f h - 2 b (d f g + d e h + c f h))) \sqrt{c+d x} \sqrt{e+f x} \sqrt{g+h x} + \frac{2 b^2 C (a+b x) \sqrt{c+d x} \sqrt{e+f x} \sqrt{g+h x}}{5 d f h} -$$

$$\left( 2 b \sqrt{-d e+c f} (15 a^2 C d^2 f^2 h^2 - 10 a b d f h (3 B d f h - C (d f g + d e h + c f h))) + \right.$$

$$\left. b^2 (10 B d f h (d f g + d e h + c f h) - C (8 c^2 f^2 h^2 + 7 c d f h (f g + e h) + d^2 (8 f^2 g^2 + 7 e f g h + 8 e^2 h^2))) \right)$$

$$\sqrt{\frac{d (e+f x)}{d e-c f}} \sqrt{g+h x} \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{f} \sqrt{c+d x}}{\sqrt{-d e+c f}}\right], \frac{(d e-c f) h}{f (d g-c h)}\right] \Big/$$

$$\left( 15 d^3 f^{5/2} h^3 \sqrt{e+f x} \sqrt{\frac{d (g+h x)}{d g-c h}} \right) - \frac{1}{15 d^3 f^{5/2} h^3 \sqrt{e+f x} \sqrt{g+h x}}$$

$$2 \sqrt{-d e+c f} (15 a^3 C d^2 f^2 h^3 - 15 a^2 b d^2 f^2 h^2 (C g+B h) + 5 a b^2 d f h (6 B d f g h - C (c h (f g-e h) + d g (2 f g+e h)))) - b^3 (5 B d f h (c h (f g-e h) + d g (2 f g+e h)) - C (4 c^2 f h^2 (f g-e h) + c d h (3 f^2 g^2 + e f g h - 4 e^2 h^2) + d^2 g (8 f^2 g^2 + 3 e f g h + 4 e^2 h^2)))$$

$$\sqrt{\frac{d (e+f x)}{d e-c f}} \sqrt{\frac{d (g+h x)}{d g-c h}} \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{f} \sqrt{c+d x}}{\sqrt{-d e+c f}}\right], \frac{(d e-c f) h}{f (d g-c h)}\right]$$

Result (type 4, 12665 leaves):

$$\sqrt{c+d x} \sqrt{e+f x} \left( \frac{2 b^2 (-4 b C d f g - 4 b C d e h - 4 b c C f h + 5 b B d f h + 5 a C d f h)}{15 d^2 f^2 h^2} + \frac{2 b^3 C x}{5 d f h} \right) \sqrt{g+h x} +$$

$$\frac{1}{15 d^4 f^2 h^2} 2 \left( - \frac{1}{f h \sqrt{e + \frac{(c+d x) (f - \frac{c f}{c+d x})}{d}} \sqrt{g + \frac{(c+d x) (h - \frac{c h}{c+d x})}{d}}} b (-8 b^2 C d^2 f^2 g^2 - 7 b^2 C d^2 e f g h - 7 b^2 c C d f^2 g h + 10 b^2 B d^2 f^2 g h + 10 a b C d^2 f^2 g h - 8 b^2 C d^2 e^2 h^2 - 7 b^2 c C d e f h^2 + 10 b^2 B d^2 e f h^2 + 10 a b C d^2 e f h^2 - 8 b^2 c^2 C f^2 h^2 + 10 b^2 B c d f^2 h^2 + 10 a b c C d f^2 h^2 - 30 a b B d^2 f^2 h^2 + 15 a^2 C d^2 f^2 h^2) (c+d x)^{3/2} \left( f + \frac{d e}{c+d x} - \frac{c f}{c+d x} \right) \left( h + \frac{d g}{c+d x} - \frac{c h}{c+d x} \right) - \frac{1}{f h \sqrt{e + \frac{(c+d x) (f - \frac{c f}{c+d x})}{d}} \sqrt{g + \frac{(c+d x) (h - \frac{c h}{c+d x})}{d}}} (c+d x) \right)$$

$$\begin{aligned}
 & \sqrt{\left(f + \frac{de}{c+dx} - \frac{cf}{c+dx}\right) \left(h + \frac{dg}{c+dx} - \frac{ch}{c+dx}\right)} \left( \left( 8 i b^3 C d^4 e f^2 g^3 h \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \right. \right. \\
 & \left. \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \left( \text{EllipticE}\left[ i \text{ArcSinh}\left[ \frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] - \right. \right. \\
 & \left. \left. \text{EllipticF}\left[ i \text{ArcSinh}\left[ \frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) \right) / \\
 & \left( \sqrt{-\frac{-de+cf}{f}} (-dg+ch) \sqrt{\left(f + \frac{de-cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} \right) - \left( 8 i b^3 c C d^3 \right. \\
 & \left. f^3 g^3 h \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \left( \text{EllipticE}\left[ i \text{ArcSinh}\left[ \frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}} \right], \right. \right. \\
 & \left. \left. \frac{f(-dg+ch)}{(-de+cf)h} \right] - \text{EllipticF}\left[ i \text{ArcSinh}\left[ \frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) \right) / \\
 & \left( \sqrt{-\frac{-de+cf}{f}} (-dg+ch) \sqrt{\left(f + \frac{de-cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} \right) + \left( 7 i b^3 C d^4 \right. \\
 & \left. e^2 f g^2 h^2 \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \left( \text{EllipticE}\left[ i \text{ArcSinh}\left[ \frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}} \right], \right. \right. \right.
 \end{aligned}$$

$$\left. \left. \left. \frac{f(-dg+ch)}{(-de+cf)h} \right] - \text{EllipticF} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) \right) /$$

$$\left( \sqrt{-\frac{de+cf}{f}} (-dg+ch) \sqrt{\left(f + \frac{de-cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} \right) -$$

$$\left( 8 i b^3 c C d^3 e f^2 g^2 h^2 \sqrt{1 - \frac{de+cf}{f(c+dx)}} \sqrt{1 - \frac{dg+ch}{h(c+dx)}} \right)$$

$$\left( \text{EllipticE} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] - \right.$$

$$\left. \left. \left. \text{EllipticF} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) \right) \right) /$$

$$\left( \sqrt{-\frac{de+cf}{f}} (-dg+ch) \sqrt{\left(f + \frac{de-cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} \right) -$$

$$\left( 10 i b^3 B d^4 e f^2 g^2 h^2 \sqrt{1 - \frac{de+cf}{f(c+dx)}} \sqrt{1 - \frac{dg+ch}{h(c+dx)}} \right)$$

$$\left( \text{EllipticE} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] - \right.$$

$$\left. \left. \left. \text{EllipticF} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) \right) \right) /$$

$$\begin{aligned}
 & \left( \sqrt{-\frac{-de+cf}{f}} (-dg+ch) \sqrt{\left(f + \frac{de-cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} \right) - \\
 & \left( 10 i a b^2 C d^4 e f^2 g^2 h^2 \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \right. \\
 & \left( \text{EllipticE}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}}\right], \frac{f(-dg+ch)}{(-de+cf)h}\right] - \right. \\
 & \left. \left. \text{EllipticF}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}}\right], \frac{f(-dg+ch)}{(-de+cf)h}\right] \right) \right) / \\
 & \left( \sqrt{-\frac{-de+cf}{f}} (-dg+ch) \sqrt{\left(f + \frac{de-cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} \right) + \\
 & \left( i b^3 c^2 C d^2 f^3 g^2 h^2 \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \right. \\
 & \left( \text{EllipticE}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}}\right], \frac{f(-dg+ch)}{(-de+cf)h}\right] - \right. \\
 & \left. \left. \text{EllipticF}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}}\right], \frac{f(-dg+ch)}{(-de+cf)h}\right] \right) \right) / \\
 & \left( \sqrt{-\frac{-de+cf}{f}} (-dg+ch) \sqrt{\left(f + \frac{de-cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} \right) +
 \end{aligned}$$

$$\left( 10 i b^3 B c d^3 f^3 g^2 h^2 \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \right.$$

$$\left( \text{EllipticE} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] - \right.$$

$$\left. \left. \text{EllipticF} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) \right) /$$

$$\left( \sqrt{-\frac{-de+cf}{f}} (-dg+ch) \sqrt{\left( f + \frac{de-cf}{c+dx} \right) \left( h + \frac{dg-ch}{c+dx} \right)} \right) +$$

$$\left( 10 i a b^2 c C d^3 f^3 g^2 h^2 \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \right.$$

$$\left( \text{EllipticE} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] - \right.$$

$$\left. \left. \text{EllipticF} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) \right) /$$

$$\left( \sqrt{-\frac{-de+cf}{f}} (-dg+ch) \sqrt{\left( f + \frac{de-cf}{c+dx} \right) \left( h + \frac{dg-ch}{c+dx} \right)} \right) +$$

$$\left( 8 i b^3 C d^4 e^3 g h^3 \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \right)$$

$$\left( \text{EllipticE} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] - \right.$$

$$\left. \left. \text{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) \right) /$$

$$\left( \sqrt{-\frac{de+cf}{f}} (-dg+ch) \sqrt{\left(f + \frac{de-cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} \right) -$$

$$\left( 8 i b^3 c C d^3 e^2 f g h^3 \sqrt{1 - \frac{de+cf}{f(c+dx)}} \sqrt{1 - \frac{dg+ch}{h(c+dx)}} \right)$$

$$\left( \text{EllipticE} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] - \right.$$

$$\left. \left. \text{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) \right) /$$

$$\left( \sqrt{-\frac{de+cf}{f}} (-dg+ch) \sqrt{\left(f + \frac{de-cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} \right) -$$

$$\left( 10 i b^3 B d^4 e^2 f g h^3 \sqrt{1 - \frac{de+cf}{f(c+dx)}} \sqrt{1 - \frac{dg+ch}{h(c+dx)}} \right)$$

$$\left( \text{EllipticE} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] - \right.$$

$$\begin{aligned}
 & \left. \left( \text{EllipticF} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) \right) / \\
 & \left( \sqrt{-\frac{de+cf}{f}} (-dg+ch) \sqrt{\left(f + \frac{de-cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} \right) - \\
 & \left( 10 i a b^2 C d^4 e^2 f g h^3 \sqrt{1 - \frac{de+cf}{f(c+dx)}} \sqrt{1 - \frac{dg+ch}{h(c+dx)}} \right. \\
 & \left. \left( \text{EllipticE} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) - \right. \\
 & \left. \left. \left( \text{EllipticF} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) \right) \right) / \\
 & \left( \sqrt{-\frac{de+cf}{f}} (-dg+ch) \sqrt{\left(f + \frac{de-cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} \right) + \\
 & \left( i b^3 c^2 C d^2 e f^2 g h^3 \sqrt{1 - \frac{de+cf}{f(c+dx)}} \sqrt{1 - \frac{dg+ch}{h(c+dx)}} \right. \\
 & \left. \left( \text{EllipticE} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) - \right. \\
 & \left. \left. \left( \text{EllipticF} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) \right) \right) /
 \end{aligned}$$

$$\begin{aligned}
 & \left( \sqrt{-\frac{-de+cf}{f}} (-dg+ch) \sqrt{\left(f + \frac{de-cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} \right) + \\
 & \left( 10 i b^3 B c d^3 e f^2 g h^3 \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \right. \\
 & \left( \text{EllipticE}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}}\right], \frac{f(-dg+ch)}{(-de+cf)h}\right] - \right. \\
 & \left. \left. \text{EllipticF}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}}\right], \frac{f(-dg+ch)}{(-de+cf)h}\right]\right] \right) / \\
 & \left( \sqrt{-\frac{-de+cf}{f}} (-dg+ch) \sqrt{\left(f + \frac{de-cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} \right) + \\
 & \left( 10 i a b^2 c C d^3 e f^2 g h^3 \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \right. \\
 & \left( \text{EllipticE}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}}\right], \frac{f(-dg+ch)}{(-de+cf)h}\right] - \right. \\
 & \left. \left. \text{EllipticF}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}}\right], \frac{f(-dg+ch)}{(-de+cf)h}\right]\right] \right) / \\
 & \left( \sqrt{-\frac{-de+cf}{f}} (-dg+ch) \sqrt{\left(f + \frac{de-cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} \right) +
 \end{aligned}$$

$$\left( 30 i a b^2 B d^4 e f^2 g h^3 \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \right.$$

$$\left( \text{EllipticE} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] - \right.$$

$$\left. \left. \text{EllipticF} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) \right) /$$

$$\left( \sqrt{-\frac{-de+cf}{f}} (-dg+ch) \sqrt{\left( f + \frac{de-cf}{c+dx} \right) \left( h + \frac{dg-ch}{c+dx} \right)} \right) -$$

$$\left( 15 i a^2 b C d^4 e f^2 g h^3 \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \right.$$

$$\left( \text{EllipticE} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] - \right.$$

$$\left. \left. \text{EllipticF} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) \right) /$$

$$\left( \sqrt{-\frac{-de+cf}{f}} (-dg+ch) \sqrt{\left( f + \frac{de-cf}{c+dx} \right) \left( h + \frac{dg-ch}{c+dx} \right)} \right) -$$

$$\left( i b^3 c^3 C d f^3 g h^3 \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \right.$$

$$\left( \text{EllipticE} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] - \right.$$

$$\left. \text{EllipticF} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) /$$

$$\left( \sqrt{-\frac{de+cf}{f}} (-dg+ch) \sqrt{\left( f + \frac{de-cf}{c+dx} \right) \left( h + \frac{dg-ch}{c+dx} \right)} \right) -$$

$$\left( 30 i a b^2 B c d^3 f^3 g h^3 \sqrt{1 - \frac{de+cf}{f(c+dx)}} \sqrt{1 - \frac{dg+ch}{h(c+dx)}} \right)$$

$$\left( \text{EllipticE} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] - \right.$$

$$\left. \text{EllipticF} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) /$$

$$\left( \sqrt{-\frac{de+cf}{f}} (-dg+ch) \sqrt{\left( f + \frac{de-cf}{c+dx} \right) \left( h + \frac{dg-ch}{c+dx} \right)} \right) +$$

$$\left( 15 i a^2 b c C d^3 f^3 g h^3 \sqrt{1 - \frac{de+cf}{f(c+dx)}} \sqrt{1 - \frac{dg+ch}{h(c+dx)}} \right)$$

$$\left( \text{EllipticE} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] - \right.$$

$$\begin{aligned}
 & \left. \left. \left. \text{EllipticF}\left[\text{i ArcSinh}\left[\frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}}\right], \frac{f(-dg+ch)}{(-de+cf)h}\right]\right] \right) \right) / \\
 & \left( \sqrt{-\frac{de+cf}{f}} (-dg+ch) \sqrt{\left(f + \frac{de-cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} \right) - \\
 & \left( 8 \text{i} b^3 c C d^3 e^3 h^4 \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \right) \\
 & \left( \left. \left. \left. \text{EllipticE}\left[\text{i ArcSinh}\left[\frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}}\right], \frac{f(-dg+ch)}{(-de+cf)h}\right]\right] \right) \right) - \\
 & \left. \left. \left. \text{EllipticF}\left[\text{i ArcSinh}\left[\frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}}\right], \frac{f(-dg+ch)}{(-de+cf)h}\right]\right] \right) \right) / \\
 & \left( \sqrt{-\frac{de+cf}{f}} (-dg+ch) \sqrt{\left(f + \frac{de-cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} \right) + \\
 & \left( \text{i} b^3 c^2 C d^2 e^2 f h^4 \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \right) \\
 & \left( \left. \left. \left. \text{EllipticE}\left[\text{i ArcSinh}\left[\frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}}\right], \frac{f(-dg+ch)}{(-de+cf)h}\right]\right] \right) \right) - \\
 & \left. \left. \left. \text{EllipticF}\left[\text{i ArcSinh}\left[\frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}}\right], \frac{f(-dg+ch)}{(-de+cf)h}\right]\right] \right) \right) /
 \end{aligned}$$

$$\begin{aligned}
 & \left( \sqrt{-\frac{-de+cf}{f}} (-dg+ch) \sqrt{\left(f + \frac{de-cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} \right) + \\
 & \left( 10 i b^3 B c d^3 e^2 f h^4 \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \right. \\
 & \left( \text{EllipticE}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}}\right], \frac{f(-dg+ch)}{(-de+cf)h}\right] - \right. \\
 & \left. \left. \text{EllipticF}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}}\right], \frac{f(-dg+ch)}{(-de+cf)h}\right]\right] \right) / \\
 & \left( \sqrt{-\frac{-de+cf}{f}} (-dg+ch) \sqrt{\left(f + \frac{de-cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} \right) + \\
 & \left( 10 i a b^2 c C d^3 e^2 f h^4 \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \right. \\
 & \left( \text{EllipticE}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}}\right], \frac{f(-dg+ch)}{(-de+cf)h}\right] - \right. \\
 & \left. \left. \text{EllipticF}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}}\right], \frac{f(-dg+ch)}{(-de+cf)h}\right]\right] \right) / \\
 & \left( \sqrt{-\frac{-de+cf}{f}} (-dg+ch) \sqrt{\left(f + \frac{de-cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} \right) -
 \end{aligned}$$

$$\left( \begin{aligned} & i b^3 c^3 C d e f^2 h^4 \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \\ & \left( \begin{aligned} & \text{EllipticE} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] - \\ & \text{EllipticF} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) / \\ & \left( \sqrt{-\frac{-de+cf}{f}} (-dg+ch) \sqrt{\left( f + \frac{de-cf}{c+dx} \right) \left( h + \frac{dg-ch}{c+dx} \right)} \right) - \\ & 30 i a b^2 B c d^3 e f^2 h^4 \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \\ & \left( \begin{aligned} & \text{EllipticE} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] - \\ & \text{EllipticF} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) / \\ & \left( \sqrt{-\frac{-de+cf}{f}} (-dg+ch) \sqrt{\left( f + \frac{de-cf}{c+dx} \right) \left( h + \frac{dg-ch}{c+dx} \right)} \right) + \\ & 15 i a^2 b c C d^3 e f^2 h^4 \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \end{aligned} \right)
 \end{aligned} \right)$$

$$\left( \text{EllipticE} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] - \right.$$

$$\left. \text{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) /$$

$$\left( \sqrt{-\frac{de+cf}{f}} (-dg+ch) \sqrt{\left( f + \frac{de-cf}{c+dx} \right) \left( h + \frac{dg-ch}{c+dx} \right)} \right) +$$

$$\left( 8 i b^3 c^4 C f^3 h^4 \sqrt{1 - \frac{de+cf}{f(c+dx)}} \sqrt{1 - \frac{dg+ch}{h(c+dx)}} \left( \text{EllipticE} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \right. \right. \right.$$

$$\left. \left. \frac{f(-dg+ch)}{(-de+cf)h} \right] - \text{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) \right) /$$

$$\left( \sqrt{-\frac{de+cf}{f}} (-dg+ch) \sqrt{\left( f + \frac{de-cf}{c+dx} \right) \left( h + \frac{dg-ch}{c+dx} \right)} \right) -$$

$$\left( 10 i b^3 B c^3 d f^3 h^4 \sqrt{1 - \frac{de+cf}{f(c+dx)}} \sqrt{1 - \frac{dg+ch}{h(c+dx)}} \right.$$

$$\left( \text{EllipticE} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] - \right.$$

$$\left. \left. \text{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) \right) /$$

$$\begin{aligned}
 & \left( \sqrt{-\frac{-de+cf}{f}} (-dg+ch) \sqrt{\left(f+\frac{de-cf}{c+dx}\right) \left(h+\frac{dg-ch}{c+dx}\right)} \right) - \\
 & \left( 10 i a b^2 c^3 C d f^3 h^4 \sqrt{1-\frac{-de+cf}{f(c+dx)}} \sqrt{1-\frac{-dg+ch}{h(c+dx)}} \right. \\
 & \left( \text{EllipticE}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}}\right], \frac{f(-dg+ch)}{(-de+cf)h}\right] - \right. \\
 & \left. \left. \text{EllipticF}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}}\right], \frac{f(-dg+ch)}{(-de+cf)h}\right] \right) \right) / \\
 & \left( \sqrt{-\frac{-de+cf}{f}} (-dg+ch) \sqrt{\left(f+\frac{de-cf}{c+dx}\right) \left(h+\frac{dg-ch}{c+dx}\right)} \right) + \\
 & \left( 30 i a b^2 B c^2 d^2 f^3 h^4 \sqrt{1-\frac{-de+cf}{f(c+dx)}} \sqrt{1-\frac{-dg+ch}{h(c+dx)}} \right. \\
 & \left( \text{EllipticE}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}}\right], \frac{f(-dg+ch)}{(-de+cf)h}\right] - \right. \\
 & \left. \left. \text{EllipticF}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}}\right], \frac{f(-dg+ch)}{(-de+cf)h}\right] \right) \right) / \\
 & \left( \sqrt{-\frac{-de+cf}{f}} (-dg+ch) \sqrt{\left(f+\frac{de-cf}{c+dx}\right) \left(h+\frac{dg-ch}{c+dx}\right)} \right) -
 \end{aligned}$$

$$\left( 15 i a^2 b c^2 C d^2 f^3 h^4 \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \right.$$

$$\left( \text{EllipticE} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] - \right.$$

$$\left. \left. \text{EllipticF} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) \right) /$$

$$\left( \sqrt{-\frac{-de+cf}{f}} (-dg+ch) \sqrt{\left( f + \frac{de-cf}{c+dx} \right) \left( h + \frac{dg-ch}{c+dx} \right)} \right) -$$

$$\left( 4 i b^3 C d^3 e f^2 g^2 h \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \right.$$

$$\left. \left. \text{EllipticF} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) \right) /$$

$$\left( \sqrt{-\frac{-de+cf}{f}} \sqrt{\left( f + \frac{de-cf}{c+dx} \right) \left( h + \frac{dg-ch}{c+dx} \right)} \right) +$$

$$\left( 4 i b^3 c C d^2 f^3 g^2 h \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \right.$$

$$\left. \left. \text{EllipticF} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) \right) /$$

$$\left( \sqrt{-\frac{de+cf}{f}} \sqrt{\left(f + \frac{de-cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} \right) -$$

$$\left( 4 i b^3 C d^3 e^2 f g h^2 \sqrt{1 - \frac{de+cf}{f(c+dx)}} \sqrt{1 - \frac{dg+ch}{h(c+dx)}} \right.$$

$$\left. \text{EllipticF}\left[ i \text{ArcSinh}\left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) /$$

$$\left( \sqrt{-\frac{de+cf}{f}} \sqrt{\left(f + \frac{de-cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} \right) +$$

$$\left( i b^3 c C d^2 e f^2 g h^2 \sqrt{1 - \frac{de+cf}{f(c+dx)}} \sqrt{1 - \frac{dg+ch}{h(c+dx)}} \right.$$

$$\left. \text{EllipticF}\left[ i \text{ArcSinh}\left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) /$$

$$\left( \sqrt{-\frac{de+cf}{f}} \sqrt{\left(f + \frac{de-cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} \right) +$$

$$\left( 5 i b^3 B d^3 e f^2 g h^2 \sqrt{1 - \frac{de+cf}{f(c+dx)}} \sqrt{1 - \frac{dg+ch}{h(c+dx)}} \right.$$

$$\left. \text{EllipticF}\left[ i \text{ArcSinh}\left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) /$$

$$\left( \sqrt{-\frac{de+cf}{f}} \sqrt{\left(f + \frac{de-cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} \right) +$$

$$\left( 5 i a b^2 C d^3 e f^2 g h^2 \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \right. \\ \left. \text{EllipticF}\left[ i \text{ArcSinh}\left[ \frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) /$$

$$\left( \sqrt{-\frac{-de+cf}{f}} \sqrt{\left( f + \frac{de-cf}{c+dx} \right) \left( h + \frac{dg-ch}{c+dx} \right)} \right) +$$

$$\left( 3 i b^3 c^2 C d f^3 g h^2 \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \right. \\ \left. \text{EllipticF}\left[ i \text{ArcSinh}\left[ \frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) /$$

$$\left( \sqrt{-\frac{-de+cf}{f}} \sqrt{\left( f + \frac{de-cf}{c+dx} \right) \left( h + \frac{dg-ch}{c+dx} \right)} \right) -$$

$$\left( 5 i b^3 B c d^2 f^3 g h^2 \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \right. \\ \left. \text{EllipticF}\left[ i \text{ArcSinh}\left[ \frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) /$$

$$\left( \sqrt{-\frac{-de+cf}{f}} \sqrt{\left( f + \frac{de-cf}{c+dx} \right) \left( h + \frac{dg-ch}{c+dx} \right)} \right) -$$

$$\left( 5 i a b^2 c C d^2 f^3 g h^2 \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \right. \\ \left. \text{EllipticF}\left[ i \text{ArcSinh}\left[ \frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) /$$

$$\left( \sqrt{-\frac{-de+cf}{f}} \sqrt{\left( f + \frac{de-cf}{c+dx} \right) \left( h + \frac{dg-ch}{c+dx} \right)} \right) +$$

$$\left( 4 i b^3 c C d^2 e^2 f h^3 \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \right. \\ \left. \text{EllipticF}\left[ i \text{ArcSinh}\left[ \frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) /$$

$$\left( \sqrt{-\frac{-de+cf}{f}} \sqrt{\left( f + \frac{de-cf}{c+dx} \right) \left( h + \frac{dg-ch}{c+dx} \right)} \right) +$$

$$\left( 3 i b^3 c^2 C d e f^2 h^3 \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \right. \\ \left. \text{EllipticF}\left[ i \text{ArcSinh}\left[ \frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) /$$

$$\left( \sqrt{-\frac{-de+cf}{f}} \sqrt{\left( f + \frac{de-cf}{c+dx} \right) \left( h + \frac{dg-ch}{c+dx} \right)} \right) -$$

$$\left( 5 i b^3 B c d^2 e f^2 h^3 \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \right. \\ \left. \text{EllipticF}\left[ i \text{ArcSinh}\left[ \frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) /$$

$$\left( \sqrt{-\frac{-de+cf}{f}} \sqrt{\left( f + \frac{de-cf}{c+dx} \right) \left( h + \frac{dg-ch}{c+dx} \right)} \right) -$$

$$\left( 5 i a b^2 c C d^2 e f^2 h^3 \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \right. \\ \left. \text{EllipticF}\left[ i \text{ArcSinh}\left[ \frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) /$$

$$\left( \sqrt{-\frac{-de+cf}{f}} \sqrt{\left( f + \frac{de-cf}{c+dx} \right) \left( h + \frac{dg-ch}{c+dx} \right)} \right) +$$

$$\left( 8 i b^3 c^3 C f^3 h^3 \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \right. \\ \left. \text{EllipticF}\left[ i \text{ArcSinh}\left[ \frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) /$$

$$\left( \sqrt{-\frac{-de+cf}{f}} \sqrt{\left( f + \frac{de-cf}{c+dx} \right) \left( h + \frac{dg-ch}{c+dx} \right)} \right) - \left( 10 i b^3 B c^2 d f^3 h^3 \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \right)$$

$$\left( \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \operatorname{EllipticF}\left[ i \operatorname{ArcSinh}\left[ \frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) /$$

$$\left( \sqrt{-\frac{-de+cf}{f}} \sqrt{\left( f + \frac{de-cf}{c+dx} \right) \left( h + \frac{dg-ch}{c+dx} \right)} \right) -$$

$$\left( 10 i a b^2 c^2 C d f^3 h^3 \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \right)$$

$$\operatorname{EllipticF}\left[ i \operatorname{ArcSinh}\left[ \frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] /$$

$$\left( \sqrt{-\frac{-de+cf}{f}} \sqrt{\left( f + \frac{de-cf}{c+dx} \right) \left( h + \frac{dg-ch}{c+dx} \right)} \right) +$$

$$\left( 30 i a b^2 B c d^2 f^3 h^3 \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \right)$$

$$\operatorname{EllipticF}\left[ i \operatorname{ArcSinh}\left[ \frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] /$$

$$\left( \sqrt{-\frac{-de+cf}{f}} \sqrt{\left( f + \frac{de-cf}{c+dx} \right) \left( h + \frac{dg-ch}{c+dx} \right)} \right) -$$

$$\left( 15 i a^2 b c C d^2 f^3 h^3 \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \right)$$

$$\left( \text{EllipticF} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) /$$

$$\left( \sqrt{-\frac{de+cf}{f}} \sqrt{\left( f + \frac{de-cf}{c+dx} \right) \left( h + \frac{dg-ch}{c+dx} \right)} \right) -$$

$$\left( 15 i a^2 b B d^3 f^3 h^3 \sqrt{1 - \frac{de+cf}{f(c+dx)}} \sqrt{1 - \frac{dg+ch}{h(c+dx)}} \right)$$

$$\left( \text{EllipticF} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) /$$

$$\left( \sqrt{-\frac{de+cf}{f}} \sqrt{\left( f + \frac{de-cf}{c+dx} \right) \left( h + \frac{dg-ch}{c+dx} \right)} \right) +$$

$$\left( 15 i a^3 C d^3 f^3 h^3 \sqrt{1 - \frac{de+cf}{f(c+dx)}} \sqrt{1 - \frac{dg+ch}{h(c+dx)}} \right)$$

$$\left( \text{EllipticF} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) /$$

$$\left( \sqrt{-\frac{de+cf}{f}} \sqrt{\left( f + \frac{de-cf}{c+dx} \right) \left( h + \frac{dg-ch}{c+dx} \right)} \right)$$

**Problem 17: Result unnecessarily involves imaginary or complex numbers.**

$$\int \frac{a b B - a^2 C + b^2 B x + b^2 C x^2}{\sqrt{c+dx} \sqrt{e+fx} \sqrt{g+hx}} dx$$

Optimal (type 4, 410 leaves, 7 steps):

$$\frac{2 b^2 C \sqrt{c+dx} \sqrt{e+fx} \sqrt{g+hx}}{3 d f h} +$$

$$\left( 2 b^2 \sqrt{-de+cf} (3 B d f h - 2 C (d f g + d e h + c f h)) \sqrt{\frac{d (e+fx)}{d e - c f}} \sqrt{g+hx} \right.$$

$$\left. \text{EllipticE}\left[\text{ArcSin}\left[\frac{\sqrt{f} \sqrt{c+dx}}{\sqrt{-de+cf}}\right], \frac{(de - cf) h}{f (dg - ch)}\right] \right) / \left( 3 d^2 f^{3/2} h^2 \sqrt{e+fx} \sqrt{\frac{d (g+hx)}{dg - ch}} \right) +$$

$$\left( 2 \sqrt{-de+cf} (3 a b B d f h^2 - 3 a^2 C d f h^2 - b^2 (3 B d f g h - C (ch (fg - eh) + dg (2fg + eh)))) \right.$$

$$\left. \sqrt{\frac{d (e+fx)}{d e - c f}} \sqrt{\frac{d (g+hx)}{d g - c h}} \text{EllipticF}\left[\text{ArcSin}\left[\frac{\sqrt{f} \sqrt{c+dx}}{\sqrt{-de+cf}}\right], \frac{(de - cf) h}{f (dg - ch)}\right] \right) /$$

$$(3 d^2 f^{3/2} h^2 \sqrt{e+fx} \sqrt{g+hx})$$

Result (type 4, 569 leaves):

$$\begin{aligned}
 & \frac{2b^2 C \sqrt{c+dx} \sqrt{e+fx} \sqrt{g+hx}}{3dfh} + \\
 & \frac{1}{3d^3 \sqrt{-c + \frac{de}{f}} f^2 h^2 \sqrt{e + \frac{(c+dx)(f - \frac{cf}{c+dx})}{d}} \sqrt{g + \frac{(c+dx)(h - \frac{ch}{c+dx})}{d}}} (c+dx)^{3/2} \left( -2b^2 \sqrt{-c + \frac{de}{f}} \right. \\
 & \quad \left. (-3Bdfh + 2C(df g + de h + cf h)) \left( f + \frac{de}{c+dx} - \frac{cf}{c+dx} \right) \left( h + \frac{dg}{c+dx} - \frac{ch}{c+dx} \right) - \frac{1}{\sqrt{c+dx}} \right. \\
 & \quad \left. 2ib^2(-de + cf)h(3Bdfh - 2C(df g + de h + cf h)) \sqrt{1 - \frac{c}{c+dx} + \frac{de}{f(c+dx)}} \right. \\
 & \quad \left. \sqrt{1 - \frac{c}{c+dx} + \frac{dg}{h(c+dx)}} \operatorname{EllipticE} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{-c + \frac{de}{f}}}{\sqrt{c+dx}} \right], \frac{dfg - cfh}{deh - cfh} \right] + \frac{1}{\sqrt{c+dx}} \right. \\
 & \quad \left. 2idh(3abBdf^2h - 3a^2Cdf^2h + b^2(-3Bdefh + cCf(-fg + eh) + Cde(fg + 2eh))) \right. \\
 & \quad \left. \sqrt{1 - \frac{c}{c+dx} + \frac{de}{f(c+dx)}} \sqrt{1 - \frac{c}{c+dx} + \frac{dg}{h(c+dx)}} \right. \\
 & \quad \left. \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{-c + \frac{de}{f}}}{\sqrt{c+dx}} \right], \frac{dfg - cfh}{deh - cfh} \right] \right)
 \end{aligned}$$

**Problem 18: Result unnecessarily involves imaginary or complex numbers.**

$$\int \frac{aBx - a^2C + b^2Bx + b^2Cx^2}{(a+bx)\sqrt{c+dx}\sqrt{e+fx}\sqrt{g+hx}} dx$$

Optimal (type 4, 291 leaves, 7 steps):

$$\left( 2 b C \sqrt{-d e+c f} \sqrt{\frac{d(e+f x)}{d e-c f}} \sqrt{g+h x} \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{f} \sqrt{c+d x}}{\sqrt{-d e+c f}}\right], \frac{(d e-c f) h}{f(d g-c h)}\right] \right) /$$

$$\left( d \sqrt{f} h \sqrt{e+f x} \sqrt{\frac{d(g+h x)}{d g-c h}} \right) -$$

$$\left( 2 \sqrt{-d e+c f} (b C g-b B h+a C h) \sqrt{\frac{d(e+f x)}{d e-c f}} \sqrt{\frac{d(g+h x)}{d g-c h}} \right.$$

$$\left. \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{f} \sqrt{c+d x}}{\sqrt{-d e+c f}}\right], \frac{(d e-c f) h}{f(d g-c h)}\right] \right) / \left( d \sqrt{f} h \sqrt{e+f x} \sqrt{g+h x} \right)$$

Result (type 4, 326 leaves):

$$\left( 2 \left( b C d^2 \sqrt{-c+\frac{d e}{f}} (e+f x)(g+h x) + i b C (d e-c f) h (c+d x)^{3/2} \sqrt{\frac{d(e+f x)}{f(c+d x)}} \sqrt{\frac{d(g+h x)}{h(c+d x)}} \right. \right.$$

$$\left. \operatorname{EllipticE}\left[ i \operatorname{ArcSinh}\left[\frac{\sqrt{-c+\frac{d e}{f}}}{\sqrt{c+d x}}\right], \frac{d f g-c f h}{d e h-c f h}\right] - i d (b C e-b B f+a C f) h (c+d x)^{3/2} \right.$$

$$\left. \left. \sqrt{\frac{d(e+f x)}{f(c+d x)}} \sqrt{\frac{d(g+h x)}{h(c+d x)}} \operatorname{EllipticF}\left[ i \operatorname{ArcSinh}\left[\frac{\sqrt{-c+\frac{d e}{f}}}{\sqrt{c+d x}}\right], \frac{d f g-c f h}{d e h-c f h}\right] \right) \right) /$$

$$\left( d^2 \sqrt{-c+\frac{d e}{f}} f h \sqrt{c+d x} \sqrt{e+f x} \sqrt{g+h x} \right)$$

**Problem 19: Result unnecessarily involves imaginary or complex numbers.**

$$\int \frac{a b B - a^2 C + b^2 B x + b^2 C x^2}{(a + b x)^2 \sqrt{c + d x} \sqrt{e + f x} \sqrt{g + h x}} dx$$

Optimal (type 4, 309 leaves, 10 steps):

$$\left( 2C \sqrt{-de+cf} \sqrt{\frac{d(e+fx)}{de-cf}} \sqrt{\frac{d(g+hx)}{dg-ch}} \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{f}\sqrt{c+dx}}{\sqrt{-de+cf}}\right], \frac{(de-cf)h}{f(dg-ch)}\right] \right) /$$

$$\left( d \sqrt{f} \sqrt{e+fx} \sqrt{g+hx} \right) -$$

$$\left( 2(bB-2aC) \sqrt{-de+cf} \sqrt{\frac{d(e+fx)}{de-cf}} \sqrt{\frac{d(g+hx)}{dg-ch}} \operatorname{EllipticPi}\left[-\frac{b(de-cf)}{(bc-ad)f}, \right.$$

$$\left. \operatorname{ArcSin}\left[\frac{\sqrt{f}\sqrt{c+dx}}{\sqrt{-de+cf}}\right], \frac{(de-cf)h}{f(dg-ch)}\right] \right) / \left( (bc-ad) \sqrt{f} \sqrt{e+fx} \sqrt{g+hx} \right)$$

Result (type 4, 248 leaves):

$$\left( 2i \sqrt{e+fx} \sqrt{\frac{d(g+hx)}{h(c+dx)}} \right.$$

$$\left( - (bcC - bBd + aCd) \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{-c + \frac{de}{f}}}{\sqrt{c+dx}}\right], \frac{dfg - cfh}{deh - cfh}\right] + \right.$$

$$\left. \left. (-bB + 2aC) d \operatorname{EllipticPi}\left[\frac{(bc-ad)f}{b(-de+cf)}, i \operatorname{ArcSinh}\left[\frac{\sqrt{-c + \frac{de}{f}}}{\sqrt{c+dx}}\right], \frac{dfg - cfh}{deh - cfh}\right] \right) \right) /$$

$$\left( (-bc + ad) \sqrt{-c + \frac{de}{f}} f \sqrt{\frac{d(e+fx)}{f(c+dx)}} \sqrt{g+hx} \right)$$

**Problem 20: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{abB - a^2C + b^2Bx + b^2Cx^2}{(a+bx)^3 \sqrt{c+dx} \sqrt{e+fx} \sqrt{g+hx}} dx$$

Optimal (type 4, 680 leaves, 13 steps):

$$\begin{aligned}
 & - \frac{b^2 (bB - 2aC) \sqrt{c+dx} \sqrt{e+fx} \sqrt{g+hx}}{(bc-ad)(be-af)(bg-ah)(a+bx)} + \left( b (bB - 2aC) \sqrt{f} \sqrt{-de+cf} \right. \\
 & \left. \sqrt{\frac{d(e+fx)}{de-cf}} \sqrt{g+hx} \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{f} \sqrt{c+dx}}{\sqrt{-de+cf}}\right], \frac{(de-cf)h}{f(dg-ch)}\right] \right) / \\
 & \left( (bc-ad)(be-af)(bg-ah) \sqrt{e+fx} \sqrt{\frac{d(g+hx)}{dg-ch}} \right) - \\
 & \left( (bB - 2aC) \sqrt{f} \sqrt{-de+cf} \sqrt{\frac{d(e+fx)}{de-cf}} \sqrt{\frac{d(g+hx)}{dg-ch}} \operatorname{EllipticF}\left[ \right. \right. \\
 & \left. \left. \operatorname{ArcSin}\left[\frac{\sqrt{f} \sqrt{c+dx}}{\sqrt{-de+cf}}\right], \frac{(de-cf)h}{f(dg-ch)}\right] \right) / \left( (bc-ad)(be-af) \sqrt{e+fx} \sqrt{g+hx} \right) - \\
 & \left( \sqrt{-de+cf} (4a^3 Cdfh + 2ab^2 B(dfg+deh+cfh) - b^3 (Bdeg - c(2Ceg - Bfg - Beh))) - \right. \\
 & \left. a^2 b (3Bdfh + 2C(dfg+deh+cfh)) \right) \sqrt{\frac{d(e+fx)}{de-cf}} \sqrt{\frac{d(g+hx)}{dg-ch}} \\
 & \left. \operatorname{EllipticPi}\left[-\frac{b(de-cf)}{(bc-ad)f}, \operatorname{ArcSin}\left[\frac{\sqrt{f} \sqrt{c+dx}}{\sqrt{-de+cf}}\right], \frac{(de-cf)h}{f(dg-ch)}\right] \right) / \\
 & \left( (bc-ad)^2 \sqrt{f} (be-af)(bg-ah) \sqrt{e+fx} \sqrt{g+hx} \right)
 \end{aligned}$$

Result (type 4, 16821 leaves):

$$\begin{aligned}
 & - \frac{b^2 (bB - 2aC) \sqrt{c+dx} \sqrt{e+fx} \sqrt{g+hx}}{(bc-ad)(be-af)(bg-ah)(a+bx)} - \frac{1}{d(-bc+ad)(-be+af)(-bg+ah)} \\
 & \left( \frac{b (bB - 2aC) (c+dx)^{3/2} \left( f + \frac{de}{c+dx} - \frac{cf}{c+dx} \right) \left( h + \frac{dg}{c+dx} - \frac{ch}{c+dx} \right)}{\sqrt{e + \frac{(c+dx)(f - \frac{cf}{c+dx})}{d}} \sqrt{g + \frac{(c+dx)(h - \frac{ch}{c+dx})}{d}}} \right) + \\
 & \left( (c+dx) \left( -b + \frac{bc}{c+dx} - \frac{ad}{c+dx} \right) \sqrt{f + \frac{de}{c+dx} - \frac{cf}{c+dx}} \sqrt{h + \frac{dg}{c+dx} - \frac{ch}{c+dx}} \right)
 \end{aligned}$$

$$\begin{aligned}
 & \sqrt{\left( fh + \frac{d^2 eg}{(c+dx)^2} - \frac{cdfg}{(c+dx)^2} - \frac{cdeh}{(c+dx)^2} + \frac{c^2 fh}{(c+dx)^2} + \frac{dfg}{c+dx} + \frac{deh}{c+dx} - \frac{2cfh}{c+dx} \right)} \\
 & \left( (bc-ad)h(-2b^2Ceg + b^2Bfg + b^2Beh - 2abBfh + 2a^2Cfh) \right) / \\
 & \left( (-bg+ah) \sqrt{f + \frac{de}{c+dx} - \frac{cf}{c+dx}} \sqrt{h + \frac{dg}{c+dx} - \frac{ch}{c+dx}} \right) - \\
 & \frac{b(bB-2aC)(de-cf) \sqrt{h + \frac{dg}{c+dx} - \frac{ch}{c+dx}}}{\sqrt{f + \frac{de}{c+dx} - \frac{cf}{c+dx}}} + \\
 & \left( b(2b^3cCeg - b^3Bdeg - b^3Bcfg + 2ab^2Bdfg - 2a^2bCdffg - b^3Bceh + \right. \\
 & \quad \left. 2ab^2Bdeh - 2a^2bcdeh + 2ab^2Bcfh - 2a^2bcCfh - 3a^2bBdfh + 4a^3Cdfh) \right. \\
 & \quad \left. \sqrt{h + \frac{dg}{c+dx} - \frac{ch}{c+dx}} \right) / \left( (-bg+ah) \left( b - \frac{bc}{c+dx} + \frac{ad}{c+dx} \right) \sqrt{f + \frac{de}{c+dx} - \frac{cf}{c+dx}} \right) \\
 & \left( \left( i b^2 B d^2 e f g \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \left( \text{EllipticE} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{-dg+ch}{h}}}{\sqrt{c+dx}} \right] \right), \right. \right. \right. \\
 & \quad \left. \left. \frac{(-de+cf)h}{f(-dg+ch)} \right] - \text{EllipticF} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{-dg+ch}{h}}}{\sqrt{c+dx}} \right], \frac{(-de+cf)h}{f(-dg+ch)} \right] \right) \right) / \\
 & \left( (bc-ad)(-de+cf) \sqrt{-\frac{-dg+ch}{h}} \sqrt{\left( fh + \frac{d^2 eg - cdfg - cdeh + c^2 fh}{(c+dx)^2} + \right. \right. \\
 & \quad \left. \left. \frac{dfg + deh - 2cfh}{c+dx} \right) \right) - \left( 2 i a b C d^2 e f g \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \right)
 \end{aligned}$$

$$\begin{aligned}
 & \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \left( \text{EllipticE} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{-dg+ch}{h}}}{\sqrt{c+dx}} \right], \frac{(-de+cf)h}{f(-dg+ch)} \right] - \right. \\
 & \left. \text{EllipticF} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{-dg+ch}{h}}}{\sqrt{c+dx}} \right], \frac{(-de+cf)h}{f(-dg+ch)} \right] \right) / \left( (bc-ad)(-de+cf) \right) \\
 & \sqrt{-\frac{-dg+ch}{h}} \sqrt{\left( fh + \frac{d^2eg - cdfg - cdeh + c^2fh}{(c+dx)^2} + \frac{dfg+deh-2cfh}{c+dx} \right)} - \\
 & \left( i b^2 B c d f^2 g \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \left( \text{EllipticE} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{-dg+ch}{h}}}{\sqrt{c+dx}} \right], \right. \right. \right. \\
 & \left. \left. \frac{(-de+cf)h}{f(-dg+ch)} \right] - \text{EllipticF} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{-dg+ch}{h}}}{\sqrt{c+dx}} \right], \frac{(-de+cf)h}{f(-dg+ch)} \right] \right) / \\
 & \left( (bc-ad)(-de+cf) \sqrt{-\frac{-dg+ch}{h}} \sqrt{\left( fh + \frac{d^2eg - cdfg - cdeh + c^2fh}{(c+dx)^2} + \right. \right. \\
 & \left. \left. \frac{dfg+deh-2cfh}{c+dx} \right)} \right) + \left( 2 i a b c C d f^2 g \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \right. \\
 & \left. \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \left( \text{EllipticE} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{-dg+ch}{h}}}{\sqrt{c+dx}} \right], \frac{(-de+cf)h}{f(-dg+ch)} \right] - \right. \right. \\
 & \left. \left. \text{EllipticF} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{-dg+ch}{h}}}{\sqrt{c+dx}} \right], \frac{(-de+cf)h}{f(-dg+ch)} \right] \right) \right) / \left( (bc-ad)(-de+cf) \right)
 \end{aligned}$$

$$\begin{aligned}
 & \sqrt{-\frac{-dg+ch}{h}} \sqrt{\left( fh + \frac{d^2eg - cdfg - cdeh + c^2fh}{(c+dx)^2} + \frac{dfg+deh-2cfh}{c+dx} \right)} - \\
 & \left( \frac{b^2 B c d e f h}{\sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \left( \text{EllipticE} \left[ \frac{\sqrt{-\frac{-dg+ch}{h}}}{\sqrt{c+dx}} \right], \right. \right. \\
 & \left. \left. \frac{(-de+cf)h}{f(-dg+ch)} \right) - \text{EllipticF} \left[ \frac{\sqrt{-\frac{-dg+ch}{h}}}{\sqrt{c+dx}}, \frac{(-de+cf)h}{f(-dg+ch)} \right] \right) / \\
 & \left( (bc-ad)(-de+cf) \sqrt{-\frac{-dg+ch}{h}} \sqrt{\left( fh + \frac{d^2eg - cdfg - cdeh + c^2fh}{(c+dx)^2} + \right. \right. \\
 & \left. \left. \frac{dfg+deh-2cfh}{c+dx} \right) \right) + \left( 2 \frac{b^2 B c d e f h}{\sqrt{1 - \frac{-de+cf}{f(c+dx)}}} \right. \\
 & \left. \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \left( \text{EllipticE} \left[ \frac{\sqrt{-\frac{-dg+ch}{h}}}{\sqrt{c+dx}}, \frac{(-de+cf)h}{f(-dg+ch)} \right] - \right. \right. \\
 & \left. \left. \text{EllipticF} \left[ \frac{\sqrt{-\frac{-dg+ch}{h}}}{\sqrt{c+dx}}, \frac{(-de+cf)h}{f(-dg+ch)} \right] \right) \right) / \left( (bc-ad)(-de+cf) \right. \\
 & \left. \sqrt{-\frac{-dg+ch}{h}} \sqrt{\left( fh + \frac{d^2eg - cdfg - cdeh + c^2fh}{(c+dx)^2} + \frac{dfg+deh-2cfh}{c+dx} \right) \right) + \\
 & \left( \frac{b^2 B c^2 f^2 h}{\sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \left( \text{EllipticE} \left[ \frac{\sqrt{-\frac{-dg+ch}{h}}}{\sqrt{c+dx}} \right], \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left. \left. \left. \frac{(-de+cf)h}{f(-dg+ch)} \right] - \text{EllipticF} \left[ \text{i ArcSinh} \left[ \frac{\sqrt{-\frac{dg+ch}{h}}}{\sqrt{c+dx}} \right], \frac{(-de+cf)h}{f(-dg+ch)} \right] \right) \right) / \\
 & \left( (bc-ad)(-de+cf) \sqrt{-\frac{dg+ch}{h}} \sqrt{\left( fh + \frac{d^2eg - cd fg - cdeh + c^2fh}{(c+dx)^2} + \right. \right. \\
 & \left. \left. \frac{dfg+deh-2cfh}{c+dx} \right) \right) - \left( 2 \text{i} abc^2 C f^2 h \sqrt{1 - \frac{de+cf}{f(c+dx)}} \right. \\
 & \left. \sqrt{1 - \frac{dg+ch}{h(c+dx)}} \left( \text{EllipticE} \left[ \text{i ArcSinh} \left[ \frac{\sqrt{-\frac{dg+ch}{h}}}{\sqrt{c+dx}} \right], \frac{(-de+cf)h}{f(-dg+ch)} \right] - \right. \right. \\
 & \left. \left. \text{EllipticF} \left[ \text{i ArcSinh} \left[ \frac{\sqrt{-\frac{dg+ch}{h}}}{\sqrt{c+dx}} \right], \frac{(-de+cf)h}{f(-dg+ch)} \right] \right) \right) / \left( (bc-ad)(-de+cf) \right. \\
 & \left. \sqrt{-\frac{dg+ch}{h}} \sqrt{\left( fh + \frac{d^2eg - cd fg - cdeh + c^2fh}{(c+dx)^2} + \frac{dfg+deh-2cfh}{c+dx} \right) \right) - \\
 & \left( \text{i} b^3 B d^2 eg \sqrt{1 - \frac{de+cf}{f(c+dx)}} \sqrt{1 - \frac{dg+ch}{h(c+dx)}} \text{EllipticF} \left[ \right. \right. \\
 & \left. \left. \text{i ArcSinh} \left[ \frac{\sqrt{-\frac{dg+ch}{h}}}{\sqrt{c+dx}} \right], \frac{(-de+cf)h}{f(-dg+ch)} \right] \right) / \left( (bc-ad)^2 \sqrt{-\frac{dg+ch}{h}} \right. \\
 & \left. \sqrt{\left( fh + \frac{d^2eg - cd fg - cdeh + c^2fh}{(c+dx)^2} + \frac{dfg+deh-2cfh}{c+dx} \right) \right) +
 \end{aligned}$$

$$\left( 2 i a b^2 C d^2 e g \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \text{EllipticF}\left[ \right. \right. \\ \left. \left. i \text{ArcSinh}\left[ \frac{\sqrt{\frac{-dg+ch}{h}}}{\sqrt{c+dx}} \right], \frac{(-de+cf)h}{f(-dg+ch)} \right] \right) / \left( (bc-ad)^2 \sqrt{\frac{-dg+ch}{h}} \right) \\ \sqrt{\left( fh + \frac{d^2 eg - cd fg - cde h + c^2 fh}{(c+dx)^2} + \frac{dfg + de h - 2cfh}{c+dx} \right)} +$$

$$\left( 2 i b^2 C d e g \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \text{EllipticF}\left[ \right. \right. \\ \left. \left. i \text{ArcSinh}\left[ \frac{\sqrt{\frac{-dg+ch}{h}}}{\sqrt{c+dx}} \right], \frac{(-de+cf)h}{f(-dg+ch)} \right] \right) / \left( (bc-ad) \sqrt{\frac{-dg+ch}{h}} \right) \\ \sqrt{\left( fh + \frac{d^2 eg - cd fg - cde h + c^2 fh}{(c+dx)^2} + \frac{dfg + de h - 2cfh}{c+dx} \right)} +$$

$$\left( i b^3 B c d f g \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \text{EllipticF}\left[ \right. \right. \\ \left. \left. i \text{ArcSinh}\left[ \frac{\sqrt{\frac{-dg+ch}{h}}}{\sqrt{c+dx}} \right], \frac{(-de+cf)h}{f(-dg+ch)} \right] \right) / \left( (bc-ad)^2 \sqrt{\frac{-dg+ch}{h}} \right) \\ \sqrt{\left( fh + \frac{d^2 eg - cd fg - cde h + c^2 fh}{(c+dx)^2} + \frac{dfg + de h - 2cfh}{c+dx} \right)} -$$

$$\begin{aligned}
 & \left( 2 i a b^2 c C d f g \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \operatorname{EllipticF} \left[ \right. \right. \\
 & \quad \left. \left. i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{-dg+ch}{h}}}{\sqrt{c+dx}} \right], \frac{(-de+cf)h}{f(-dg+ch)} \right] \right) / \left( (bc-ad)^2 \sqrt{\frac{-dg+ch}{h}} \right. \\
 & \quad \left. \sqrt{\left( fh + \frac{d^2 eg - cdfg - cdeh + c^2 fh}{(c+dx)^2} + \frac{dfg + deh - 2cfh}{c+dx} \right)} \right) - \\
 & \left( 2 i b^2 B d f g \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \operatorname{EllipticF} \left[ \right. \right. \\
 & \quad \left. \left. i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{-dg+ch}{h}}}{\sqrt{c+dx}} \right], \frac{(-de+cf)h}{f(-dg+ch)} \right] \right) / \left( (bc-ad) \sqrt{\frac{-dg+ch}{h}} \right. \\
 & \quad \left. \sqrt{\left( fh + \frac{d^2 eg - cdfg - cdeh + c^2 fh}{(c+dx)^2} + \frac{dfg + deh - 2cfh}{c+dx} \right)} \right) + \\
 & \left( 2 i a b C d f g \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \operatorname{EllipticF} \left[ \right. \right. \\
 & \quad \left. \left. i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{-dg+ch}{h}}}{\sqrt{c+dx}} \right], \frac{(-de+cf)h}{f(-dg+ch)} \right] \right) / \left( (bc-ad) \sqrt{\frac{-dg+ch}{h}} \right. \\
 & \quad \left. \sqrt{\left( fh + \frac{d^2 eg - cdfg - cdeh + c^2 fh}{(c+dx)^2} + \frac{dfg + deh - 2cfh}{c+dx} \right)} \right) +
 \end{aligned}$$

$$\begin{aligned}
 & \left( i b^3 B c d e h \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \operatorname{EllipticF} \left[ \right. \right. \\
 & \quad \left. \left. i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{-dg+ch}{h}}}{\sqrt{c+dx}}, \frac{(-de+cf)h}{f(-dg+ch)} \right] \right] / \left( (bc-ad)^2 \sqrt{\frac{-dg+ch}{h}} \right. \right. \\
 & \quad \left. \left. \sqrt{\left( fh + \frac{d^2 eg - cd fg - cdeh + c^2 fh}{(c+dx)^2} + \frac{dfg+deh-2cfh}{c+dx} \right)} \right) \right) - \\
 & \left( 2 i a b^2 c C d e h \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \operatorname{EllipticF} \left[ \right. \right. \\
 & \quad \left. \left. i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{-dg+ch}{h}}}{\sqrt{c+dx}}, \frac{(-de+cf)h}{f(-dg+ch)} \right] \right] / \left( (bc-ad)^2 \sqrt{\frac{-dg+ch}{h}} \right. \right. \\
 & \quad \left. \left. \sqrt{\left( fh + \frac{d^2 eg - cd fg - cdeh + c^2 fh}{(c+dx)^2} + \frac{dfg+deh-2cfh}{c+dx} \right)} \right) \right) - \\
 & \left( 2 i b^2 B d e h \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \operatorname{EllipticF} \left[ \right. \right. \\
 & \quad \left. \left. i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{-dg+ch}{h}}}{\sqrt{c+dx}}, \frac{(-de+cf)h}{f(-dg+ch)} \right] \right] / \left( (bc-ad) \sqrt{\frac{-dg+ch}{h}} \right. \right. \\
 & \quad \left. \left. \sqrt{\left( fh + \frac{d^2 eg - cd fg - cdeh + c^2 fh}{(c+dx)^2} + \frac{dfg+deh-2cfh}{c+dx} \right)} \right) \right) +
 \end{aligned}$$

$$\begin{aligned}
 & \left( 2 i a b c d e h \sqrt{1 - \frac{-d e + c f}{f (c + d x)}} \sqrt{1 - \frac{-d g + c h}{h (c + d x)}} \operatorname{EllipticF} \left[ \right. \right. \\
 & \quad \left. \left. i \operatorname{ArcSinh} \left[ \frac{\sqrt{-\frac{d g + c h}{h}}}{\sqrt{c + d x}} \right], \frac{(-d e + c f) h}{f (-d g + c h)} \right] \right) / \left( (b c - a d) \sqrt{-\frac{d g + c h}{h}} \right. \\
 & \quad \left. \sqrt{\left( f h + \frac{d^2 e g - c d f g - c d e h + c^2 f h}{(c + d x)^2} + \frac{d f g + d e h - 2 c f h}{c + d x} \right)} \right) - \\
 & \left( i b^3 B c^2 f h \sqrt{1 - \frac{-d e + c f}{f (c + d x)}} \sqrt{1 - \frac{-d g + c h}{h (c + d x)}} \operatorname{EllipticF} \left[ \right. \right. \\
 & \quad \left. \left. i \operatorname{ArcSinh} \left[ \frac{\sqrt{-\frac{d g + c h}{h}}}{\sqrt{c + d x}} \right], \frac{(-d e + c f) h}{f (-d g + c h)} \right] \right) / \left( (b c - a d)^2 \sqrt{-\frac{d g + c h}{h}} \right. \\
 & \quad \left. \sqrt{\left( f h + \frac{d^2 e g - c d f g - c d e h + c^2 f h}{(c + d x)^2} + \frac{d f g + d e h - 2 c f h}{c + d x} \right)} \right) + \\
 & \left( 2 i a b^2 c^2 C f h \sqrt{1 - \frac{-d e + c f}{f (c + d x)}} \sqrt{1 - \frac{-d g + c h}{h (c + d x)}} \operatorname{EllipticF} \left[ \right. \right. \\
 & \quad \left. \left. i \operatorname{ArcSinh} \left[ \frac{\sqrt{-\frac{d g + c h}{h}}}{\sqrt{c + d x}} \right], \frac{(-d e + c f) h}{f (-d g + c h)} \right] \right) / \left( (b c - a d)^2 \sqrt{-\frac{d g + c h}{h}} \right. \\
 & \quad \left. \sqrt{\left( f h + \frac{d^2 e g - c d f g - c d e h + c^2 f h}{(c + d x)^2} + \frac{d f g + d e h - 2 c f h}{c + d x} \right)} \right) +
 \end{aligned}$$

$$\begin{aligned}
 & \left( 2 i b^2 B c f h \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \operatorname{EllipticF} \left[ \right. \right. \\
 & \quad \left. \left. i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{-dg+ch}{h}}}{\sqrt{c+dx}} \right], \frac{(-de+cf)h}{f(-dg+ch)} \right] \right) / \left( (bc-ad) \sqrt{-\frac{-dg+ch}{h}} \right) \\
 & \quad \sqrt{\left( fh + \frac{d^2 eg - cdfg - cdeh + c^2 fh}{(c+dx)^2} + \frac{dfg + deh - 2cfh}{c+dx} \right)} - \\
 & \left( 4 i a b c C f h \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \operatorname{EllipticF} \left[ \right. \right. \\
 & \quad \left. \left. i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{-dg+ch}{h}}}{\sqrt{c+dx}} \right], \frac{(-de+cf)h}{f(-dg+ch)} \right] \right) / \left( (bc-ad) \sqrt{-\frac{-dg+ch}{h}} \right) \\
 & \quad \sqrt{\left( fh + \frac{d^2 eg - cdfg - cdeh + c^2 fh}{(c+dx)^2} + \frac{dfg + deh - 2cfh}{c+dx} \right)} + \\
 & \left( 2 i a b B d f h \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \operatorname{EllipticF} \left[ \right. \right. \\
 & \quad \left. \left. i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{-dg+ch}{h}}}{\sqrt{c+dx}} \right], \frac{(-de+cf)h}{f(-dg+ch)} \right] \right) / \left( (bc-ad) \sqrt{-\frac{-dg+ch}{h}} \right) \\
 & \quad \sqrt{\left( fh + \frac{d^2 eg - cdfg - cdeh + c^2 fh}{(c+dx)^2} + \frac{dfg + deh - 2cfh}{c+dx} \right)} -
 \end{aligned}$$

$$\begin{aligned}
 & \left( 2 i a^2 C d f h \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \operatorname{EllipticF} \left[ \right. \right. \\
 & \quad \left. \left. i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{-dg+ch}{h}}}{\sqrt{c+dx}}, \frac{(-de+cf)h}{f(-dg+ch)} \right] \right] / \left( (bc-ad) \sqrt{\frac{-dg+ch}{h}} \right. \right. \\
 & \quad \left. \left. \sqrt{\left( fh + \frac{d^2 eg - cdfg - cdeh + c^2 fh}{(c+dx)^2} + \frac{dfg + deh - 2cfh}{c+dx} \right)} \right) + \frac{1}{(bc-ad)^3} \right. \\
 & b^4 B d^2 e g \left( \left( i c \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \operatorname{EllipticPi} \left[ \frac{(bc-ad)h}{b(-dg+ch)}, \right. \right. \right. \\
 & \quad \left. \left. i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{-dg+ch}{h}}}{\sqrt{c+dx}}, \frac{(-de+cf)h}{f(-dg+ch)} \right] \right] / \left( \sqrt{\frac{-dg+ch}{h}} \sqrt{\left( fh + \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{d^2 eg}{(c+dx)^2} - \frac{cdfg}{(c+dx)^2} - \frac{cdeh}{(c+dx)^2} + \frac{c^2 fh}{(c+dx)^2} + \frac{dfg}{c+dx} + \frac{deh}{c+dx} - \frac{2cfh}{c+dx} \right)} \right) - \right. \\
 & \left. \left( i a d \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \operatorname{EllipticPi} \left[ \frac{(bc-ad)h}{b(-dg+ch)}, i \operatorname{ArcSinh} \left[ \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{\sqrt{\frac{-dg+ch}{h}}}{\sqrt{c+dx}}, \frac{(-de+cf)h}{f(-dg+ch)} \right] \right] / \left( b \sqrt{\frac{-dg+ch}{h}} \sqrt{\left( fh + \frac{d^2 eg}{(c+dx)^2} - \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{cdfg}{(c+dx)^2} - \frac{cdeh}{(c+dx)^2} + \frac{c^2 fh}{(c+dx)^2} + \frac{dfg}{c+dx} + \frac{deh}{c+dx} - \frac{2cfh}{c+dx} \right)} \right) - \frac{1}{(bc-ad)^3} \right)
 \end{aligned}$$

$$\begin{aligned}
 & 2ab^3Cd^2eg \left( \left( \int \left( \int c \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \operatorname{EllipticPi} \left[ \frac{(bc-ad)h}{b(-dg+ch)}, \right. \right. \right. \\
 & \quad \left. \left. \left. \int \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{-dg+ch}{h}}}{\sqrt{c+dx}} \right], \frac{(-de+cf)h}{f(-dg+ch)} \right] \right) / \left( \sqrt{\frac{-dg+ch}{h}} \sqrt{\left( fh + \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{d^2eg}{(c+dx)^2} - \frac{cdfg}{(c+dx)^2} - \frac{cdeh}{(c+dx)^2} + \frac{c^2fh}{(c+dx)^2} + \frac{dfg}{c+dx} + \frac{deh}{c+dx} - \frac{2cfh}{c+dx} \right) \right) - \right. \\
 & \left. \left( \int \left( \int ad \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \operatorname{EllipticPi} \left[ \frac{(bc-ad)h}{b(-dg+ch)}, \int \operatorname{ArcSinh} \left[ \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{\sqrt{\frac{-dg+ch}{h}}}{\sqrt{c+dx}} \right], \frac{(-de+cf)h}{f(-dg+ch)} \right] \right) / \left( b \sqrt{\frac{-dg+ch}{h}} \sqrt{\left( fh + \frac{d^2eg}{(c+dx)^2} - \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{cdfg}{(c+dx)^2} - \frac{cdeh}{(c+dx)^2} + \frac{c^2fh}{(c+dx)^2} + \frac{dfg}{c+dx} + \frac{deh}{c+dx} - \frac{2cfh}{c+dx} \right) \right) \right) - \frac{1}{(bc-ad)^2} \\
 & 2b^3Cdeg \left( \left( \int \left( \int c \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \operatorname{EllipticPi} \left[ \frac{(bc-ad)h}{b(-dg+ch)}, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \int \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{-dg+ch}{h}}}{\sqrt{c+dx}} \right], \frac{(-de+cf)h}{f(-dg+ch)} \right] \right) / \left( \sqrt{\frac{-dg+ch}{h}} \sqrt{\left( fh + \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{d^2eg}{(c+dx)^2} - \frac{cdfg}{(c+dx)^2} - \frac{cdeh}{(c+dx)^2} + \frac{c^2fh}{(c+dx)^2} + \frac{dfg}{c+dx} + \frac{deh}{c+dx} - \frac{2cfh}{c+dx} \right) \right) - \right.
 \end{aligned}$$



$$\left. \left( \frac{c^2 f h}{(c+dx)^2} + \frac{d f g}{c+dx} + \frac{d e h}{c+dx} - \frac{2 c f h}{c+dx} \right) \right) + \frac{1}{(bc-ad)^3}$$

$$2 a b^3 c c d f g \left( \left( i c \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \operatorname{EllipticPi} \left[ \frac{(bc-ad)h}{b(-dg+ch)}, \right. \right. \right.$$

$$\left. \left. \left. i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{-dg+ch}{h}}}{\sqrt{c+dx}} \right], \frac{(-de+cf)h}{f(-dg+ch)} \right] \right) / \left( \sqrt{\frac{-dg+ch}{h}} \sqrt{fh +} \right. \right.$$

$$\left. \left. \frac{d^2 e g}{(c+dx)^2} - \frac{c d f g}{(c+dx)^2} - \frac{c d e h}{(c+dx)^2} + \frac{c^2 f h}{(c+dx)^2} + \frac{d f g}{c+dx} + \frac{d e h}{c+dx} - \frac{2 c f h}{c+dx} \right) \right) -$$

$$\left( i a d \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \operatorname{EllipticPi} \left[ \frac{(bc-ad)h}{b(-dg+ch)}, \right. \right.$$

$$\left. \left. \left. i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{-dg+ch}{h}}}{\sqrt{c+dx}} \right], \frac{(-de+cf)h}{f(-dg+ch)} \right] \right) / \left( b \sqrt{\frac{-dg+ch}{h}} \sqrt{fh +} \right. \right.$$

$$\left. \left. \frac{d^2 e g}{(c+dx)^2} - \frac{c d f g}{(c+dx)^2} - \frac{c d e h}{(c+dx)^2} + \frac{c^2 f h}{(c+dx)^2} + \frac{d f g}{c+dx} + \frac{d e h}{c+dx} - \frac{2 c f h}{c+dx} \right) \right) +$$

$$\frac{1}{(bc-ad)^2} 2 b^3 B d f g \left( \left( i c \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \operatorname{EllipticPi} \left[ \right. \right. \right.$$

$$\left. \left. \left. \frac{(bc-ad)h}{b(-dg+ch)}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{-dg+ch}{h}}}{\sqrt{c+dx}} \right], \frac{(-de+cf)h}{f(-dg+ch)} \right] \right) / \right.$$

$$\begin{aligned}
 & \left( \sqrt{-\frac{dg+ch}{h}} \sqrt{\left( fh + \frac{d^2 eg}{(c+dx)^2} - \frac{cdfg}{(c+dx)^2} - \frac{cdeh}{(c+dx)^2} + \frac{c^2 fh}{(c+dx)^2} + \right.} \right. \\
 & \quad \left. \frac{dfg}{c+dx} + \frac{deh}{c+dx} - \frac{2cfh}{c+dx} \right) - \left( i ad \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \right. \\
 & \quad \left. \text{EllipticPi} \left[ \frac{(bc-ad)h}{b(-dg+ch)}, i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{dg+ch}{h}}}{\sqrt{c+dx}} \right], \frac{(-de+cf)h}{f(-dg+ch)} \right] \right) / \\
 & \left( b \sqrt{-\frac{dg+ch}{h}} \sqrt{\left( fh + \frac{d^2 eg}{(c+dx)^2} - \frac{cdfg}{(c+dx)^2} - \frac{cdeh}{(c+dx)^2} + \right.} \right. \\
 & \quad \left. \frac{c^2 fh}{(c+dx)^2} + \frac{dfg}{c+dx} + \frac{deh}{c+dx} - \frac{2cfh}{c+dx} \right) \left. \right) - \frac{1}{(bc-ad)^2} \\
 & 2ab^2cdfg \left( \left( i c \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \text{EllipticPi} \left[ \frac{(bc-ad)h}{b(-dg+ch)}, \right. \right. \right. \\
 & \quad \left. \left. i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{dg+ch}{h}}}{\sqrt{c+dx}} \right], \frac{(-de+cf)h}{f(-dg+ch)} \right] \right) / \left( \sqrt{-\frac{dg+ch}{h}} \sqrt{\left( fh + \right.} \right. \\
 & \quad \left. \frac{d^2 eg}{(c+dx)^2} - \frac{cdfg}{(c+dx)^2} - \frac{cdeh}{(c+dx)^2} + \frac{c^2 fh}{(c+dx)^2} + \frac{dfg}{c+dx} + \frac{deh}{c+dx} - \frac{2cfh}{c+dx} \right) \left. \right) - \\
 & \left( i ad \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \text{EllipticPi} \left[ \frac{(bc-ad)h}{b(-dg+ch)}, \right. \right.
 \end{aligned}$$





$$\begin{aligned}
 & \left. \left( \frac{dfg}{c+dx} + \frac{deh}{c+dx} - \frac{2cfh}{c+dx} \right) \right) - \left( i a d \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \right. \\
 & \left. \text{EllipticPi} \left[ \frac{(bc-ad)h}{b(-dg+ch)}, i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{-dg+ch}{h}}}{\sqrt{c+dx}} \right], \frac{(-de+cf)h}{f(-dg+ch)} \right] \right) / \\
 & \left( b \sqrt{-\frac{-dg+ch}{h}} \sqrt{\left( fh + \frac{d^2eg}{(c+dx)^2} - \frac{cdfg}{(c+dx)^2} - \frac{cdeh}{(c+dx)^2} + \right. \right. \\
 & \left. \left. \frac{c^2fh}{(c+dx)^2} + \frac{dfg}{c+dx} + \frac{deh}{c+dx} - \frac{2cfh}{c+dx} \right)} \right) - \frac{1}{(bc-ad)^2} \\
 & 2ab^2Cdeh \left( \left( i c \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \text{EllipticPi} \left[ \frac{(bc-ad)h}{b(-dg+ch)}, \right. \right. \right. \\
 & \left. \left. i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{-dg+ch}{h}}}{\sqrt{c+dx}} \right], \frac{(-de+cf)h}{f(-dg+ch)} \right] \right) / \left( \sqrt{-\frac{-dg+ch}{h}} \sqrt{\left( fh + \right. \right.} \\
 & \left. \left. \frac{d^2eg}{(c+dx)^2} - \frac{cdfg}{(c+dx)^2} - \frac{cdeh}{(c+dx)^2} + \frac{c^2fh}{(c+dx)^2} + \frac{dfg}{c+dx} + \frac{deh}{c+dx} - \frac{2cfh}{c+dx} \right)} \right) - \\
 & \left( i a d \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \text{EllipticPi} \left[ \frac{(bc-ad)h}{b(-dg+ch)}, \right. \right. \\
 & \left. \left. i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{-dg+ch}{h}}}{\sqrt{c+dx}} \right], \frac{(-de+cf)h}{f(-dg+ch)} \right] \right) / \left( b \sqrt{-\frac{-dg+ch}{h}} \sqrt{\left( fh + \right. \right.}
 \end{aligned}$$

$$\left. \left( \frac{d^2 e g}{(c+dx)^2} - \frac{c d f g}{(c+dx)^2} - \frac{c d e h}{(c+dx)^2} + \frac{c^2 f h}{(c+dx)^2} + \frac{d f g}{c+dx} + \frac{d e h}{c+dx} - \frac{2 c f h}{c+dx} \right) \right) +$$

$$\frac{1}{(bc-ad)^3} b^4 B c^2 f h \left( \left( i c \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \operatorname{EllipticPi} \left[ \frac{(bc-ad)h}{b(-dg+ch)}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{-dg+ch}{h}}}{\sqrt{c+dx}} \right], \frac{(-de+cf)h}{f(-dg+ch)} \right] \right) / \right.$$

$$\left. \left( \sqrt{\frac{-dg+ch}{h}} \sqrt{\left( f h + \frac{d^2 e g}{(c+dx)^2} - \frac{c d f g}{(c+dx)^2} - \frac{c d e h}{(c+dx)^2} + \frac{c^2 f h}{(c+dx)^2} + \frac{d f g}{c+dx} + \frac{d e h}{c+dx} - \frac{2 c f h}{c+dx} \right)} \right) - \left( i a d \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \operatorname{EllipticPi} \left[ \frac{(bc-ad)h}{b(-dg+ch)}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{-dg+ch}{h}}}{\sqrt{c+dx}} \right], \frac{(-de+cf)h}{f(-dg+ch)} \right] \right) / \right.$$

$$\left. \left( b \sqrt{\frac{-dg+ch}{h}} \sqrt{\left( f h + \frac{d^2 e g}{(c+dx)^2} - \frac{c d f g}{(c+dx)^2} - \frac{c d e h}{(c+dx)^2} + \frac{c^2 f h}{(c+dx)^2} + \frac{d f g}{c+dx} + \frac{d e h}{c+dx} - \frac{2 c f h}{c+dx} \right)} \right) \right) - \frac{1}{(bc-ad)^3}$$

$$2 a b^3 c^2 C f h \left( \left( i c \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \operatorname{EllipticPi} \left[ \frac{(bc-ad)h}{b(-dg+ch)}, \right. \right.$$



$$\begin{aligned}
 & \left. \text{EllipticPi} \left[ \frac{(bc-ad)h}{b(-dg+ch)}, \text{i ArcSinh} \left[ \frac{\sqrt{-\frac{dg+ch}{h}}}{\sqrt{c+dx}} \right], \frac{(-de+cf)h}{f(-dg+ch)} \right] \right/ \\
 & \left( b \sqrt{-\frac{dg+ch}{h}} \sqrt{\left( fh + \frac{d^2 eg}{(c+dx)^2} - \frac{cdfg}{(c+dx)^2} - \frac{cdeh}{(c+dx)^2} + \right.} \right. \\
 & \left. \left. \frac{c^2 fh}{(c+dx)^2} + \frac{dfg}{c+dx} + \frac{deh}{c+dx} - \frac{2cfh}{c+dx} \right) \right) + \frac{1}{(bc-ad)^2} \\
 & 4ab^2 c C f h \left( \left( \text{i c} \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \text{EllipticPi} \left[ \frac{(bc-ad)h}{b(-dg+ch)}, \right. \right. \right. \\
 & \left. \left. \left. \text{i ArcSinh} \left[ \frac{\sqrt{-\frac{dg+ch}{h}}}{\sqrt{c+dx}} \right], \frac{(-de+cf)h}{f(-dg+ch)} \right] \right) / \left( \sqrt{-\frac{dg+ch}{h}} \sqrt{\left( fh + \right.} \right. \\
 & \left. \left. \frac{d^2 eg}{(c+dx)^2} - \frac{cdfg}{(c+dx)^2} - \frac{cdeh}{(c+dx)^2} + \frac{c^2 fh}{(c+dx)^2} + \frac{dfg}{c+dx} + \frac{deh}{c+dx} - \frac{2cfh}{c+dx} \right) \right) - \\
 & \left( \text{i a d} \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \text{EllipticPi} \left[ \frac{(bc-ad)h}{b(-dg+ch)}, \right. \right. \\
 & \left. \left. \left. \text{i ArcSinh} \left[ \frac{\sqrt{-\frac{dg+ch}{h}}}{\sqrt{c+dx}} \right], \frac{(-de+cf)h}{f(-dg+ch)} \right] \right) / \left( b \sqrt{-\frac{dg+ch}{h}} \sqrt{\left( fh + \right.} \right. \\
 & \left. \left. \frac{d^2 eg}{(c+dx)^2} - \frac{cdfg}{(c+dx)^2} - \frac{cdeh}{(c+dx)^2} + \frac{c^2 fh}{(c+dx)^2} + \frac{dfg}{c+dx} + \frac{deh}{c+dx} - \frac{2cfh}{c+dx} \right) \right) -
 \end{aligned}$$

$$\begin{aligned}
 & \frac{1}{(bc-ad)^2} 2ab^2 Bdfh \left( \left( i c \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \operatorname{EllipticPi} \left[ \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{(bc-ad)h}{b(-dg+ch)}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{-\frac{-dg+ch}{h}}}{\sqrt{c+dx}} \right], \frac{(-de+cf)h}{f(-dg+ch)} \right] \right) / \right. \\
 & \left( \sqrt{-\frac{-dg+ch}{h}} \sqrt{\left( fh + \frac{d^2 eg}{(c+dx)^2} - \frac{cdfg}{(c+dx)^2} - \frac{cdeh}{(c+dx)^2} + \frac{c^2 fh}{(c+dx)^2} + \right. \right. \\
 & \quad \left. \left. \frac{dfg}{c+dx} + \frac{deh}{c+dx} - \frac{2cfh}{c+dx} \right) \right) - \left( i ad \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \right. \\
 & \quad \left. \operatorname{EllipticPi} \left[ \frac{(bc-ad)h}{b(-dg+ch)}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{-\frac{-dg+ch}{h}}}{\sqrt{c+dx}} \right], \frac{(-de+cf)h}{f(-dg+ch)} \right] \right) / \right. \\
 & \left( b \sqrt{-\frac{-dg+ch}{h}} \sqrt{\left( fh + \frac{d^2 eg}{(c+dx)^2} - \frac{cdfg}{(c+dx)^2} - \frac{cdeh}{(c+dx)^2} + \right. \right. \\
 & \quad \left. \left. \frac{c^2 fh}{(c+dx)^2} + \frac{dfg}{c+dx} + \frac{deh}{c+dx} - \frac{2cfh}{c+dx} \right) \right) \left. \right) + \frac{1}{(bc-ad)^2} \\
 & 2a^2 b Cdfh \left( \left( i c \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \operatorname{EllipticPi} \left[ \frac{(bc-ad)h}{b(-dg+ch)}, \right. \right. \right. \\
 & \quad \left. \left. \left. i \operatorname{ArcSinh} \left[ \frac{\sqrt{-\frac{-dg+ch}{h}}}{\sqrt{c+dx}} \right], \frac{(-de+cf)h}{f(-dg+ch)} \right] \right) / \left( \sqrt{-\frac{-dg+ch}{h}} \sqrt{\left( fh + \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left. \left( \frac{d^2 e g}{(c+dx)^2} - \frac{c d f g}{(c+dx)^2} - \frac{c d e h}{(c+dx)^2} + \frac{c^2 f h}{(c+dx)^2} + \frac{d f g}{c+dx} + \frac{d e h}{c+dx} - \frac{2 c f h}{c+dx} \right) \right) - \\
 & \left( i a d \sqrt{1 - \frac{-d e + c f}{f (c+dx)}} \sqrt{1 - \frac{-d g + c h}{h (c+dx)}} \operatorname{EllipticPi} \left[ \frac{(b c - a d) h}{b (-d g + c h)}, \right. \right. \\
 & \left. \left. i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{-d g + c h}{h}}}{\sqrt{c+dx}} \right], \frac{(-d e + c f) h}{f (-d g + c h)} \right] \right) / \left( b \sqrt{\frac{-d g + c h}{h}} \sqrt{f h +} \right. \\
 & \left. \left. \frac{d^2 e g}{(c+dx)^2} - \frac{c d f g}{(c+dx)^2} - \frac{c d e h}{(c+dx)^2} + \frac{c^2 f h}{(c+dx)^2} + \frac{d f g}{c+dx} + \frac{d e h}{c+dx} - \frac{2 c f h}{c+dx} \right) \right) + \\
 & \frac{1}{b c - a d} b^2 B f h \left( \left( i c \sqrt{1 - \frac{-d e + c f}{f (c+dx)}} \sqrt{1 - \frac{-d g + c h}{h (c+dx)}} \operatorname{EllipticPi} \left[ \frac{(b c - a d) h}{b (-d g + c h)}, \right. \right. \right. \\
 & \left. \left. i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{-d g + c h}{h}}}{\sqrt{c+dx}} \right], \frac{(-d e + c f) h}{f (-d g + c h)} \right] \right) / \left( \sqrt{\frac{-d g + c h}{h}} \sqrt{f h +} \right. \\
 & \left. \left. \frac{d^2 e g}{(c+dx)^2} - \frac{c d f g}{(c+dx)^2} - \frac{c d e h}{(c+dx)^2} + \frac{c^2 f h}{(c+dx)^2} + \frac{d f g}{c+dx} + \frac{d e h}{c+dx} - \frac{2 c f h}{c+dx} \right) \right) - \\
 & \left( i a d \sqrt{1 - \frac{-d e + c f}{f (c+dx)}} \sqrt{1 - \frac{-d g + c h}{h (c+dx)}} \operatorname{EllipticPi} \left[ \frac{(b c - a d) h}{b (-d g + c h)}, \right. \right. \\
 & \left. \left. i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{-d g + c h}{h}}}{\sqrt{c+dx}} \right], \frac{(-d e + c f) h}{f (-d g + c h)} \right] \right) / \left( b \sqrt{\frac{-d g + c h}{h}} \sqrt{f h +} \right.
 \end{aligned}$$

$$\left. \left( \frac{d^2 e g}{(c+dx)^2} - \frac{c d f g}{(c+dx)^2} - \frac{c d e h}{(c+dx)^2} + \frac{c^2 f h}{(c+dx)^2} + \frac{d f g}{c+dx} + \frac{d e h}{c+dx} - \frac{2 c f h}{c+dx} \right) \right) -$$

$$\frac{1}{b c - a d} 2 a b C f h \left( \left( i c \sqrt{1 - \frac{-d e + c f}{f (c+dx)}} \sqrt{1 - \frac{-d g + c h}{h (c+dx)}} \text{EllipticPi} \left[ \right. \right. \right.$$

$$\left. \left. \left. \frac{(b c - a d) h}{b (-d g + c h)}, i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{-d g + c h}{h}}}{\sqrt{c+dx}} \right], \frac{(-d e + c f) h}{f (-d g + c h)} \right] \right) \right) /$$

$$\left( \sqrt{-\frac{-d g + c h}{h}} \sqrt{\left( f h + \frac{d^2 e g}{(c+dx)^2} - \frac{c d f g}{(c+dx)^2} - \frac{c d e h}{(c+dx)^2} + \frac{c^2 f h}{(c+dx)^2} + \right. \right.$$

$$\left. \left. \frac{d f g}{c+dx} + \frac{d e h}{c+dx} - \frac{2 c f h}{c+dx} \right) \right) - \left( i a d \sqrt{1 - \frac{-d e + c f}{f (c+dx)}} \sqrt{1 - \frac{-d g + c h}{h (c+dx)}} \right.$$

$$\left. \left. \text{EllipticPi} \left[ \frac{(b c - a d) h}{b (-d g + c h)}, i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{-d g + c h}{h}}}{\sqrt{c+dx}} \right], \frac{(-d e + c f) h}{f (-d g + c h)} \right] \right) \right) /$$

$$\left( b \sqrt{-\frac{-d g + c h}{h}} \sqrt{\left( f h + \frac{d^2 e g}{(c+dx)^2} - \frac{c d f g}{(c+dx)^2} - \frac{c d e h}{(c+dx)^2} + \right. \right.$$

$$\left. \left. \frac{c^2 f h}{(c+dx)^2} + \frac{d f g}{c+dx} + \frac{d e h}{c+dx} - \frac{2 c f h}{c+dx} \right) \right) \right) \right) /$$

$$\left( \left( b^2 B f h - 2 a b C f h + \frac{b^2 B d^2 e g}{(c+dx)^2} - \frac{2 a b C d^2 e g}{(c+dx)^2} - \frac{b^2 B c d f g}{(c+dx)^2} + \frac{2 a b c C d f g}{(c+dx)^2} - \right. \right.$$

$$\left. \left. \frac{b^2 B c d e h}{(c+dx)^2} + \frac{2 a b c C d e h}{(c+dx)^2} + \right. \right.$$

$$\left( \begin{aligned} & \frac{b^2 B c^2 f h}{(c+dx)^2} - \frac{2 a b c^2 C f h}{(c+dx)^2} - \\ & \frac{2 b^2 C d e g}{c+dx} + \frac{2 b^2 B d f g}{c+dx} - \frac{2 a b C d f g}{c+dx} + \\ & \frac{2 b^2 B d e h}{c+dx} - \frac{2 a b C d e h}{c+dx} - \\ & \frac{2 b^2 B c f h}{c+dx} + \frac{4 a b c C f h}{c+dx} - \\ & \left. \frac{2 a b B d f h}{c+dx} + \frac{2 a^2 C d f h}{c+dx} \right) \sqrt{e + \frac{(c+dx) \left( f - \frac{cf}{c+dx} \right)}{d}} \sqrt{g + \frac{(c+dx) \left( h - \frac{ch}{c+dx} \right)}{d}} \end{aligned} \right)$$

**Problem 21: Result more than twice size of optimal antiderivative.**

$$\int \frac{\sqrt{a+bx} (abB - a^2C + b^2Bx + b^2Cx^2)}{\sqrt{c+dx} \sqrt{e+fx} \sqrt{g+hx}} dx$$

Optimal (type 4, 980 leaves, 9 steps):

$$\begin{aligned}
 & \frac{1}{4 d f^2 h^2 \sqrt{c+d x}} b (4 b B d f h + C (a d f h - 3 b (d f g + d e h + c f h))) \sqrt{a+b x} \sqrt{e+f x} \sqrt{g+h x} + \\
 & \frac{b^2 C \sqrt{a+b x} \sqrt{c+d x} \sqrt{e+f x} \sqrt{g+h x}}{2 d f h} - \\
 & \left( b \sqrt{d g - c h} \sqrt{f g - e h} (4 b B d f h + C (a d f h - 3 b (d f g + d e h + c f h))) \sqrt{a+b x} \right. \\
 & \left. \sqrt{-\frac{(d e - c f) (g + h x)}{(f g - e h) (c + d x)}} \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{d g - c h} \sqrt{e + f x}}{\sqrt{f g - e h} \sqrt{c + d x}}\right], \frac{(b c - a d) (f g - e h)}{(b e - a f) (d g - c h)}\right] \right) / \\
 & \left( 4 d^2 f^2 h^2 \sqrt{\frac{(d e - c f) (a + b x)}{(b e - a f) (c + d x)}} \sqrt{g + h x} \right) + \\
 & \left( (b e - a f) \sqrt{b g - a h} (a C d f h - b (4 B d f h - C (3 d f g + 3 d e h + c f h))) \sqrt{\frac{(b e - a f) (c + d x)}{(d e - c f) (a + b x)}} \right. \\
 & \left. \sqrt{g + h x} \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{b g - a h} \sqrt{e + f x}}{\sqrt{f g - e h} \sqrt{a + b x}}\right], -\frac{(b c - a d) (f g - e h)}{(d e - c f) (b g - a h)}\right] \right) / \\
 & \left( 4 d f^2 h^2 \sqrt{f g - e h} \sqrt{c + d x} \sqrt{-\frac{(b e - a f) (g + h x)}{(f g - e h) (a + b x)}} - \frac{1}{4 d^2 \sqrt{b c - a d} f^2 h^3 \sqrt{c + d x} \sqrt{e + f x}} \right. \\
 & \left. \sqrt{-d g + c h} ((a d f h + b (d f g + d e h + c f h)) (4 b B d f h + C (a d f h - 3 b (d f g + d e h + c f h))) + \right. \\
 & \left. 4 d f h (2 a^2 C d f h + b^2 C (d e g + c f g + c e h) - a b (4 B d f h - C (d f g + d e h + c f h)))) \right) \\
 & (a + b x) \sqrt{\frac{(b g - a h) (c + d x)}{(d g - c h) (a + b x)}} \sqrt{\frac{(b g - a h) (e + f x)}{(f g - e h) (a + b x)}} \\
 & \operatorname{EllipticPi}\left[-\frac{b (d g - c h)}{(b c - a d) h}, \operatorname{ArcSin}\left[\frac{\sqrt{b c - a d} \sqrt{g + h x}}{\sqrt{-d g + c h} \sqrt{a + b x}}\right], \frac{(b e - a f) (d g - c h)}{(b c - a d) (f g - e h)}\right]
 \end{aligned}$$

Result (type 4, 21555 leaves): Display of huge result suppressed!

**Problem 22: Result more than twice size of optimal antiderivative.**

$$\int \frac{a b B - a^2 C + b^2 B x + b^2 C x^2}{\sqrt{a+b x} \sqrt{c+d x} \sqrt{e+f x} \sqrt{g+h x}} dx$$

Optimal (type 4, 734 leaves, 8 steps):

$$\frac{bC\sqrt{a+bx}\sqrt{e+fx}\sqrt{g+hx}}{fh\sqrt{c+dx}} - \left( bC\sqrt{dg-ch}\sqrt{fg-eh}\sqrt{a+bx}\sqrt{-\frac{(de-cf)(g+hx)}{(fg-eh)(c+dx)}} \right. \\ \left. \text{EllipticE}\left[\text{ArcSin}\left[\frac{\sqrt{dg-ch}\sqrt{e+fx}}{\sqrt{fg-eh}\sqrt{c+dx}}\right], \frac{(bc-ad)(fg-eh)}{(be-af)(dg-ch)}\right] \right) / \\ \left( dfh\sqrt{\frac{(de-cf)(a+bx)}{(be-af)(c+dx)}}\sqrt{g+hx} \right) - \left( C(be-af)\sqrt{bg-ah}\sqrt{\frac{(be-af)(c+dx)}{(de-cf)(a+bx)}} \right. \\ \left. \sqrt{g+hx}\text{EllipticF}\left[\text{ArcSin}\left[\frac{\sqrt{bg-ah}\sqrt{e+fx}}{\sqrt{fg-eh}\sqrt{a+bx}}\right], -\frac{(bc-ad)(fg-eh)}{(de-cf)(bg-ah)}\right] \right) / \\ \left( fh\sqrt{fg-eh}\sqrt{c+dx}\sqrt{-\frac{(be-af)(g+hx)}{(fg-eh)(a+bx)}} \right) - \\ \left( \sqrt{-dg+ch}(aCdfh-b(2Bdfh-C(dfg+deh+cfh)))(a+bx)\sqrt{\frac{(bg-ah)(c+dx)}{(dg-ch)(a+bx)}} \right. \\ \left. \sqrt{\frac{(bg-ah)(e+fx)}{(fg-eh)(a+bx)}}\text{EllipticPi}\left[-\frac{b(dg-ch)}{(bc-ad)h}, \text{ArcSin}\left[\frac{\sqrt{bc-ad}\sqrt{g+hx}}{\sqrt{-dg+ch}\sqrt{a+bx}}\right], \right. \right. \\ \left. \left. \frac{(be-af)(dg-ch)}{(bc-ad)(fg-eh)} \right) \right] / (d\sqrt{bc-ad}fh^2\sqrt{c+dx}\sqrt{e+fx})$$

Result (type 4, 6667 leaves):

$$\frac{1}{d^2} 2 \left( \left( bC(c+dx)^{3/2} \left( f + \frac{de}{c+dx} - \frac{cf}{c+dx} \right) \left( h + \frac{dg}{c+dx} - \frac{ch}{c+dx} \right) \sqrt{a + \frac{(c+dx)(b - \frac{bc}{c+dx})}{d}} \right) / \right. \\ \left( 2fh\sqrt{e + \frac{(c+dx)(f - \frac{cf}{c+dx})}{d}}\sqrt{g + \frac{(c+dx)(h - \frac{ch}{c+dx})}{d}} \right) - \\ \left( d(bg-ah)(dg-ch)(bCfg+bCeh-2bBfh+2aCfh)\sqrt{c+dx}\sqrt{\left( \left( b - \frac{bc}{c+dx} + \frac{ad}{c+dx} \right) \right.} \right. \\ \left. \left. \left( f + \frac{de}{c+dx} - \frac{cf}{c+dx} \right) \left( h + \frac{dg}{c+dx} - \frac{ch}{c+dx} \right) \right) \sqrt{a + \frac{(c+dx)(b - \frac{bc}{c+dx})}{d}} \right)$$

$$\left( \left( d e \sqrt{-\frac{(bc-ad)(-dg+ch)\left(-\frac{b}{bc-ad} + \frac{1}{c+dx}\right)}{-bdg+adh}} \left(-\frac{f}{-de+cf} + \frac{1}{c+dx}\right) \sqrt{\frac{-\frac{h}{-dg+ch} + \frac{1}{c+dx}}{\frac{f}{-de+cf} - \frac{h}{-dg+ch}}} \right. \right.$$

$$\left. \left. \left( (-bdg+adh) \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\sqrt{\frac{(de-cf)\left(h + \frac{dg}{c+dx} - \frac{ch}{c+dx}\right)}{d(-fg+eh)}}\right]\right], \right. \right.$$

$$\left. \left. \frac{(bc-ad)(-fg+eh)}{(-de+cf)(-bg+ah)} \right] \right) / \left( (bc-ad)(-dg+ch) - \frac{1}{bc-ad} b \operatorname{EllipticF}\left[ \right. \right.$$

$$\left. \left. \operatorname{ArcSin}\left[\sqrt{\frac{(de-cf)\left(h + \frac{dg}{c+dx} - \frac{ch}{c+dx}\right)}{d(-fg+eh)}}\right], \frac{(bc-ad)(-fg+eh)}{(-de+cf)(-bg+ah)} \right] \right) \right) /$$

$$\left( \sqrt{\frac{-\frac{f}{-de+cf} + \frac{1}{c+dx}}{-\frac{f}{-de+cf} + \frac{h}{-dg+ch}}} \sqrt{\left(b + \frac{-bc+ad}{c+dx}\right) \left(f + \frac{de-cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} \right) - \left( c f$$

$$\sqrt{-\frac{(bc-ad)(-dg+ch)\left(-\frac{b}{bc-ad} + \frac{1}{c+dx}\right)}{-bdg+adh}} \left(-\frac{f}{-de+cf} + \frac{1}{c+dx}\right) \sqrt{\frac{-\frac{h}{-dg+ch} + \frac{1}{c+dx}}{\frac{f}{-de+cf} - \frac{h}{-dg+ch}}} \right.$$

$$\left. \left( (-bdg+adh) \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\sqrt{\frac{(de-cf)\left(h + \frac{dg}{c+dx} - \frac{ch}{c+dx}\right)}{d(-fg+eh)}}\right]\right], \right. \right.$$

$$\left. \left. \frac{(bc-ad)(-fg+eh)}{(-de+cf)(-bg+ah)} \right] \right) / \left( (bc-ad)(-dg+ch) - \frac{1}{bc-ad} b \operatorname{EllipticF}\left[ \right. \right.$$

$$\left. \left. \operatorname{ArcSin}\left[\sqrt{\frac{(de-cf)\left(h + \frac{dg}{c+dx} - \frac{ch}{c+dx}\right)}{d(-fg+eh)}}\right], \frac{(bc-ad)(-fg+eh)}{(-de+cf)(-bg+ah)} \right] \right) \right) /$$

$$\left( \sqrt{\frac{-\frac{f}{-de+cf} + \frac{1}{c+dx}}{-\frac{f}{-de+cf} + \frac{h}{-dg+ch}}} \sqrt{\left(b + \frac{-bc+ad}{c+dx}\right) \left(f + \frac{de-cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} \right) +$$

$$\left( f \sqrt{\frac{-\frac{b}{bc-ad} + \frac{1}{c+dx}}{-\frac{b}{bc-ad} + \frac{h}{-dg+ch}}} \sqrt{\frac{-\frac{f}{-de+cf} + \frac{1}{c+dx}}{-\frac{f}{-de+cf} + \frac{h}{-dg+ch}}} \left(-\frac{h}{-dg+ch} + \frac{1}{c+dx}\right) \right)$$

$$\begin{aligned}
 & \left. \text{EllipticF}\left[\text{ArcSin}\left[\sqrt{\frac{(-de+cf)\left(-h-\frac{dg}{c+dx}+\frac{ch}{c+dx}\right)}{d(-fg+eh)}}\right], \frac{(bc-ad)(-fg+eh)}{(-de+cf)(-bg+ah)}\right]\right/ \\
 & \left(\sqrt{\frac{-\frac{h}{-dg+ch}+\frac{1}{c+dx}}{\frac{f}{-de+cf}-\frac{h}{-dg+ch}}}\sqrt{\left(b+\frac{-bc+ad}{c+dx}\right)\left(f+\frac{de-cf}{c+dx}\right)\left(h+\frac{dg-ch}{c+dx}\right)}\right)\right/ \\
 & \left(2fh^2(fg-eh)\left(b-\frac{bc}{c+dx}+\frac{ad}{c+dx}\right)\sqrt{e+\frac{(c+dx)\left(f-\frac{cf}{c+dx}\right)}{d}}\right. \\
 & \left.\sqrt{g+\frac{(c+dx)\left(h-\frac{ch}{c+dx}\right)}{d}}\right)+ \\
 & \left(d(b e-a f)(d e-c f)(b c f g+b c e h-2 b b f h+2 a c f h)\sqrt{c+d x}\right. \\
 & \left.\sqrt{\left(\left(b-\frac{b c}{c+d x}+\frac{a d}{c+d x}\right)\left(f+\frac{d e}{c+d x}-\frac{c f}{c+d x}\right)\left(h+\frac{d g}{c+d x}-\frac{c h}{c+d x}\right)\right)}\right. \\
 & \left.\sqrt{a+\frac{(c+d x)\left(b-\frac{b c}{c+d x}\right)}{d}}\right. \\
 & \left.\left(d g \sqrt{-\frac{(b c-a d)(-d g+c h)\left(-\frac{b}{b c-a d}+\frac{1}{c+d x}\right)}{-b d g+a d h}\left(-\frac{f}{-d e+c f}+\frac{1}{c+d x}\right)}\sqrt{\frac{-\frac{h}{-d g+c h}+\frac{1}{c+d x}}{\frac{f}{-d e+c f}-\frac{h}{-d g+c h}}}\right.\right. \\
 & \left.\left.\left(\left(-b d g+a d h\right) \text{EllipticE}\left[\text{ArcSin}\left[\sqrt{\frac{(d e-c f)\left(h+\frac{d g}{c+d x}-\frac{c h}{c+d x}\right)}{d(-f g+e h)}}\right],\right.\right.\right. \\
 & \left.\left.\left.\frac{(b c-a d)(-f g+e h)}{(-d e+c f)(-b g+a h)}\right]\right) / \left(\left(b c-a d\right)(-d g+c h)\right)-\frac{1}{b c-a d} b \text{EllipticF}\left[\right. \\
 & \left.\left.\text{ArcSin}\left[\sqrt{\frac{(d e-c f)\left(h+\frac{d g}{c+d x}-\frac{c h}{c+d x}\right)}{d(-f g+e h)}}\right], \frac{(b c-a d)(-f g+e h)}{(-d e+c f)(-b g+a h)}\right]\right)\right) /
 \end{aligned}$$

$$\begin{aligned}
 & \left( \sqrt{\frac{-\frac{f}{-de+cf} + \frac{1}{c+dx}}{-\frac{f}{-de+cf} + \frac{h}{-dg+ch}}} \sqrt{\left(b + \frac{-bc+ad}{c+dx}\right) \left(f + \frac{de-cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} \right) - \left( ch \right. \\
 & \sqrt{-\frac{(bc-ad)(-dg+ch)\left(-\frac{b}{bc-ad} + \frac{1}{c+dx}\right)}{-bdg+adh}} \left(-\frac{f}{-de+cf} + \frac{1}{c+dx}\right) \sqrt{\frac{-\frac{h}{-dg+ch} + \frac{1}{c+dx}}{\frac{f}{-de+cf} - \frac{h}{-dg+ch}}} \\
 & \left. \left( (-bdg+adh) \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\sqrt{\frac{(de-cf)\left(h + \frac{dg}{c+dx} - \frac{ch}{c+dx}\right)}{d(-fg+eh)}}\right], \right. \right. \\
 & \left. \left. \frac{(bc-ad)(-fg+eh)}{(-de+cf)(-bg+ah)} \right] \right) / \left( (bc-ad)(-dg+ch) - \frac{1}{bc-ad} b \operatorname{EllipticF}\left[ \right. \right. \\
 & \left. \left. \operatorname{ArcSin}\left[\sqrt{\frac{(de-cf)\left(h + \frac{dg}{c+dx} - \frac{ch}{c+dx}\right)}{d(-fg+eh)}}\right], \frac{(bc-ad)(-fg+eh)}{(-de+cf)(-bg+ah)} \right] \right) / \\
 & \left( \sqrt{\frac{-\frac{f}{-de+cf} + \frac{1}{c+dx}}{-\frac{f}{-de+cf} + \frac{h}{-dg+ch}}} \sqrt{\left(b + \frac{-bc+ad}{c+dx}\right) \left(f + \frac{de-cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} \right) + \\
 & \left( h \sqrt{\frac{-\frac{b}{bc-ad} + \frac{1}{c+dx}}{-\frac{b}{bc-ad} + \frac{h}{-dg+ch}}} \sqrt{\frac{-\frac{f}{-de+cf} + \frac{1}{c+dx}}{-\frac{f}{-de+cf} + \frac{h}{-dg+ch}}} \left(-\frac{h}{-dg+ch} + \frac{1}{c+dx}\right) \right. \\
 & \left. \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\sqrt{\frac{(-de+cf)\left(-h - \frac{dg}{c+dx} + \frac{ch}{c+dx}\right)}{d(-fg+eh)}}\right], \frac{(bc-ad)(-fg+eh)}{(-de+cf)(-bg+ah)} \right] \right) / \\
 & \left( \sqrt{\frac{-\frac{h}{-dg+ch} + \frac{1}{c+dx}}{\frac{f}{-de+cf} - \frac{h}{-dg+ch}}} \sqrt{\left(b + \frac{-bc+ad}{c+dx}\right) \left(f + \frac{de-cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} \right) / \\
 & \left( 2f^2 h (fg-eh) \left(b - \frac{bc}{c+dx} + \frac{ad}{c+dx}\right) \sqrt{e + \frac{(c+dx)\left(f - \frac{cf}{c+dx}\right)}{d}} \right. \\
 & \left. \sqrt{g + \frac{(c+dx)\left(h - \frac{ch}{c+dx}\right)}{d}} \right) +
 \end{aligned}$$

$$\frac{1}{2 f^2 h^2 \left( b - \frac{bc}{c+dx} + \frac{ad}{c+dx} \right) \sqrt{e + \frac{(c+dx) \left( f - \frac{cf}{c+dx} \right)}{d}} \sqrt{g + \frac{(c+dx) \left( h - \frac{ch}{c+dx} \right)}{d}}}$$

b

$$\frac{(b c d f g + b c d e h + b c c f h - 2 b b d f h + a c d f h)}{\sqrt{c+dx}}$$

$$\sqrt{\left( \left( b - \frac{bc}{c+dx} + \frac{ad}{c+dx} \right) \left( f + \frac{de}{c+dx} - \frac{cf}{c+dx} \right) \left( h + \frac{dg}{c+dx} - \frac{ch}{c+dx} \right) \right)}$$

$$\sqrt{a + \frac{(c+dx) \left( b - \frac{bc}{c+dx} \right)}{d}}$$

$$\left( d^2 e g \sqrt{-\frac{(bc-ad)(-dg+ch) \left( -\frac{b}{bc-ad} + \frac{1}{c+dx} \right)}{-bdg+adh}} \right.$$

$$\left. \left( -\frac{f}{-de+cf} + \frac{1}{c+dx} \right) \sqrt{\frac{-\frac{h}{-dg+ch} + \frac{1}{c+dx}}{\frac{f}{-de+cf} - \frac{h}{-dg+ch}}} \right.$$

$$\left. \left( (-bdg+adh) \operatorname{EllipticE} \left[ \operatorname{ArcSin} \left[ \sqrt{\frac{(de-cf) \left( h + \frac{dg}{c+dx} - \frac{ch}{c+dx} \right)}{d(-fg+eh)}} \right], \right. \right.$$

$$\left. \left. \frac{(bc-ad)(-fg+eh)}{(-de+cf)(-bg+ah)} \right] \right) / \left( (bc-ad)(-dg+ch) - \frac{1}{bc-ad} \right)$$

$$b \operatorname{EllipticF} \left[ \operatorname{ArcSin} \left[ \sqrt{\frac{(de-cf) \left( h + \frac{dg}{c+dx} - \frac{ch}{c+dx} \right)}{d(-fg+eh)}} \right], \frac{(bc-ad)(-fg+eh)}{(-de+cf)(-bg+ah)} \right] \right) /$$

$$\left( \sqrt{\frac{-\frac{f}{-de+cf} + \frac{1}{c+dx}}{-\frac{f}{-de+cf} + \frac{h}{-dg+ch}}} \sqrt{\left( b + \frac{-bc+ad}{c+dx} \right) \left( f + \frac{de-cf}{c+dx} \right) \left( h + \frac{dg-ch}{c+dx} \right)} \right) -$$

$$\left( c d f g \sqrt{-\frac{(bc-ad)(-dg+ch) \left( -\frac{b}{bc-ad} + \frac{1}{c+dx} \right)}{-bdg+adh}} \right.$$

$$\left. \left( -\frac{f}{-de+cf} + \frac{1}{c+dx} \right) \sqrt{\frac{-\frac{h}{-dg+ch} + \frac{1}{c+dx}}{-\frac{f}{-de+cf} - \frac{h}{-dg+ch}}} \right)$$

$$\left( \left( (-bdg + adh) \operatorname{EllipticE} \left[ \operatorname{ArcSin} \left[ \sqrt{\frac{(de - cf) \left( h + \frac{dg}{c+dx} - \frac{ch}{c+dx} \right)}{d(-fg + eh)}} \right], \right. \right. \right.$$

$$\left. \left. \left. \frac{(bc - ad)(-fg + eh)}{(-de + cf)(-bg + ah)} \right] \right) / \left( (bc - ad)(-dg + ch) \right) - \frac{1}{bc - ad} \right.$$

$$\left. \left. \left. b \operatorname{EllipticF} \left[ \operatorname{ArcSin} \left[ \sqrt{\frac{(de - cf) \left( h + \frac{dg}{c+dx} - \frac{ch}{c+dx} \right)}{d(-fg + eh)}} \right], \frac{(bc - ad)(-fg + eh)}{(-de + cf)(-bg + ah)} \right] \right) \right) /$$

$$\left( \sqrt{\frac{-\frac{f}{-de+cf} + \frac{1}{c+dx}}{-\frac{f}{-de+cf} + \frac{h}{-dg+ch}}} \sqrt{\left( b + \frac{-bc+ad}{c+dx} \right) \left( f + \frac{de- cf}{c+dx} \right) \left( h + \frac{dg-ch}{c+dx} \right)} \right) -$$

$$\left( cdeh \sqrt{-\frac{(bc - ad)(-dg + ch) \left( -\frac{b}{bc - ad} + \frac{1}{c+dx} \right)}{-bdg + adh}} \right.$$

$$\left. \left( -\frac{f}{-de + cf} + \frac{1}{c + dx} \right) \sqrt{\frac{-\frac{h}{-dg+ch} + \frac{1}{c+dx}}{\frac{f}{-de+cf} - \frac{h}{-dg+ch}}} \right)$$

$$\left( \left( (-bdg + adh) \operatorname{EllipticE} \left[ \operatorname{ArcSin} \left[ \sqrt{\frac{(de - cf) \left( h + \frac{dg}{c+dx} - \frac{ch}{c+dx} \right)}{d(-fg + eh)}} \right], \right. \right. \right.$$

$$\left. \left. \left. \frac{(bc - ad)(-fg + eh)}{(-de + cf)(-bg + ah)} \right] \right) / \left( (bc - ad)(-dg + ch) \right) - \frac{1}{bc - ad} \right.$$

$$\left. \left. \left. b \operatorname{EllipticF} \left[ \operatorname{ArcSin} \left[ \sqrt{\frac{(de - cf) \left( h + \frac{dg}{c+dx} - \frac{ch}{c+dx} \right)}{d(-fg + eh)}} \right], \frac{(bc - ad)(-fg + eh)}{(-de + cf)(-bg + ah)} \right] \right) \right) /$$

$$\left( \sqrt{\frac{-\frac{f}{-de+cf} + \frac{1}{c+dx}}{-\frac{f}{-de+cf} + \frac{h}{-dg+ch}}} \sqrt{\left( b + \frac{-bc+ad}{c+dx} \right) \left( f + \frac{de- cf}{c+dx} \right) \left( h + \frac{dg-ch}{c+dx} \right)} \right) +$$

$$\left( c^2fh \sqrt{-\frac{(bc - ad)(-dg + ch) \left( -\frac{b}{bc - ad} + \frac{1}{c+dx} \right)}{-bdg + adh}} \right)$$

$$\left( -\frac{f}{-de+cf} + \frac{1}{c+dx} \right) \sqrt{\frac{-\frac{h}{-dg+ch} + \frac{1}{c+dx}}{\frac{f}{-de+cf} - \frac{h}{-dg+ch}}}$$

$$\left( (-bdg+adh) \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\sqrt{\frac{(de-cf)\left(h+\frac{dg}{c+dx}-\frac{ch}{c+dx}\right)}{d(-fg+eh)}}\right]\right], \right.$$

$$\left. \frac{(bc-ad)(-fg+eh)}{(-de+cf)(-bg+ah)} \right] \Big/ \left( (bc-ad)(-dg+ch) \right) - \frac{1}{bc-ad}$$

$$b \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\sqrt{\frac{(de-cf)\left(h+\frac{dg}{c+dx}-\frac{ch}{c+dx}\right)}{d(-fg+eh)}}\right], \frac{(bc-ad)(-fg+eh)}{(-de+cf)(-bg+ah)}\right] \Big/$$

$$\left( \sqrt{\frac{-\frac{f}{-de+cf} + \frac{1}{c+dx}}{-\frac{f}{-de+cf} + \frac{h}{-dg+ch}}} \sqrt{\left(b + \frac{-bc+ad}{c+dx}\right) \left(f + \frac{de-cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} \right) +$$

$$d f g \sqrt{\frac{-\frac{b}{bc-ad} + \frac{1}{c+dx}}{-\frac{b}{bc-ad} + \frac{h}{-dg+ch}}} \sqrt{\frac{-\frac{f}{-de+cf} + \frac{1}{c+dx}}{-\frac{f}{-de+cf} + \frac{h}{-dg+ch}}} \left( -\frac{h}{-dg+ch} + \frac{1}{c+dx} \right)$$

$$\operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\sqrt{\frac{(-de+cf)\left(-h-\frac{dg}{c+dx}+\frac{ch}{c+dx}\right)}{d(-fg+eh)}}\right], \frac{(bc-ad)(-fg+eh)}{(-de+cf)(-bg+ah)}\right] \Big/$$

$$\left( \sqrt{\frac{-\frac{h}{-dg+ch} + \frac{1}{c+dx}}{\frac{f}{-de+cf} - \frac{h}{-dg+ch}}} \sqrt{\left(b + \frac{-bc+ad}{c+dx}\right) \left(f + \frac{de-cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} \right) +$$

$$d e h \sqrt{\frac{-\frac{b}{bc-ad} + \frac{1}{c+dx}}{-\frac{b}{bc-ad} + \frac{h}{-dg+ch}}} \sqrt{\frac{-\frac{f}{-de+cf} + \frac{1}{c+dx}}{-\frac{f}{-de+cf} + \frac{h}{-dg+ch}}} \left( -\frac{h}{-dg+ch} + \frac{1}{c+dx} \right)$$

$$\operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\sqrt{\frac{(-de+cf)\left(-h-\frac{dg}{c+dx}+\frac{ch}{c+dx}\right)}{d(-fg+eh)}}\right], \frac{(bc-ad)(-fg+eh)}{(-de+cf)(-bg+ah)}\right] \Big/$$

$$\left( \sqrt{\frac{-\frac{h}{-dg+ch} + \frac{1}{c+dx}}{\frac{f}{-de+cf} - \frac{h}{-dg+ch}}} \sqrt{\left(b + \frac{-bc+ad}{c+dx}\right) \left(f + \frac{de-cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} \right) -$$

$$\begin{aligned}
 & \left( 2 c f h \sqrt{\frac{-\frac{b}{bc-ad} + \frac{1}{c+dx}}{-\frac{b}{bc-ad} + \frac{h}{-dg+ch}}} \sqrt{\frac{-\frac{f}{-de+cf} + \frac{1}{c+dx}}{-\frac{f}{-de+cf} + \frac{h}{-dg+ch}}} \left( -\frac{h}{-dg+ch} + \frac{1}{c+dx} \right) \right. \\
 & \quad \left. \text{EllipticF} \left[ \text{ArcSin} \left[ \sqrt{\frac{(-de+cf) \left( -h - \frac{dg}{c+dx} + \frac{ch}{c+dx} \right)}{d(-fg+eh)}} \right], \frac{(bc-ad)(-fg+eh)}{(-de+cf)(-bg+ah)} \right] \right) / \\
 & \left( \sqrt{\frac{-\frac{h}{-dg+ch} + \frac{1}{c+dx}}{\frac{f}{-de+cf} - \frac{h}{-dg+ch}}} \sqrt{\left( b + \frac{-bc+ad}{c+dx} \right) \left( f + \frac{de-cf}{c+dx} \right) \left( h + \frac{dg-ch}{c+dx} \right)} \right) - \\
 & \left( f(-dg+ch) \left( -\frac{f}{-de+cf} + \frac{h}{-dg+ch} \right) \sqrt{\frac{-\frac{b}{bc-ad} + \frac{1}{c+dx}}{-\frac{b}{bc-ad} + \frac{h}{-dg+ch}}} \right. \\
 & \quad \left. \sqrt{-\frac{\left( -\frac{f}{-de+cf} + \frac{1}{c+dx} \right) \left( -\frac{h}{-dg+ch} + \frac{1}{c+dx} \right)}{\left( -\frac{f}{-de+cf} + \frac{h}{-dg+ch} \right)^2}} \text{EllipticPi} \left[ -\frac{-dfg+deh}{(-de+cf)h}, \right. \right. \\
 & \quad \left. \left. \text{ArcSin} \left[ \sqrt{\frac{(-de+cf) \left( -h - \frac{dg}{c+dx} + \frac{ch}{c+dx} \right)}{d(-fg+eh)}} \right], \frac{(bc-ad)(-fg+eh)}{(-de+cf)(-bg+ah)} \right] \right) / \\
 & \left. \left( \sqrt{\left( b + \frac{-bc+ad}{c+dx} \right) \left( f + \frac{de-cf}{c+dx} \right) \left( h + \frac{dg-ch}{c+dx} \right)} \right) \right)
 \end{aligned}$$

**Problem 24: Result more than twice size of optimal antiderivative.**

$$\int \frac{a b B - a^2 C + b^2 B x + b^2 C x^2}{(a+bx)^{5/2} \sqrt{c+dx} \sqrt{e+fx} \sqrt{g+hx}} dx$$

Optimal (type 4, 616 leaves, 8 steps):

$$\frac{2b(bB-2aC)d\sqrt{a+bx}\sqrt{e+fx}\sqrt{g+hx}}{(bc-ad)(be-af)(bg-ah)\sqrt{c+dx}} - \frac{2b^2(bB-2aC)\sqrt{c+dx}\sqrt{e+fx}\sqrt{g+hx}}{(bc-ad)(be-af)(bg-ah)\sqrt{a+bx}}$$

$$\left( 2b(bB-2aC)\sqrt{dg-ch}\sqrt{fg-eh}\sqrt{a+bx}\sqrt{-\frac{(de-cf)(g+hx)}{(fg-eh)(c+dx)}} \right.$$

$$\left. \text{EllipticE}\left[\text{ArcSin}\left[\frac{\sqrt{dg-ch}\sqrt{e+fx}}{\sqrt{fg-eh}\sqrt{c+dx}}\right], \frac{(bc-ad)(fg-eh)}{(be-af)(dg-ch)}\right] \right) /$$

$$\left( (bc-ad)(be-af)(bg-ah)\sqrt{\frac{(de-cf)(a+bx)}{(be-af)(c+dx)}}\sqrt{g+hx} \right) +$$

$$\left( 2(bcC-bBd+aCd)\sqrt{\frac{(be-af)(c+dx)}{(de-cf)(a+bx)}}\sqrt{g+hx} \right.$$

$$\left. \text{EllipticF}\left[\text{ArcSin}\left[\frac{\sqrt{bg-ah}\sqrt{e+fx}}{\sqrt{fg-eh}\sqrt{a+bx}}\right], -\frac{(bc-ad)(fg-eh)}{(de-cf)(bg-ah)}\right] \right) /$$

$$\left( (bc-ad)\sqrt{bg-ah}\sqrt{fg-eh}\sqrt{c+dx}\sqrt{-\frac{(be-af)(g+hx)}{(fg-eh)(a+bx)}} \right)$$

Result (type 4, 1753 leaves):

$$-\frac{2b^2(bB-2aC)\sqrt{c+dx}\sqrt{e+fx}\sqrt{g+hx}}{(bc-ad)(be-af)(bg-ah)\sqrt{a+bx}} + \frac{1}{b(-bc+ad)(-be+af)(-bg+ah)}$$

$$2 \left( \left( (-bB+2aC)(a+bx)^{5/2} \left( d + \frac{bc}{a+bx} - \frac{ad}{a+bx} \right) \left( f + \frac{be}{a+bx} - \frac{af}{a+bx} \right) \left( h + \frac{bg}{a+bx} - \frac{ah}{a+bx} \right) \right) \right) /$$

$$\left( \sqrt{c + \frac{(a+bx)(d - \frac{ad}{a+bx})}{b}} \sqrt{e + \frac{(a+bx)(f - \frac{af}{a+bx})}{b}} \sqrt{g + \frac{(a+bx)(h - \frac{ah}{a+bx})}{b}} \right) -$$

$$\frac{1}{\sqrt{c + \frac{(a+bx)(d - \frac{ad}{a+bx})}{b}} \sqrt{e + \frac{(a+bx)(f - \frac{af}{a+bx})}{b}} \sqrt{g + \frac{(a+bx)(h - \frac{ah}{a+bx})}{b}}} (bc-ad)(be-af)$$

$$(bg-ah)(a+bx)^{3/2} \sqrt{\left( \left( d + \frac{bc}{a+bx} - \frac{ad}{a+bx} \right) \left( f + \frac{be}{a+bx} - \frac{af}{a+bx} \right) \left( h + \frac{bg}{a+bx} - \frac{ah}{a+bx} \right) \right)}$$

$$\begin{aligned}
 & \left( - \left( \left( b B \sqrt{\frac{(bc-ad)(bg-ah) \left(-\frac{d}{-bc+ad} + \frac{1}{a+bx}\right)}{bdg-bch} \left(-\frac{f}{-be+af} + \frac{1}{a+bx}\right) \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{\frac{f}{-be+af} - \frac{h}{-bg+ah}}} \right. \right. \right. \\
 & \left. \left. \left( (bdg-bch) \operatorname{EllipticE} \left[ \operatorname{ArcSin} \left[ \sqrt{\frac{(be-af) \left(h + \frac{bg}{a+bx} - \frac{ah}{a+bx}\right)}{b(-fg+eh)}} \right], \right. \right. \right. \\
 & \left. \left. \left. \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right) / ((bc-ad)(bg-ah)) \right) - \\
 & \frac{1}{-bc+ad} d \operatorname{EllipticF} \left[ \operatorname{ArcSin} \left[ \sqrt{\frac{(be-af) \left(h + \frac{bg}{a+bx} - \frac{ah}{a+bx}\right)}{b(-fg+eh)}} \right], \right. \\
 & \left. \left. \left. \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right) \right] / \\
 & \left( \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right) \left(h + \frac{bg-ah}{a+bx}\right)} \right) + \\
 & \left( 2aC \sqrt{\frac{(bc-ad)(bg-ah) \left(-\frac{d}{-bc+ad} + \frac{1}{a+bx}\right)}{bdg-bch} \left(-\frac{f}{-be+af} + \frac{1}{a+bx}\right) \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{\frac{f}{-be+af} - \frac{h}{-bg+ah}}} \right. \right. \\
 & \left. \left. \left( (bdg-bch) \operatorname{EllipticE} \left[ \operatorname{ArcSin} \left[ \sqrt{\frac{(be-af) \left(h + \frac{bg}{a+bx} - \frac{ah}{a+bx}\right)}{b(-fg+eh)}} \right], \right. \right. \right. \\
 & \left. \left. \left. \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right) / ((bc-ad)(bg-ah)) \right) - \\
 & \frac{1}{-bc+ad} d \operatorname{EllipticF} \left[ \operatorname{ArcSin} \left[ \sqrt{\frac{(be-af) \left(h + \frac{bg}{a+bx} - \frac{ah}{a+bx}\right)}{b(-fg+eh)}} \right], \right. \\
 & \left. \left. \left. \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right) \right] /
 \end{aligned}$$

$$\left( \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right) \left(h + \frac{bg-ah}{a+bx}\right)} \right) -$$

$$\left( C \sqrt{\frac{-\frac{d}{-bc+ad} + \frac{1}{a+bx}}{-\frac{d}{-bc+ad} + \frac{h}{-bg+ah}}} \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \left(-\frac{h}{-bg+ah} + \frac{1}{a+bx}\right) \right)$$

$$\text{EllipticF}\left[\text{ArcSin}\left[\sqrt{\frac{(-be+af) \left(-h - \frac{bg}{a+bx} + \frac{ah}{a+bx}\right)}{b(-fg+eh)}}\right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)}\right] \Big/$$

$$\left( \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{\frac{f}{-be+af} - \frac{h}{-bg+ah}}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right) \left(h + \frac{bg-ah}{a+bx}\right)} \right) \Bigg)$$

**Problem 25: Result more than twice size of optimal antiderivative.**

$$\int \frac{abB - a^2C + b^2Bx + b^2Cx^2}{(a+bx)^{7/2} \sqrt{c+dx} \sqrt{e+fx} \sqrt{g+hx}} dx$$

Optimal (type 4, 1128 leaves, 9 steps):

$$\begin{aligned}
 & \left( 2bd(9a^3Cdfh - b^3(2Bdeg - c(3Ceg - 2Bfg - 2Beh))) + ab^2 \right. \\
 & \quad \left. (C(deg + cfg + ceh) + 4B(dfg + deh + cfh)) - a^2b(6Bdfh + 5C(dfg + deh + cfh))) \right) \\
 & \quad \sqrt{a+bx} \sqrt{e+fx} \sqrt{g+hx} \Big/ \left( 3(bc-ad)^2 (be-af)^2 (bg-ah)^2 \sqrt{c+dx} \right) - \\
 & \quad \frac{2b^2(bB - 2aC) \sqrt{c+dx} \sqrt{e+fx} \sqrt{g+hx}}{3(bc-ad)(be-af)(bg-ah)(a+bx)^{3/2}} - \\
 & \left( 2b^2(9a^3Cdfh - b^3(2Bdeg - c(3Ceg - 2Bfg - 2Beh))) + ab^2 \right. \\
 & \quad \left. (C(deg + cfg + ceh) + 4B(dfg + deh + cfh)) - a^2b(6Bdfh + 5C(dfg + deh + cfh))) \right) \\
 & \quad \sqrt{c+dx} \sqrt{e+fx} \sqrt{g+hx} \Big/ \left( 3(bc-ad)^2 (be-af)^2 (bg-ah)^2 \sqrt{a+bx} \right) - \\
 & \left( 2b\sqrt{dg-ch} \sqrt{fg-eh} (9a^3Cdfh - b^3(2Bdeg - c(3Ceg - 2Bfg - 2Beh))) + \right. \\
 & \quad \left. ab^2(C(deg + cfg + ceh) + 4B(dfg + deh + cfh)) - \right. \\
 & \quad \left. a^2b(6Bdfh + 5C(dfg + deh + cfh))) \sqrt{a+bx} \sqrt{-\frac{(de-cf)(g+hx)}{(fg-eh)(c+dx)}} \right. \\
 & \quad \left. \text{EllipticE}\left[\text{ArcSin}\left[\frac{\sqrt{dg-ch} \sqrt{e+fx}}{\sqrt{fg-eh} \sqrt{c+dx}}\right], \frac{(bc-ad)(fg-eh)}{(be-af)(dg-ch)}\right] \right) \Big/ \\
 & \left( 3(bc-ad)^2 (be-af)^2 (bg-ah)^2 \sqrt{\frac{(de-cf)(a+bx)}{(be-af)(c+dx)}} \sqrt{g+hx} \right) - \\
 & \left( 2(3a^3C^2dfh - b^3(2Bd^2eg - Bc^2fh - cd(3Ceg - Bfg - Beh))) - \right. \\
 & \quad \left. 3a^2bd(Bdfh + C(dfg + deh - cfh)) + \right. \\
 & \quad \left. ab^2(3Bd^2(fg+eh) + C(d^2eg - cd fg - cdeh - 2c^2fh))) \sqrt{\frac{(be-af)(c+dx)}{(de-cf)(a+bx)}} \right. \\
 & \quad \left. \sqrt{g+hx} \text{EllipticF}\left[\text{ArcSin}\left[\frac{\sqrt{bg-ah} \sqrt{e+fx}}{\sqrt{fg-eh} \sqrt{a+bx}}\right], -\frac{(bc-ad)(fg-eh)}{(de-cf)(bg-ah)}\right] \right) \Big/ \\
 & \left( 3(bc-ad)^2 (be-af)(bg-ah)^{3/2} \sqrt{fg-eh} \sqrt{c+dx} \sqrt{-\frac{(be-af)(g+hx)}{(fg-eh)(a+bx)}} \right)
 \end{aligned}$$

Result (type 4, 10645 leaves):

$$\begin{aligned}
 & \sqrt{a+bx} \sqrt{c+dx} \sqrt{e+fx} \sqrt{g+hx} \\
 & \left( -\frac{2b^2(bB - 2aC)}{3(bc-ad)(be-af)(bg-ah)(a+bx)^2} - (2b^2(3b^3cCeg - 2b^3Bdeg + ab^2Cdeg - \right. \\
 & \quad \left. 2b^3Bcfg + ab^2ccfg + 4ab^2Bdfg - 5a^2bcdfg - 2b^3Bceh + ab^2cCeh + \right. \\
 & \quad \left. 4ab^2Bdeh - 5a^2bcdeh + 4ab^2Bcfh - 5a^2bccfh - 6a^2bBdfh + 9a^3Cdfh)) \Big/
 \end{aligned}$$

$$\begin{aligned}
 & \left( 3 (bc - ad)^2 (be - af)^2 (bg - ah)^2 (a + bx) \right) - \\
 & \frac{1}{3b (-bc + ad)^2 (-be + af)^2 (-bg + ah)^2} \\
 & 2 \left( \left( (-3b^3 c C e g + 2b^3 B d e g - ab^2 C d e g + 2b^3 B c f g - ab^2 c C f g - \right. \right. \\
 & \quad \left. \left. 4ab^2 B d f g + 5a^2 b C d f g + 2b^3 B c e h - ab^2 c C e h - 4ab^2 B d e h + \right. \right. \\
 & \quad \left. \left. 5a^2 b C d e h - 4ab^2 B c f h + 5a^2 b c C f h + 6a^2 b B d f h - 9a^3 C d f h \right) \right) / \\
 & \left( (a + bx)^{5/2} \left( d + \frac{bc}{a + bx} - \frac{ad}{a + bx} \right) \left( f + \frac{be}{a + bx} - \frac{af}{a + bx} \right) \left( h + \frac{bg}{a + bx} - \frac{ah}{a + bx} \right) \right) / \\
 & \left( \sqrt{c + \frac{(a + bx) \left( d - \frac{ad}{a + bx} \right)}{b}} \sqrt{e + \frac{(a + bx) \left( f - \frac{af}{a + bx} \right)}{b}} \sqrt{g + \frac{(a + bx) \left( h - \frac{ah}{a + bx} \right)}{b}} \right) - \\
 & \frac{1}{\sqrt{c + \frac{(a + bx) \left( d - \frac{ad}{a + bx} \right)}{b}} \sqrt{e + \frac{(a + bx) \left( f - \frac{af}{a + bx} \right)}{b}} \sqrt{g + \frac{(a + bx) \left( h - \frac{ah}{a + bx} \right)}{b}}} (bc - ad) (be - af) \\
 & (bg - ah) (a + bx)^{3/2} \sqrt{\left( \left( d + \frac{bc}{a + bx} - \frac{ad}{a + bx} \right) \left( f + \frac{be}{a + bx} - \frac{af}{a + bx} \right) \left( h + \frac{bg}{a + bx} - \frac{ah}{a + bx} \right) \right)} \\
 & \left( - \left( \left( 3b^3 c C e g \sqrt{\frac{(bc - ad) (bg - ah) \left( -\frac{d}{-bc + ad} + \frac{1}{a + bx} \right)}{bdg - bch}} \right. \right. \right. \\
 & \quad \left. \left. \left( -\frac{f}{-be + af} + \frac{1}{a + bx} \right) \sqrt{\frac{-\frac{h}{-bg + ah} + \frac{1}{a + bx}}{\frac{f}{-be + af} - \frac{h}{-bg + ah}}} \left( - \left( \left( (bdg - bch) \text{EllipticE} \left[ \right. \right. \right. \right. \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \text{ArcSin} \left[ \sqrt{\frac{(be - af) \left( h + \frac{bg}{a + bx} - \frac{ah}{a + bx} \right)}{b (-fg + eh)}} \right], \frac{(-bc + ad) (-fg + eh)}{(-be + af) (-dg + ch)} \right] \right) \right) \right) / \\
 & \left( (bc - ad) (bg - ah) \right) - \frac{1}{-bc + ad} d \text{EllipticF} \left[ \text{ArcSin} \left[ \right. \right. \\
 & \quad \left. \left. \sqrt{\frac{(be - af) \left( h + \frac{bg}{a + bx} - \frac{ah}{a + bx} \right)}{b (-fg + eh)}} \right], \frac{(-bc + ad) (-fg + eh)}{(-be + af) (-dg + ch)} \right] \right) /
 \end{aligned}$$

$$\begin{aligned}
 & \left( \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right) \left(h + \frac{bg-ah}{a+bx}\right)} \right) + \\
 & \left( 2b^3 Bdeg \sqrt{\frac{(bc-ad)(bg-ah) \left(-\frac{d}{-bc+ad} + \frac{1}{a+bx}\right)}{bdg-bch}} \left(-\frac{f}{-be+af} + \frac{1}{a+bx}\right) \right. \\
 & \left. \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{\frac{f}{-be+af} - \frac{h}{-bg+ah}}} \left( - \left( (bdg-bch) \text{EllipticE} \left[ \right. \right. \right. \right. \\
 & \left. \left. \left. \left. \text{ArcSin} \left[ \sqrt{\frac{(be-af) \left(h + \frac{bg}{a+bx} - \frac{ah}{a+bx}\right)}{b(-fg+eh)}} \right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right) \right) \right) / \\
 & \left( (bc-ad)(bg-ah) \right) - \frac{1}{-bc+ad} d \text{EllipticF} \left[ \text{ArcSin} \left[ \right. \right. \right. \\
 & \left. \left. \left. \sqrt{\frac{(be-af) \left(h + \frac{bg}{a+bx} - \frac{ah}{a+bx}\right)}{b(-fg+eh)}} \right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right) / \\
 & \left( \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right) \left(h + \frac{bg-ah}{a+bx}\right)} \right) - \\
 & \left( ab^2 Cdeg \sqrt{\frac{(bc-ad)(bg-ah) \left(-\frac{d}{-bc+ad} + \frac{1}{a+bx}\right)}{bdg-bch}} \left(-\frac{f}{-be+af} + \frac{1}{a+bx}\right) \right. \\
 & \left. \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{\frac{f}{-be+af} - \frac{h}{-bg+ah}}} \left( - \left( (bdg-bch) \text{EllipticE} \left[ \right. \right. \right. \right. \\
 & \left. \left. \left. \left. \text{ArcSin} \left[ \sqrt{\frac{(be-af) \left(h + \frac{bg}{a+bx} - \frac{ah}{a+bx}\right)}{b(-fg+eh)}} \right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right) \right) \right) / \\
 & \left( (bc-ad)(bg-ah) \right) - \frac{1}{-bc+ad} d \text{EllipticF} \left[ \text{ArcSin} \left[ \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left( \sqrt{\frac{(be-af) \left( h + \frac{bg}{a+bx} - \frac{ah}{a+bx} \right)}{b(-fg+eh)}}, \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right) / \\
 & \left( \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \sqrt{\left( d + \frac{bc-ad}{a+bx} \right) \left( f + \frac{be-af}{a+bx} \right) \left( h + \frac{bg-ah}{a+bx} \right)} \right) + \\
 & \left( 2b^3 B c f g \sqrt{\frac{(bc-ad)(bg-ah) \left( -\frac{d}{-bc+ad} + \frac{1}{a+bx} \right)}{bdg-bch}} \left( -\frac{f}{-be+af} + \frac{1}{a+bx} \right) \right. \\
 & \left. \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{\frac{f}{-be+af} - \frac{h}{-bg+ah}}} \left( \left( (bdg-bch) \text{EllipticE} \left[ \right. \right. \right. \right. \\
 & \left. \left. \left. \left. \text{ArcSin} \left[ \sqrt{\frac{(be-af) \left( h + \frac{bg}{a+bx} - \frac{ah}{a+bx} \right)}{b(-fg+eh)}}, \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right) \right) \right) / \\
 & \left( (bc-ad)(bg-ah) \right) \left. - \frac{1}{-bc+ad} d \text{EllipticF} \left[ \text{ArcSin} \left[ \right. \right. \right. \right. \right. \\
 & \left. \left. \left. \left. \sqrt{\frac{(be-af) \left( h + \frac{bg}{a+bx} - \frac{ah}{a+bx} \right)}{b(-fg+eh)}}, \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right) \right) \right) / \\
 & \left( \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \sqrt{\left( d + \frac{bc-ad}{a+bx} \right) \left( f + \frac{be-af}{a+bx} \right) \left( h + \frac{bg-ah}{a+bx} \right)} \right) - \\
 & \left( a b^2 c C f g \sqrt{\frac{(bc-ad)(bg-ah) \left( -\frac{d}{-bc+ad} + \frac{1}{a+bx} \right)}{bdg-bch}} \left( -\frac{f}{-be+af} + \frac{1}{a+bx} \right) \right. \\
 & \left. \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{\frac{f}{-be+af} - \frac{h}{-bg+ah}}} \left( \left( (bdg-bch) \text{EllipticE} \left[ \right. \right. \right. \right. \right. \\
 & \left. \left. \left. \left. \text{ArcSin} \left[ \sqrt{\frac{(be-af) \left( h + \frac{bg}{a+bx} - \frac{ah}{a+bx} \right)}{b(-fg+eh)}}, \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right) \right) \right) \right) /
 \end{aligned}$$

$$\begin{aligned}
 & \left. \left( (bc-ad)(bg-ah) \right) - \frac{1}{-bc+ad} d \operatorname{EllipticF} \left[ \operatorname{ArcSin} \left[ \sqrt{\frac{(be-af) \left( h + \frac{bg}{a+bx} - \frac{ah}{a+bx} \right)}{b(-fg+eh)}}, \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right] \right) / \\
 & \left( \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \sqrt{\left( d + \frac{bc-ad}{a+bx} \right) \left( f + \frac{be-af}{a+bx} \right) \left( h + \frac{bg-ah}{a+bx} \right)} \right) - \\
 & \left( 4ab^2 Bdfg \sqrt{\frac{(bc-ad)(bg-ah) \left( -\frac{d}{-bc+ad} + \frac{1}{a+bx} \right)}{bdg-bch}} \left( -\frac{f}{-be+af} + \frac{1}{a+bx} \right) \right. \\
 & \left. \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{\frac{f}{-be+af} - \frac{h}{-bg+ah}}} \left( \left( (bdg-bch) \operatorname{EllipticE} \left[ \operatorname{ArcSin} \left[ \sqrt{\frac{(be-af) \left( h + \frac{bg}{a+bx} - \frac{ah}{a+bx} \right)}{b(-fg+eh)}}, \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right] \right) \right) / \right. \\
 & \left. \left( (bc-ad)(bg-ah) \right) - \frac{1}{-bc+ad} d \operatorname{EllipticF} \left[ \operatorname{ArcSin} \left[ \sqrt{\frac{(be-af) \left( h + \frac{bg}{a+bx} - \frac{ah}{a+bx} \right)}{b(-fg+eh)}}, \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right] \right) / \\
 & \left( \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \sqrt{\left( d + \frac{bc-ad}{a+bx} \right) \left( f + \frac{be-af}{a+bx} \right) \left( h + \frac{bg-ah}{a+bx} \right)} \right) + \\
 & \left( 5a^2 bCd fg \sqrt{\frac{(bc-ad)(bg-ah) \left( -\frac{d}{-bc+ad} + \frac{1}{a+bx} \right)}{bdg-bch}} \left( -\frac{f}{-be+af} + \frac{1}{a+bx} \right) \right. \\
 & \left. \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{\frac{f}{-be+af} - \frac{h}{-bg+ah}}} \left( \left( (bdg-bch) \operatorname{EllipticE} \left[ \right. \right. \right) \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left. \text{ArcSin} \left[ \sqrt{\frac{(be-af) \left( h + \frac{bg}{a+bx} - \frac{ah}{a+bx} \right)}{b(-fg+eh)}}, \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right/ \\
 & \left. \left( (bc-ad)(bg-ah) \right) - \frac{1}{-bc+ad} d \text{EllipticF} \left[ \text{ArcSin} \left[ \sqrt{\frac{(be-af) \left( h + \frac{bg}{a+bx} - \frac{ah}{a+bx} \right)}{b(-fg+eh)}}, \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right] \right/ \\
 & \left( \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \sqrt{\left( d + \frac{bc-ad}{a+bx} \right) \left( f + \frac{be-af}{a+bx} \right) \left( h + \frac{bg-ah}{a+bx} \right)} \right) + \\
 & \left( 2b^3 C c e h \sqrt{\frac{(bc-ad)(bg-ah) \left( -\frac{d}{-bc+ad} + \frac{1}{a+bx} \right)}{bdg-bch}} \left( -\frac{f}{-be+af} + \frac{1}{a+bx} \right) \right. \\
 & \left. \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{\frac{f}{-be+af} - \frac{h}{-bg+ah}}} \left( - \left( (bdg-bch) \text{EllipticE} \left[ \right. \right. \right. \right. \right. \\
 & \left. \left. \left. \left. \left. \text{ArcSin} \left[ \sqrt{\frac{(be-af) \left( h + \frac{bg}{a+bx} - \frac{ah}{a+bx} \right)}{b(-fg+eh)}}, \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right] \right) \right) \right) \right/ \\
 & \left. \left( (bc-ad)(bg-ah) \right) - \frac{1}{-bc+ad} d \text{EllipticF} \left[ \text{ArcSin} \left[ \sqrt{\frac{(be-af) \left( h + \frac{bg}{a+bx} - \frac{ah}{a+bx} \right)}{b(-fg+eh)}}, \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right] \right) \right/ \\
 & \left( \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \sqrt{\left( d + \frac{bc-ad}{a+bx} \right) \left( f + \frac{be-af}{a+bx} \right) \left( h + \frac{bg-ah}{a+bx} \right)} \right) - \\
 & \left( ab^2 c c e h \sqrt{\frac{(bc-ad)(bg-ah) \left( -\frac{d}{-bc+ad} + \frac{1}{a+bx} \right)}{bdg-bch}} \left( -\frac{f}{-be+af} + \frac{1}{a+bx} \right) \right.
 \end{aligned}$$

$$\begin{aligned}
 & \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{-be+af} - \frac{h}{-bg+ah}} \left( - \left( (bdg - bch) \text{EllipticE} \left[ \right. \right. \right. \\
 & \quad \left. \left. \left. \text{ArcSin} \left[ \sqrt{\frac{(be-af) \left( h + \frac{bg}{a+bx} - \frac{ah}{a+bx} \right)}{b(-fg+eh)}} \right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right) / \right. \\
 & \quad \left. \left( (bc-ad)(bg-ah) \right) - \frac{1}{-bc+ad} d \text{EllipticF} \left[ \text{ArcSin} \left[ \right. \right. \right. \\
 & \quad \left. \left. \left. \sqrt{\frac{(be-af) \left( h + \frac{bg}{a+bx} - \frac{ah}{a+bx} \right)}{b(-fg+eh)}} \right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right) / \right. \\
 & \quad \left( \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-be+af} + \frac{1}{a+bx}} \sqrt{\left( d + \frac{bc-ad}{a+bx} \right) \left( f + \frac{be-af}{a+bx} \right) \left( h + \frac{bg-ah}{a+bx} \right)} \right) - \\
 & \quad \left( 4ab^2 Bdeh \sqrt{\frac{(bc-ad)(bg-ah) \left( -\frac{d}{-bc+ad} + \frac{1}{a+bx} \right)}{bdg-bch}} \left( -\frac{f}{-be+af} + \frac{1}{a+bx} \right) \right. \\
 & \quad \left. \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{-be+af} - \frac{h}{-bg+ah}} \left( - \left( (bdg - bch) \text{EllipticE} \left[ \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \text{ArcSin} \left[ \sqrt{\frac{(be-af) \left( h + \frac{bg}{a+bx} - \frac{ah}{a+bx} \right)}{b(-fg+eh)}} \right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right) / \right. \\
 & \quad \left. \left( (bc-ad)(bg-ah) \right) - \frac{1}{-bc+ad} d \text{EllipticF} \left[ \text{ArcSin} \left[ \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \sqrt{\frac{(be-af) \left( h + \frac{bg}{a+bx} - \frac{ah}{a+bx} \right)}{b(-fg+eh)}} \right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right) / \right. \\
 & \quad \left( \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-be+af} + \frac{1}{a+bx}} \sqrt{\left( d + \frac{bc-ad}{a+bx} \right) \left( f + \frac{be-af}{a+bx} \right) \left( h + \frac{bg-ah}{a+bx} \right)} \right) +
 \end{aligned}$$

$$\begin{aligned}
 & \left( 5 a^2 b c d e h \sqrt{\frac{(b c - a d) (b g - a h) \left(-\frac{d}{-b c + a d} + \frac{1}{a + b x}\right)}{b d g - b c h}} \left(-\frac{f}{-b e + a f} + \frac{1}{a + b x}\right) \right. \\
 & \left. \sqrt{\frac{-\frac{h}{-b g + a h} + \frac{1}{a + b x}}{\frac{f}{-b e + a f} - \frac{h}{-b g + a h}}} \left( \left( (b d g - b c h) \text{EllipticE} \left[ \right. \right. \right. \right. \\
 & \left. \left. \left. \left. \text{ArcSin} \left[ \sqrt{\frac{(b e - a f) \left(h + \frac{b g}{a + b x} - \frac{a h}{a + b x}\right)}{b (-f g + e h)} \right], \frac{(-b c + a d) (-f g + e h)}{(-b e + a f) (-d g + c h)} \right] \right) \right) \right) / \\
 & \left( (b c - a d) (b g - a h) \right) - \frac{1}{-b c + a d} d \text{EllipticF} \left[ \text{ArcSin} \left[ \right. \right. \\
 & \left. \left. \sqrt{\frac{(b e - a f) \left(h + \frac{b g}{a + b x} - \frac{a h}{a + b x}\right)}{b (-f g + e h)} \right], \frac{(-b c + a d) (-f g + e h)}{(-b e + a f) (-d g + c h)} \right] \right) / \\
 & \left( \sqrt{\frac{-\frac{f}{-b e + a f} + \frac{1}{a + b x}}{-\frac{f}{-b e + a f} + \frac{h}{-b g + a h}}} \sqrt{\left(d + \frac{b c - a d}{a + b x}\right) \left(f + \frac{b e - a f}{a + b x}\right) \left(h + \frac{b g - a h}{a + b x}\right)} \right) - \\
 & \left( 4 a b^2 B c f h \sqrt{\frac{(b c - a d) (b g - a h) \left(-\frac{d}{-b c + a d} + \frac{1}{a + b x}\right)}{b d g - b c h}} \left(-\frac{f}{-b e + a f} + \frac{1}{a + b x}\right) \right. \\
 & \left. \sqrt{\frac{-\frac{h}{-b g + a h} + \frac{1}{a + b x}}{\frac{f}{-b e + a f} - \frac{h}{-b g + a h}}} \left( \left( (b d g - b c h) \text{EllipticE} \left[ \right. \right. \right. \right. \\
 & \left. \left. \left. \left. \text{ArcSin} \left[ \sqrt{\frac{(b e - a f) \left(h + \frac{b g}{a + b x} - \frac{a h}{a + b x}\right)}{b (-f g + e h)} \right], \frac{(-b c + a d) (-f g + e h)}{(-b e + a f) (-d g + c h)} \right] \right) \right) \right) / \\
 & \left( (b c - a d) (b g - a h) \right) - \frac{1}{-b c + a d} d \text{EllipticF} \left[ \text{ArcSin} \left[ \right. \right. \\
 & \left. \left. \sqrt{\frac{(b e - a f) \left(h + \frac{b g}{a + b x} - \frac{a h}{a + b x}\right)}{b (-f g + e h)} \right], \frac{(-b c + a d) (-f g + e h)}{(-b e + a f) (-d g + c h)} \right] \right) /
 \end{aligned}$$

$$\begin{aligned}
 & \left( \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right) \left(h + \frac{bg-ah}{a+bx}\right)} \right) + \\
 & \left( 5a^2bcCfh \sqrt{\frac{(bc-ad)(bg-ah)\left(-\frac{d}{-bc+ad} + \frac{1}{a+bx}\right)}{bdg-bch}} \left(-\frac{f}{-be+af} + \frac{1}{a+bx}\right) \right. \\
 & \left. \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{-\frac{f}{-be+af} - \frac{h}{-bg+ah}}} \left( \left( (bdg-bch) \text{EllipticE} \left[ \right. \right. \right. \right. \\
 & \left. \left. \left. \left. \text{ArcSin} \left[ \sqrt{\frac{(be-af)\left(h + \frac{bg}{a+bx} - \frac{ah}{a+bx}\right)}{b(-fg+eh)}} \right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right) / \right. \right. \\
 & \left. \left. \left( (bc-ad)(bg-ah) \right) \right) - \frac{1}{-bc+ad} d \text{EllipticF} \left[ \text{ArcSin} \left[ \right. \right. \right. \right. \\
 & \left. \left. \left. \left. \sqrt{\frac{(be-af)\left(h + \frac{bg}{a+bx} - \frac{ah}{a+bx}\right)}{b(-fg+eh)}} \right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right) / \right. \\
 & \left. \left( \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right) \left(h + \frac{bg-ah}{a+bx}\right)} \right) + \\
 & \left( 6a^2bBdfh \sqrt{\frac{(bc-ad)(bg-ah)\left(-\frac{d}{-bc+ad} + \frac{1}{a+bx}\right)}{bdg-bch}} \left(-\frac{f}{-be+af} + \frac{1}{a+bx}\right) \right. \\
 & \left. \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{-\frac{f}{-be+af} - \frac{h}{-bg+ah}}} \left( \left( (bdg-bch) \text{EllipticE} \left[ \right. \right. \right. \right. \right. \\
 & \left. \left. \left. \left. \text{ArcSin} \left[ \sqrt{\frac{(be-af)\left(h + \frac{bg}{a+bx} - \frac{ah}{a+bx}\right)}{b(-fg+eh)}} \right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right) / \right. \\
 & \left. \left. \left( (bc-ad)(bg-ah) \right) \right) - \frac{1}{-bc+ad} d \text{EllipticF} \left[ \text{ArcSin} \left[ \right. \right. \right. \right.
 \end{aligned}$$

$$\left( \sqrt{\frac{(be-af) \left( h + \frac{bg}{a+bx} - \frac{ah}{a+bx} \right)}{b(-fg+eh)}} \right), \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \Bigg) /$$

$$\left( \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \sqrt{\left( d + \frac{bc-ad}{a+bx} \right) \left( f + \frac{be-af}{a+bx} \right) \left( h + \frac{bg-ah}{a+bx} \right)} \right) -$$

$$\left( 9a^3 C d f h \sqrt{\frac{(bc-ad)(bg-ah) \left( -\frac{d}{-bc+ad} + \frac{1}{a+bx} \right)}{bdg-bch}} \left( -\frac{f}{-be+af} + \frac{1}{a+bx} \right) \right.$$

$$\left. \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{\frac{f}{-be+af} - \frac{h}{-bg+ah}}} \left( \left( (bdg-bch) \text{EllipticE} \left[ \right. \right. \right. \right.$$

$$\left. \left. \left. \left. \text{ArcSin} \left[ \sqrt{\frac{(be-af) \left( h + \frac{bg}{a+bx} - \frac{ah}{a+bx} \right)}{b(-fg+eh)}} \right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right) \right) \right) /$$

$$\left( (bc-ad)(bg-ah) \right) \left. - \frac{1}{-bc+ad} d \text{EllipticF} \left[ \text{ArcSin} \left[ \right. \right. \right. \right.$$

$$\left. \left. \left. \left. \sqrt{\frac{(be-af) \left( h + \frac{bg}{a+bx} - \frac{ah}{a+bx} \right)}{b(-fg+eh)}} \right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right) \right) \Bigg) /$$

$$\left( \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \sqrt{\left( d + \frac{bc-ad}{a+bx} \right) \left( f + \frac{be-af}{a+bx} \right) \left( h + \frac{bg-ah}{a+bx} \right)} \right) +$$

$$\left( b^2 B d f g \sqrt{\frac{-\frac{d}{-bc+ad} + \frac{1}{a+bx}}{-\frac{d}{-bc+ad} + \frac{h}{-bg+ah}}} \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \left( -\frac{h}{-bg+ah} + \frac{1}{a+bx} \right) \right.$$

$$\left. \text{EllipticF} \left[ \text{ArcSin} \left[ \sqrt{\frac{(-be+af) \left( -h - \frac{bg}{a+bx} + \frac{ah}{a+bx} \right)}{b(-fg+eh)}} \right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right) \Bigg) /$$

$$\left( \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{\frac{f}{-be+af} - \frac{h}{-bg+ah}}} \sqrt{\left( d + \frac{bc-ad}{a+bx} \right) \left( f + \frac{be-af}{a+bx} \right) \left( h + \frac{bg-ah}{a+bx} \right)} \right) -$$

$$\begin{aligned}
 & \left( 2 a b C d f g \sqrt{\frac{-\frac{d}{-bc+ad} + \frac{1}{a+bx}}{-\frac{d}{-bc+ad} + \frac{h}{-bg+ah}}} \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \left( -\frac{h}{-bg+ah} + \frac{1}{a+bx} \right) \right. \\
 & \quad \left. \text{EllipticF}\left[\text{ArcSin}\left[\sqrt{\frac{(-be+af)\left(-h - \frac{bg}{a+bx} + \frac{ah}{a+bx}\right)}{b(-fg+eh)}}\right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)}\right] \right) / \\
 & \left( \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{\frac{f}{-be+af} - \frac{h}{-bg+ah}}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right) \left(h + \frac{bg-ah}{a+bx}\right)} \right) + \\
 & \left( b^2 B d e h \sqrt{\frac{-\frac{d}{-bc+ad} + \frac{1}{a+bx}}{-\frac{d}{-bc+ad} + \frac{h}{-bg+ah}}} \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \left( -\frac{h}{-bg+ah} + \frac{1}{a+bx} \right) \right. \\
 & \quad \left. \text{EllipticF}\left[\text{ArcSin}\left[\sqrt{\frac{(-be+af)\left(-h - \frac{bg}{a+bx} + \frac{ah}{a+bx}\right)}{b(-fg+eh)}}\right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)}\right] \right) / \\
 & \left( \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{\frac{f}{-be+af} - \frac{h}{-bg+ah}}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right) \left(h + \frac{bg-ah}{a+bx}\right)} \right) - \\
 & \left( 2 a b C d e h \sqrt{\frac{-\frac{d}{-bc+ad} + \frac{1}{a+bx}}{-\frac{d}{-bc+ad} + \frac{h}{-bg+ah}}} \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \left( -\frac{h}{-bg+ah} + \frac{1}{a+bx} \right) \right. \\
 & \quad \left. \text{EllipticF}\left[\text{ArcSin}\left[\sqrt{\frac{(-be+af)\left(-h - \frac{bg}{a+bx} + \frac{ah}{a+bx}\right)}{b(-fg+eh)}}\right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)}\right] \right) / \\
 & \left( \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{\frac{f}{-be+af} - \frac{h}{-bg+ah}}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right) \left(h + \frac{bg-ah}{a+bx}\right)} \right) + \\
 & \left( b^2 B c f h \sqrt{\frac{-\frac{d}{-bc+ad} + \frac{1}{a+bx}}{-\frac{d}{-bc+ad} + \frac{h}{-bg+ah}}} \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \left( -\frac{h}{-bg+ah} + \frac{1}{a+bx} \right) \right. \\
 & \quad \left. \text{EllipticF}\left[\text{ArcSin}\left[\sqrt{\frac{(-be+af)\left(-h - \frac{bg}{a+bx} + \frac{ah}{a+bx}\right)}{b(-fg+eh)}}\right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)}\right] \right) /
 \end{aligned}$$

$$\left( \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{\frac{f}{-be+af} - \frac{h}{-bg+ah}}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right) \left(h + \frac{bg-ah}{a+bx}\right)} \right) -$$

$$\left( 2abcCfh \sqrt{\frac{-\frac{d}{-bc+ad} + \frac{1}{a+bx}}{-\frac{d}{-bc+ad} + \frac{h}{-bg+ah}}} \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \left(-\frac{h}{-bg+ah} + \frac{1}{a+bx}\right) \right.$$

$$\left. \text{EllipticF}\left[\text{ArcSin}\left[\sqrt{\frac{(-be+af)\left(-h - \frac{bg}{a+bx} + \frac{ah}{a+bx}\right)}{b(-fg+eh)}}\right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)}\right] \right) /$$

$$\left( \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{\frac{f}{-be+af} - \frac{h}{-bg+ah}}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right) \left(h + \frac{bg-ah}{a+bx}\right)} \right) -$$

$$\left( 3abBdfh \sqrt{\frac{-\frac{d}{-bc+ad} + \frac{1}{a+bx}}{-\frac{d}{-bc+ad} + \frac{h}{-bg+ah}}} \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \left(-\frac{h}{-bg+ah} + \frac{1}{a+bx}\right) \right.$$

$$\left. \text{EllipticF}\left[\text{ArcSin}\left[\sqrt{\frac{(-be+af)\left(-h - \frac{bg}{a+bx} + \frac{ah}{a+bx}\right)}{b(-fg+eh)}}\right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)}\right] \right) /$$

$$\left( \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{\frac{f}{-be+af} - \frac{h}{-bg+ah}}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right) \left(h + \frac{bg-ah}{a+bx}\right)} \right) +$$

$$\left( 6a^2Cdfh \sqrt{\frac{-\frac{d}{-bc+ad} + \frac{1}{a+bx}}{-\frac{d}{-bc+ad} + \frac{h}{-bg+ah}}} \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \left(-\frac{h}{-bg+ah} + \frac{1}{a+bx}\right) \right.$$

$$\left. \text{EllipticF}\left[\text{ArcSin}\left[\sqrt{\frac{(-be+af)\left(-h - \frac{bg}{a+bx} + \frac{ah}{a+bx}\right)}{b(-fg+eh)}}\right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)}\right] \right) /$$

$$\left( \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{\frac{f}{-be+af} - \frac{h}{-bg+ah}}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right) \left(h + \frac{bg-ah}{a+bx}\right)} \right)$$

Problem 26: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \frac{(a+bx)^2 (A+Cx^2)}{\sqrt{c+dx} \sqrt{e+fx} \sqrt{g+hx}} dx$$

Optimal (type 4, 1097 leaves, 9 steps):

$$\begin{aligned} & \frac{1}{105 d^3 f^3 h^3} 2 (4C (2adfh - 3b(df g + de h + cf h)) (adfh - 2b(df g + de h + cf h)) + \\ & \quad 5bd f h (7Abdf h - C(5b(deg + cf g + ce h) + 2a(df g + de h + cf h)))) \\ & \quad \sqrt{c+dx} \sqrt{e+fx} \sqrt{g+hx} + \frac{1}{35 d^2 f^2 h^2} 4C (2adfh - 3b(df g + de h + cf h)) \\ & \quad (a+bx) \sqrt{c+dx} \sqrt{e+fx} \sqrt{g+hx} + \frac{2C(a+bx)^2 \sqrt{c+dx} \sqrt{e+fx} \sqrt{g+hx}}{7dfh} - \\ & \quad \frac{1}{105 d^4 f^{7/2} h^4 \sqrt{e+fx}} 4 \sqrt{-de+cf} (35 a^2 C d^2 f^2 h^2 (df g + de h + cf h) - \\ & \quad \sqrt{\frac{d(g+hx)}{dg-ch}} (7abd f h (15Ad^2 f^2 h^2 + C(8c^2 f^2 h^2 + 7cdf h (fg+eh) + d^2(8f^2 g^2 + 7efgh + 8e^2 h^2))) + \\ & \quad b^2 (35Ad^2 f^2 h^2 (df g + de h + cf h) + 2C(12c^3 f^3 h^3 + 10c^2 d f^2 h^2 (fg+eh) + \\ & \quad c d^2 f h (10f^2 g^2 + 9efgh + 10e^2 h^2) + 2d^3 (6f^3 g^3 + 5ef^2 g^2 h + 5e^2 f g h^2 + 6e^3 h^3)))))) \\ & \quad \sqrt{\frac{d(e+fx)}{de-cf}} \sqrt{g+hx} \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{f} \sqrt{c+dx}}{\sqrt{-de+cf}}\right], \frac{(de-cf)h}{f(dg-ch)}\right] + \\ & \quad \frac{1}{105 d^4 f^{7/2} h^4 \sqrt{e+fx} \sqrt{g+hx}} 2 \sqrt{-de+cf} \\ & \quad (35 a^2 d^2 f^2 h^2 (3Ad f h^2 + C(ch(fg-eh) + dg(2fg+eh))) - 14abd f h (15Ad^2 f^2 g h^2 + \\ & \quad C(4c^2 f h^2 (fg-eh) + cdh(3f^2 g^2 + efgh - 4e^2 h^2) + d^2 g(8f^2 g^2 + 3efgh + 4e^2 h^2))) + \\ & \quad b^2 (35Ad^2 f^2 h^2 (ch(fg-eh) + dg(2fg+eh)) + C(24c^3 f^2 h^3 (fg-eh) + \\ & \quad c^2 d f h^2 (17f^2 g^2 + 6efgh - 23e^2 h^2) + 2cd^2 h(8f^3 g^3 + ef^2 g^2 h + 3e^2 f g h^2 - 12e^3 h^3) + \\ & \quad d^3 g(48f^3 g^3 + 16ef^2 g^2 h + 17e^2 f g h^2 + 24e^3 h^3)))))) \\ & \quad \sqrt{\frac{d(e+fx)}{de-cf}} \sqrt{\frac{d(g+hx)}{dg-ch}} \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{f} \sqrt{c+dx}}{\sqrt{-de+cf}}\right], \frac{(de-cf)h}{f(dg-ch)}\right] \end{aligned}$$

Result (type 4, 18383 leaves):

$$\begin{aligned} & \sqrt{c+dx} \sqrt{e+fx} \sqrt{g+hx} \\ & \left( \frac{1}{105 d^3 f^3 h^3} 2 (24 b^2 C d^2 f^2 g^2 + 23 b^2 C d^2 e f g h + 23 b^2 C C d f^2 g h - 56 a b C d^2 f^2 g h + \right. \\ & \quad 24 b^2 C d^2 e^2 h^2 + 23 b^2 C C d e f h^2 - 56 a b C d^2 e f h^2 + \\ & \quad \left. 24 b^2 C^2 C f^2 h^2 - 56 a b C C d f^2 h^2 + 35 A b^2 d^2 f^2 h^2 + 35 a^2 C d^2 f^2 h^2) - \right. \\ & \quad \left. \frac{4 b C (3 b d f g + 3 b d e h + 3 b c f h - 7 a d f h) x}{35 d^2 f^2 h^2} + \frac{2 b^2 C x^2}{7 d f h} \right) + \\ & \quad \frac{1}{105 d^5 f^3 h^3} \left( \frac{1}{f h \sqrt{e + \frac{(c+dx)(f - \frac{cf}{c+dx})}{d}}} \sqrt{g + \frac{(c+dx)(h - \frac{ch}{c+dx})}{d}} \right) \end{aligned}$$

$$\begin{aligned}
 & 4 \left( -24 b^2 C d^3 f^3 g^3 - 20 b^2 C d^3 e f^2 g^2 h - 20 b^2 c C d^2 f^3 g^2 h + 56 a b C d^3 f^3 g^2 h - 20 b^2 C d^3 e^2 f g \right. \\
 & \quad h^2 - 18 b^2 c C d^2 e f^2 g h^2 + 49 a b C d^3 e f^2 g h^2 - 20 b^2 c^2 C d f^3 g h^2 + 49 a b c C d^2 f^3 g h^2 - \\
 & \quad 35 A b^2 d^3 f^3 g h^2 - 35 a^2 C d^3 f^3 g h^2 - 24 b^2 C d^3 e^3 h^3 - 20 b^2 c C d^2 e^2 f h^3 + 56 a b C d^3 e^2 f h^3 - \\
 & \quad 20 b^2 c^2 C d e f^2 h^3 + 49 a b c C d^2 e f^2 h^3 - 35 A b^2 d^3 e f^2 h^3 - 35 a^2 C d^3 e f^2 h^3 - \\
 & \quad \left. 24 b^2 c^3 C f^3 h^3 + 56 a b c^2 C d f^3 h^3 - 35 A b^2 c d^2 f^3 h^3 - 35 a^2 c C d^2 f^3 h^3 + 105 a A b d^3 f^3 h^3 \right) \\
 & (c+dx)^{3/2} \left( f + \frac{de}{c+dx} - \frac{cf}{c+dx} \right) \left( h + \frac{dg}{c+dx} - \frac{ch}{c+dx} \right) + \\
 & \frac{1}{f h \sqrt{e + \frac{(c+dx)(f - \frac{cf}{c+dx})}{d}} \sqrt{g + \frac{(c+dx)(h - \frac{ch}{c+dx})}{d}}} 2 (c+dx) \\
 & \sqrt{\left( f + \frac{de}{c+dx} - \frac{cf}{c+dx} \right) \left( h + \frac{dg}{c+dx} - \frac{ch}{c+dx} \right)} \left( \left( 48 i b^2 C d^5 e f^3 g^4 h \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \right. \right. \\
 & \left. \left. \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \left[ \text{EllipticE} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] - \right. \right. \right. \\
 & \left. \left. \left. \text{EllipticF} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right] \right) \right) / \\
 & \left( \sqrt{-\frac{-de+cf}{f}} (-dg+ch) \sqrt{\left( f + \frac{de-cf}{c+dx} \right) \left( h + \frac{dg-ch}{c+dx} \right)} \right) - \left( 48 i b^2 c C d^4 \right. \\
 & \left. f^4 g^4 h \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \left( \text{EllipticE} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}} \right], \right. \right. \right. \\
 & \left. \left. \left. \frac{f(-dg+ch)}{(-de+cf)h} \right] - \text{EllipticF} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) \right) /
 \end{aligned}$$

$$\begin{aligned}
 & \left( \sqrt{-\frac{-de+cf}{f}} (-dg+ch) \sqrt{\left(f + \frac{de-cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} \right) + \left( 40 i b^2 c d^5 e^2 \right. \\
 & f^2 g^3 h^2 \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \left( \text{EllipticE} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}} \right], \right. \right. \\
 & \left. \left. \frac{f(-dg+ch)}{(-de+cf)h} \right] - \text{EllipticF} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) \Bigg/ \\
 & \left( \sqrt{-\frac{-de+cf}{f}} (-dg+ch) \sqrt{\left(f + \frac{de-cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} \right) - \left( 48 i b^2 c C d^4 \right. \\
 & e f^3 g^3 h^2 \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \left( \text{EllipticE} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}} \right], \right. \right. \\
 & \left. \left. \frac{f(-dg+ch)}{(-de+cf)h} \right] - \text{EllipticF} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) \Bigg/ \\
 & \left( \sqrt{-\frac{-de+cf}{f}} (-dg+ch) \sqrt{\left(f + \frac{de-cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} \right) - \left( 112 i a b C d^5 \right. \\
 & e f^3 g^3 h^2 \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \left( \text{EllipticE} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}} \right], \right. \right.
 \end{aligned}$$

$$\left. \left. \left. \frac{f(-dg+ch)}{(-de+cf)h} \right] - \text{EllipticF} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) \right) /$$

$$\left( \sqrt{-\frac{de+cf}{f}} (-dg+ch) \sqrt{\left(f + \frac{de-cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} \right) + \left( 8 i b^2 c^2 c d^3 \right.$$

$$f^4 g^3 h^2 \sqrt{1 - \frac{de+cf}{f(c+dx)}} \sqrt{1 - \frac{dg+ch}{h(c+dx)}} \left( \text{EllipticE} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \right. \right.$$

$$\left. \left. \left. \frac{f(-dg+ch)}{(-de+cf)h} \right] - \text{EllipticF} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) \right) /$$

$$\left( \sqrt{-\frac{de+cf}{f}} (-dg+ch) \sqrt{\left(f + \frac{de-cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} \right) +$$

$$\left( 112 i a b c c d^4 f^4 g^3 h^2 \sqrt{1 - \frac{de+cf}{f(c+dx)}} \sqrt{1 - \frac{dg+ch}{h(c+dx)}} \right.$$

$$\left( \text{EllipticE} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] - \right.$$

$$\left. \left. \left. \text{EllipticF} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) \right) /$$

$$\left( \sqrt{-\frac{de+cf}{f}} (-dg+ch) \sqrt{\left(f + \frac{de-cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} \right) +$$

$$\left( 40 i b^2 C d^5 e^3 f g^2 h^3 \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \right.$$

$$\left( \text{EllipticE}\left[ i \text{ArcSinh}\left[ \frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] - \right.$$

$$\left. \left. \text{EllipticF}\left[ i \text{ArcSinh}\left[ \frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) \right) /$$

$$\left( \sqrt{-\frac{-de+cf}{f}} (-dg+ch) \sqrt{\left(f + \frac{de-cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} \right) -$$

$$\left( 44 i b^2 c C d^4 e^2 f^2 g^2 h^3 \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \right.$$

$$\left( \text{EllipticE}\left[ i \text{ArcSinh}\left[ \frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] - \right.$$

$$\left. \left. \text{EllipticF}\left[ i \text{ArcSinh}\left[ \frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) \right) /$$

$$\left( \sqrt{-\frac{-de+cf}{f}} (-dg+ch) \sqrt{\left(f + \frac{de-cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} \right) -$$

$$\left( 98 i a b C d^5 e^2 f^2 g^2 h^3 \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \right.$$

$$\left( \text{EllipticE}\left[ i \text{ArcSinh}\left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] - \right.$$

$$\left. \text{EllipticF}\left[ i \text{ArcSinh}\left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) /$$

$$\left( \sqrt{-\frac{de+cf}{f}} (-dg+ch) \sqrt{\left( f + \frac{de-cf}{c+dx} \right) \left( h + \frac{dg-ch}{c+dx} \right)} \right) +$$

$$\left( 4 i b^2 c^2 C d^3 e f^3 g^2 h^3 \sqrt{1 - \frac{de+cf}{f(c+dx)}} \sqrt{1 - \frac{dg+ch}{h(c+dx)}} \right.$$

$$\left. \left( \text{EllipticE}\left[ i \text{ArcSinh}\left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] - \right.$$

$$\left. \text{EllipticF}\left[ i \text{ArcSinh}\left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) /$$

$$\left( \sqrt{-\frac{de+cf}{f}} (-dg+ch) \sqrt{\left( f + \frac{de-cf}{c+dx} \right) \left( h + \frac{dg-ch}{c+dx} \right)} \right) +$$

$$\left( 112 i a b c C d^4 e f^3 g^2 h^3 \sqrt{1 - \frac{de+cf}{f(c+dx)}} \sqrt{1 - \frac{dg+ch}{h(c+dx)}} \right.$$

$$\left. \left( \text{EllipticE}\left[ i \text{ArcSinh}\left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] - \right.$$

$$\left. \left( \text{EllipticF} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) \right) /$$

$$\left( \sqrt{-\frac{de+cf}{f}} (-dg+ch) \sqrt{\left(f + \frac{de-cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} \right) +$$

$$\left( 70 i A b^2 d^5 e f^3 g^2 h^3 \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \right)$$

$$\left( \text{EllipticE} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] - \right.$$

$$\left. \text{EllipticF} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) /$$

$$\left( \sqrt{-\frac{de+cf}{f}} (-dg+ch) \sqrt{\left(f + \frac{de-cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} \right) +$$

$$\left( 70 i a^2 C d^5 e f^3 g^2 h^3 \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \right)$$

$$\left( \text{EllipticE} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] - \right.$$

$$\left. \text{EllipticF} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) /$$

$$\left( \sqrt{-\frac{-de+cf}{f}} (-dg+ch) \sqrt{\left(f + \frac{de-cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} \right) -$$

$$\left( 14 i a b c^2 C d^3 f^4 g^2 h^3 \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \right.$$

$$\left( \text{EllipticE}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}}\right], \frac{f(-dg+ch)}{(-de+cf)h}\right] - \right.$$

$$\left. \left. \text{EllipticF}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}}\right], \frac{f(-dg+ch)}{(-de+cf)h}\right] \right) \right) /$$

$$\left( \sqrt{-\frac{-de+cf}{f}} (-dg+ch) \sqrt{\left(f + \frac{de-cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} \right) -$$

$$\left( 70 i A b^2 c d^4 f^4 g^2 h^3 \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \right.$$

$$\left( \text{EllipticE}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}}\right], \frac{f(-dg+ch)}{(-de+cf)h}\right] - \right.$$

$$\left. \left. \text{EllipticF}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}}\right], \frac{f(-dg+ch)}{(-de+cf)h}\right] \right) \right) /$$

$$\left( \sqrt{-\frac{-de+cf}{f}} (-dg+ch) \sqrt{\left(f + \frac{de-cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} \right) -$$

$$\left( 70 i a^2 c C d^4 f^4 g^2 h^3 \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \right.$$

$$\left( \text{EllipticE}\left[ i \text{ArcSinh}\left[ \frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] - \right.$$

$$\left. \left. \text{EllipticF}\left[ i \text{ArcSinh}\left[ \frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) \right) /$$

$$\left( \sqrt{-\frac{-de+cf}{f}} (-dg+ch) \sqrt{\left(f + \frac{de-cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} \right) +$$

$$\left( 48 i b^2 C d^5 e^4 g h^4 \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \right.$$

$$\left( \text{EllipticE}\left[ i \text{ArcSinh}\left[ \frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] - \right.$$

$$\left. \left. \text{EllipticF}\left[ i \text{ArcSinh}\left[ \frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) \right) /$$

$$\left( \sqrt{-\frac{-de+cf}{f}} (-dg+ch) \sqrt{\left(f + \frac{de-cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} \right) -$$

$$\left( 48 i b^2 c C d^4 e^3 f g h^4 \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \right.$$

$$\left( \left( \text{EllipticE} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] - \right. \right. \\ \left. \left. \text{EllipticF} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) \right) / \\ \left( \sqrt{-\frac{de+cf}{f}} (-dg+ch) \sqrt{\left( f + \frac{de-cf}{c+dx} \right) \left( h + \frac{dg-ch}{c+dx} \right)} \right) - \\ \left( 112 i a b c d^5 e^3 f g h^4 \sqrt{1 - \frac{de+cf}{f(c+dx)}} \sqrt{1 - \frac{dg+ch}{h(c+dx)}} \right. \\ \left. \left( \left( \text{EllipticE} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] - \right. \right. \right. \\ \left. \left. \left. \text{EllipticF} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) \right) \right) / \\ \left( \sqrt{-\frac{de+cf}{f}} (-dg+ch) \sqrt{\left( f + \frac{de-cf}{c+dx} \right) \left( h + \frac{dg-ch}{c+dx} \right)} \right) + \\ \left( 4 i b^2 c^2 C d^3 e^2 f^2 g h^4 \sqrt{1 - \frac{de+cf}{f(c+dx)}} \sqrt{1 - \frac{dg+ch}{h(c+dx)}} \right. \\ \left. \left( \left( \text{EllipticE} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] - \right. \right. \right.$$

$$\left( \left( \text{EllipticF}\left[ i \text{ArcSinh}\left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) \right) /$$

$$\left( \sqrt{-\frac{de+cf}{f}} (-dg+ch) \sqrt{\left(f + \frac{de-cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} \right) +$$

$$\left( 112 i a b c C d^4 e^2 f^2 g h^4 \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \right)$$

$$\left( \text{EllipticE}\left[ i \text{ArcSinh}\left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] - \right)$$

$$\left( \left( \text{EllipticF}\left[ i \text{ArcSinh}\left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) \right) /$$

$$\left( \sqrt{-\frac{de+cf}{f}} (-dg+ch) \sqrt{\left(f + \frac{de-cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} \right) +$$

$$\left( 70 i A b^2 d^5 e^2 f^2 g h^4 \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \right)$$

$$\left( \text{EllipticE}\left[ i \text{ArcSinh}\left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] - \right)$$

$$\left( \left( \text{EllipticF}\left[ i \text{ArcSinh}\left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) \right) /$$

$$\begin{aligned}
 & \left( \sqrt{-\frac{-de+cf}{f}} (-dg+ch) \sqrt{\left(f + \frac{de-cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} \right) + \\
 & \left( 70 i a^2 C d^5 e^2 f^2 g h^4 \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \right. \\
 & \left( \text{EllipticE}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}}\right], \frac{f(-dg+ch)}{(-de+cf)h}\right] - \right. \\
 & \left. \left. \text{EllipticF}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}}\right], \frac{f(-dg+ch)}{(-de+cf)h}\right] \right) \right) / \\
 & \left( \sqrt{-\frac{-de+cf}{f}} (-dg+ch) \sqrt{\left(f + \frac{de-cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} \right) + \\
 & \left( 4 i b^2 c^3 C d^2 e f^3 g h^4 \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \right. \\
 & \left( \text{EllipticE}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}}\right], \frac{f(-dg+ch)}{(-de+cf)h}\right] - \right. \\
 & \left. \left. \text{EllipticF}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}}\right], \frac{f(-dg+ch)}{(-de+cf)h}\right] \right) \right) / \\
 & \left( \sqrt{-\frac{-de+cf}{f}} (-dg+ch) \sqrt{\left(f + \frac{de-cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} \right) -
 \end{aligned}$$

$$\left( 14 i a b c^2 C d^3 e f^3 g h^4 \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \right.$$

$$\left( \text{EllipticE}\left[ i \text{ArcSinh}\left[ \frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] - \right.$$

$$\left. \left. \text{EllipticF}\left[ i \text{ArcSinh}\left[ \frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) \right) /$$

$$\left( \sqrt{-\frac{-de+cf}{f}} (-dg+ch) \sqrt{\left(f + \frac{de-cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} \right) -$$

$$\left( 70 i A b^2 c d^4 e f^3 g h^4 \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \right.$$

$$\left( \text{EllipticE}\left[ i \text{ArcSinh}\left[ \frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] - \right.$$

$$\left. \left. \text{EllipticF}\left[ i \text{ArcSinh}\left[ \frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) \right) /$$

$$\left( \sqrt{-\frac{-de+cf}{f}} (-dg+ch) \sqrt{\left(f + \frac{de-cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} \right) -$$

$$\left( 70 i a^2 c C d^4 e f^3 g h^4 \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \right.$$

$$\left( \left( \text{EllipticE} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] - \right. \right. \\ \left. \left. \text{EllipticF} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) \right) / \\ \left( \sqrt{-\frac{de+cf}{f}} (-dg+ch) \sqrt{\left( f + \frac{de-cf}{c+dx} \right) \left( h + \frac{dg-ch}{c+dx} \right)} \right) - \\ \left( 210 i a A b d^5 e f^3 g h^4 \sqrt{1 - \frac{de+cf}{f(c+dx)}} \sqrt{1 - \frac{dg+ch}{h(c+dx)}} \right) \\ \left( \left( \text{EllipticE} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] - \right. \right. \\ \left. \left. \text{EllipticF} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) \right) / \\ \left( \sqrt{-\frac{de+cf}{f}} (-dg+ch) \sqrt{\left( f + \frac{de-cf}{c+dx} \right) \left( h + \frac{dg-ch}{c+dx} \right)} \right) - \\ \left( 8 i b^2 c^4 C d f^4 g h^4 \sqrt{1 - \frac{de+cf}{f(c+dx)}} \sqrt{1 - \frac{dg+ch}{h(c+dx)}} \right) \\ \left( \left( \text{EllipticE} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] - \right. \right.$$

$$\left. \left( \text{EllipticF}\left[\text{i ArcSinh}\left[\frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}}\right], \frac{f(-dg+ch)}{(-de+cf)h}\right]\right) \right) /$$

$$\left( \sqrt{-\frac{de+cf}{f}} (-dg+ch) \sqrt{\left(f + \frac{de- cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} \right) +$$

$$\left( 14 \text{i a b c}^3 \text{C d}^2 \text{f}^4 \text{g h}^4 \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \right)$$

$$\left( \text{EllipticE}\left[\text{i ArcSinh}\left[\frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}}\right], \frac{f(-dg+ch)}{(-de+cf)h}\right] - \right.$$

$$\left. \text{EllipticF}\left[\text{i ArcSinh}\left[\frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}}\right], \frac{f(-dg+ch)}{(-de+cf)h}\right]\right) /$$

$$\left( \sqrt{-\frac{de+cf}{f}} (-dg+ch) \sqrt{\left(f + \frac{de- cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} \right) +$$

$$\left( 210 \text{i a A b c d}^4 \text{f}^4 \text{g h}^4 \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \right)$$

$$\left( \text{EllipticE}\left[\text{i ArcSinh}\left[\frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}}\right], \frac{f(-dg+ch)}{(-de+cf)h}\right] - \right.$$

$$\left. \text{EllipticF}\left[\text{i ArcSinh}\left[\frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}}\right], \frac{f(-dg+ch)}{(-de+cf)h}\right]\right) /$$

$$\begin{aligned}
 & \left( \sqrt{-\frac{-de+cf}{f}} (-dg+ch) \sqrt{\left(f + \frac{de-cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} \right) - \\
 & \left( 48 i b^2 c C d^4 e^4 h^5 \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \right. \\
 & \left( \text{EllipticE}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}}\right], \frac{f(-dg+ch)}{(-de+cf)h}\right] - \right. \\
 & \left. \left. \text{EllipticF}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}}\right], \frac{f(-dg+ch)}{(-de+cf)h}\right] \right) \right) / \\
 & \left( \sqrt{-\frac{-de+cf}{f}} (-dg+ch) \sqrt{\left(f + \frac{de-cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} \right) + \\
 & \left( 8 i b^2 c^2 C d^3 e^3 f h^5 \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \right. \\
 & \left( \text{EllipticE}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}}\right], \frac{f(-dg+ch)}{(-de+cf)h}\right] - \right. \\
 & \left. \left. \text{EllipticF}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}}\right], \frac{f(-dg+ch)}{(-de+cf)h}\right] \right) \right) / \\
 & \left( \sqrt{-\frac{-de+cf}{f}} (-dg+ch) \sqrt{\left(f + \frac{de-cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} \right) +
 \end{aligned}$$

$$\left( 112 i a b c C d^4 e^3 f h^5 \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \right.$$

$$\left( \text{EllipticE}\left[ i \text{ArcSinh}\left[ \frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] - \right.$$

$$\left. \left. \text{EllipticF}\left[ i \text{ArcSinh}\left[ \frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) \right) /$$

$$\left( \sqrt{-\frac{-de+cf}{f}} (-dg+ch) \sqrt{\left(f + \frac{de-cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} \right) -$$

$$\left( 14 i a b c^2 C d^3 e^2 f^2 h^5 \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \right.$$

$$\left( \text{EllipticE}\left[ i \text{ArcSinh}\left[ \frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] - \right.$$

$$\left. \left. \text{EllipticF}\left[ i \text{ArcSinh}\left[ \frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) \right) /$$

$$\left( \sqrt{-\frac{-de+cf}{f}} (-dg+ch) \sqrt{\left(f + \frac{de-cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} \right) -$$

$$\left( 70 i A b^2 c d^4 e^2 f^2 h^5 \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \right.$$

$$\left( \begin{aligned} & \left( \text{EllipticE} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] - \right. \\ & \left. \left. \text{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) \right) / \\ & \left( \sqrt{-\frac{de+cf}{f}} (-dg+ch) \sqrt{\left(f + \frac{de- cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} \right) - \\ & \left( 70 i a^2 c C d^4 e^2 f^2 h^5 \sqrt{1 - \frac{de+cf}{f(c+dx)}} \sqrt{1 - \frac{dg+ch}{h(c+dx)}} \right. \\ & \left( \text{EllipticE} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] - \right. \\ & \left. \left. \text{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) \right) / \\ & \left( \sqrt{-\frac{de+cf}{f}} (-dg+ch) \sqrt{\left(f + \frac{de- cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} \right) - \\ & \left( 8 i b^2 c^4 C d e f^3 h^5 \sqrt{1 - \frac{de+cf}{f(c+dx)}} \sqrt{1 - \frac{dg+ch}{h(c+dx)}} \right. \\ & \left( \text{EllipticE} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] - \right. \end{aligned} \right)$$

$$\left. \left( \text{EllipticF}\left[ i \text{ArcSinh}\left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) \right) /$$

$$\left( \sqrt{-\frac{de+cf}{f}} (-dg+ch) \sqrt{\left(f + \frac{de- cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} \right) +$$

$$\left( 14 i a b c^3 C d^2 e f^3 h^5 \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \right)$$

$$\left( \text{EllipticE}\left[ i \text{ArcSinh}\left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] - \right.$$

$$\left. \text{EllipticF}\left[ i \text{ArcSinh}\left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) /$$

$$\left( \sqrt{-\frac{de+cf}{f}} (-dg+ch) \sqrt{\left(f + \frac{de- cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} \right) +$$

$$\left( 210 i a A b c d^4 e f^3 h^5 \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \right)$$

$$\left( \text{EllipticE}\left[ i \text{ArcSinh}\left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] - \right.$$

$$\left. \text{EllipticF}\left[ i \text{ArcSinh}\left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) /$$

$$\begin{aligned}
 & \left( \sqrt{-\frac{-de+cf}{f}} (-dg+ch) \sqrt{\left(f+\frac{de-cf}{c+dx}\right) \left(h+\frac{dg-ch}{c+dx}\right)} \right) + \\
 & \left( 48 i b^2 c^5 C f^4 h^5 \sqrt{1-\frac{-de+cf}{f(c+dx)}} \sqrt{1-\frac{-dg+ch}{h(c+dx)}} \left( \text{EllipticE}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}}\right], \right. \right. \right. \\
 & \left. \left. \left. \frac{f(-dg+ch)}{(-de+cf)h}\right] - \text{EllipticF}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}}\right], \frac{f(-dg+ch)}{(-de+cf)h}\right] \right) \right) / \\
 & \left( \sqrt{-\frac{-de+cf}{f}} (-dg+ch) \sqrt{\left(f+\frac{de-cf}{c+dx}\right) \left(h+\frac{dg-ch}{c+dx}\right)} \right) - \\
 & \left( 112 i a b c^4 C d f^4 h^5 \sqrt{1-\frac{-de+cf}{f(c+dx)}} \sqrt{1-\frac{-dg+ch}{h(c+dx)}} \right. \\
 & \left. \left( \text{EllipticE}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}}\right], \frac{f(-dg+ch)}{(-de+cf)h}\right] - \right. \right. \\
 & \left. \left. \text{EllipticF}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}}\right], \frac{f(-dg+ch)}{(-de+cf)h}\right] \right) \right) / \\
 & \left( \sqrt{-\frac{-de+cf}{f}} (-dg+ch) \sqrt{\left(f+\frac{de-cf}{c+dx}\right) \left(h+\frac{dg-ch}{c+dx}\right)} \right) + \\
 & \left( 70 i A b^2 c^3 d^2 f^4 h^5 \sqrt{1-\frac{-de+cf}{f(c+dx)}} \sqrt{1-\frac{-dg+ch}{h(c+dx)}} \right.
 \end{aligned}$$

$$\left( \text{EllipticE} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] - \right. \\
 \left. \text{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) / \\
 \left( \sqrt{-\frac{de+cf}{f}} (-dg+ch) \sqrt{\left(f + \frac{de-cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} \right) + \\
 \left( 70 i a^2 c^3 C d^2 f^4 h^5 \sqrt{1 - \frac{de+cf}{f(c+dx)}} \sqrt{1 - \frac{dg+ch}{h(c+dx)}} \right) \\
 \left( \text{EllipticE} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] - \right. \\
 \left. \text{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) / \\
 \left( \sqrt{-\frac{de+cf}{f}} (-dg+ch) \sqrt{\left(f + \frac{de-cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} \right) - \\
 \left( 210 i a A b c^2 d^3 f^4 h^5 \sqrt{1 - \frac{de+cf}{f(c+dx)}} \sqrt{1 - \frac{dg+ch}{h(c+dx)}} \right) \\
 \left( \text{EllipticE} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] - \right.$$

$$\left. \left( \text{EllipticF} \left[ \text{i ArcSinh} \left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) \right) /$$

$$\left( \sqrt{-\frac{de+cf}{f}} (-dg+ch) \sqrt{\left(f + \frac{de- cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} \right) -$$

$$\left( 24 \text{i} b^2 C d^4 e f^3 g^3 h \sqrt{1 - \frac{de+cf}{f(c+dx)}} \sqrt{1 - \frac{dg+ch}{h(c+dx)}} \right)$$

$$\left. \left( \text{EllipticF} \left[ \text{i ArcSinh} \left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) \right) /$$

$$\left( \sqrt{-\frac{de+cf}{f}} \sqrt{\left(f + \frac{de- cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} \right) +$$

$$\left( 24 \text{i} b^2 c C d^3 f^4 g^3 h \sqrt{1 - \frac{de+cf}{f(c+dx)}} \sqrt{1 - \frac{dg+ch}{h(c+dx)}} \right)$$

$$\left. \left( \text{EllipticF} \left[ \text{i ArcSinh} \left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) \right) /$$

$$\left( \sqrt{-\frac{de+cf}{f}} \sqrt{\left(f + \frac{de- cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} \right) -$$

$$\left( 23 \text{i} b^2 C d^4 e^2 f^2 g^2 h^2 \sqrt{1 - \frac{de+cf}{f(c+dx)}} \sqrt{1 - \frac{dg+ch}{h(c+dx)}} \right)$$

$$\begin{aligned}
 & \left( \text{EllipticF} \left[ \text{i ArcSinh} \left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) / \\
 & \left( \sqrt{-\frac{de+cf}{f}} \sqrt{\left( f + \frac{de-cf}{c+dx} \right) \left( h + \frac{dg-ch}{c+dx} \right)} \right) + \\
 & \left( 6 \text{i} b^2 c C d^3 e f^3 g^2 h^2 \sqrt{1 - \frac{de+cf}{f(c+dx)}} \sqrt{1 - \frac{dg+ch}{h(c+dx)}} \right) \\
 & \left( \text{EllipticF} \left[ \text{i ArcSinh} \left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) / \\
 & \left( \sqrt{-\frac{de+cf}{f}} \sqrt{\left( f + \frac{de-cf}{c+dx} \right) \left( h + \frac{dg-ch}{c+dx} \right)} \right) + \\
 & \left( 56 \text{i} a b C d^4 e f^3 g^2 h^2 \sqrt{1 - \frac{de+cf}{f(c+dx)}} \sqrt{1 - \frac{dg+ch}{h(c+dx)}} \right) \\
 & \left( \text{EllipticF} \left[ \text{i ArcSinh} \left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) / \\
 & \left( \sqrt{-\frac{de+cf}{f}} \sqrt{\left( f + \frac{de-cf}{c+dx} \right) \left( h + \frac{dg-ch}{c+dx} \right)} \right) + \\
 & \left( 17 \text{i} b^2 c^2 C d^2 f^4 g^2 h^2 \sqrt{1 - \frac{de+cf}{f(c+dx)}} \sqrt{1 - \frac{dg+ch}{h(c+dx)}} \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left( \text{EllipticF} \left[ \text{i ArcSinh} \left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) / \\
 & \left( \sqrt{-\frac{de+cf}{f}} \sqrt{\left(f + \frac{de-cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} \right) - \\
 & \left( 56 \text{i} a b c C d^3 f^4 g^2 h^2 \sqrt{1 - \frac{de+cf}{f(c+dx)}} \sqrt{1 - \frac{dg+ch}{h(c+dx)}} \right) \\
 & \left( \text{EllipticF} \left[ \text{i ArcSinh} \left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) / \\
 & \left( \sqrt{-\frac{de+cf}{f}} \sqrt{\left(f + \frac{de-cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} \right) - \\
 & \left( 24 \text{i} b^2 C d^4 e^3 f g h^3 \sqrt{1 - \frac{de+cf}{f(c+dx)}} \sqrt{1 - \frac{dg+ch}{h(c+dx)}} \right) \\
 & \left( \text{EllipticF} \left[ \text{i ArcSinh} \left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) / \\
 & \left( \sqrt{-\frac{de+cf}{f}} \sqrt{\left(f + \frac{de-cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} \right) + \\
 & \left( 6 \text{i} b^2 c C d^3 e^2 f^2 g h^3 \sqrt{1 - \frac{de+cf}{f(c+dx)}} \sqrt{1 - \frac{dg+ch}{h(c+dx)}} \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left( \text{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) / \\
 & \left( \sqrt{-\frac{de+cf}{f}} \sqrt{\left( f + \frac{de-cf}{c+dx} \right) \left( h + \frac{dg-ch}{c+dx} \right)} \right) + \\
 & \left( 56 i a b C d^4 e^2 f^2 g h^3 \sqrt{1 - \frac{de+cf}{f(c+dx)}} \sqrt{1 - \frac{dg+ch}{h(c+dx)}} \right) \\
 & \left( \text{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) / \\
 & \left( \sqrt{-\frac{de+cf}{f}} \sqrt{\left( f + \frac{de-cf}{c+dx} \right) \left( h + \frac{dg-ch}{c+dx} \right)} \right) + \\
 & \left( 2 i b^2 c^2 C d^2 e f^3 g h^3 \sqrt{1 - \frac{de+cf}{f(c+dx)}} \sqrt{1 - \frac{dg+ch}{h(c+dx)}} \right) \\
 & \left( \text{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) / \\
 & \left( \sqrt{-\frac{de+cf}{f}} \sqrt{\left( f + \frac{de-cf}{c+dx} \right) \left( h + \frac{dg-ch}{c+dx} \right)} \right) - \\
 & \left( 14 i a b c C d^3 e f^3 g h^3 \sqrt{1 - \frac{de+cf}{f(c+dx)}} \sqrt{1 - \frac{dg+ch}{h(c+dx)}} \right)
 \end{aligned}$$

$$\left( \text{EllipticF} \left[ \text{i ArcSinh} \left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) /$$

$$\left( \sqrt{-\frac{de+cf}{f}} \sqrt{\left(f + \frac{de-cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} \right) -$$

$$\left( 35 \text{i Ab}^2 d^4 e f^3 g h^3 \sqrt{1 - \frac{de+cf}{f(c+dx)}} \sqrt{1 - \frac{dg+ch}{h(c+dx)}} \right)$$

$$\left( \text{EllipticF} \left[ \text{i ArcSinh} \left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) /$$

$$\left( \sqrt{-\frac{de+cf}{f}} \sqrt{\left(f + \frac{de-cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} \right) -$$

$$\left( 35 \text{i a}^2 C d^4 e f^3 g h^3 \sqrt{1 - \frac{de+cf}{f(c+dx)}} \sqrt{1 - \frac{dg+ch}{h(c+dx)}} \right)$$

$$\left( \text{EllipticF} \left[ \text{i ArcSinh} \left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) /$$

$$\left( \sqrt{-\frac{de+cf}{f}} \sqrt{\left(f + \frac{de-cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} \right) +$$

$$\left( 16 \text{i b}^2 c^3 C d f^4 g h^3 \sqrt{1 - \frac{de+cf}{f(c+dx)}} \sqrt{1 - \frac{dg+ch}{h(c+dx)}} \right)$$

$$\begin{aligned}
 & \left( \text{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) / \\
 & \left( \sqrt{-\frac{de+cf}{f}} \sqrt{\left( f + \frac{de-cf}{c+dx} \right) \left( h + \frac{dg-ch}{c+dx} \right)} \right) - \\
 & \left( 42 i a b c^2 C d^2 f^4 g h^3 \sqrt{1 - \frac{de+cf}{f(c+dx)}} \sqrt{1 - \frac{dg+ch}{h(c+dx)}} \right) \\
 & \left( \text{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) / \\
 & \left( \sqrt{-\frac{de+cf}{f}} \sqrt{\left( f + \frac{de-cf}{c+dx} \right) \left( h + \frac{dg-ch}{c+dx} \right)} \right) + \\
 & \left( 35 i A b^2 c d^3 f^4 g h^3 \sqrt{1 - \frac{de+cf}{f(c+dx)}} \sqrt{1 - \frac{dg+ch}{h(c+dx)}} \right) \\
 & \left( \text{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) / \\
 & \left( \sqrt{-\frac{de+cf}{f}} \sqrt{\left( f + \frac{de-cf}{c+dx} \right) \left( h + \frac{dg-ch}{c+dx} \right)} \right) + \\
 & \left( 35 i a^2 c C d^3 f^4 g h^3 \sqrt{1 - \frac{de+cf}{f(c+dx)}} \sqrt{1 - \frac{dg+ch}{h(c+dx)}} \right)
 \end{aligned}$$

$$\left( \text{EllipticF} \left[ \text{i ArcSinh} \left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) /$$

$$\left( \sqrt{-\frac{de+cf}{f}} \sqrt{\left( f + \frac{de-cf}{c+dx} \right) \left( h + \frac{dg-ch}{c+dx} \right)} \right) +$$

$$\left( 24 \text{i} b^2 c C d^3 e^3 f h^4 \sqrt{1 - \frac{de+cf}{f(c+dx)}} \sqrt{1 - \frac{dg+ch}{h(c+dx)}} \right)$$

$$\left( \text{EllipticF} \left[ \text{i ArcSinh} \left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) /$$

$$\left( \sqrt{-\frac{de+cf}{f}} \sqrt{\left( f + \frac{de-cf}{c+dx} \right) \left( h + \frac{dg-ch}{c+dx} \right)} \right) +$$

$$\left( 17 \text{i} b^2 c^2 C d^2 e^2 f^2 h^4 \sqrt{1 - \frac{de+cf}{f(c+dx)}} \sqrt{1 - \frac{dg+ch}{h(c+dx)}} \right)$$

$$\left( \text{EllipticF} \left[ \text{i ArcSinh} \left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) /$$

$$\left( \sqrt{-\frac{de+cf}{f}} \sqrt{\left( f + \frac{de-cf}{c+dx} \right) \left( h + \frac{dg-ch}{c+dx} \right)} \right) -$$

$$\left( 56 \text{i} a b c C d^3 e^2 f^2 h^4 \sqrt{1 - \frac{de+cf}{f(c+dx)}} \sqrt{1 - \frac{dg+ch}{h(c+dx)}} \right)$$

$$\begin{aligned}
 & \left( \text{EllipticF} \left[ \text{i ArcSinh} \left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) / \\
 & \left( \sqrt{-\frac{de+cf}{f}} \sqrt{\left( f + \frac{de-cf}{c+dx} \right) \left( h + \frac{dg-ch}{c+dx} \right)} \right) + \\
 & \left( 16 \text{i } b^2 c^3 C d e f^3 h^4 \sqrt{1 - \frac{de+cf}{f(c+dx)}} \sqrt{1 - \frac{dg+ch}{h(c+dx)}} \right) \\
 & \left( \text{EllipticF} \left[ \text{i ArcSinh} \left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) / \\
 & \left( \sqrt{-\frac{de+cf}{f}} \sqrt{\left( f + \frac{de-cf}{c+dx} \right) \left( h + \frac{dg-ch}{c+dx} \right)} \right) - \\
 & \left( 42 \text{i } a b c^2 C d^2 e f^3 h^4 \sqrt{1 - \frac{de+cf}{f(c+dx)}} \sqrt{1 - \frac{dg+ch}{h(c+dx)}} \right) \\
 & \left( \text{EllipticF} \left[ \text{i ArcSinh} \left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) / \\
 & \left( \sqrt{-\frac{de+cf}{f}} \sqrt{\left( f + \frac{de-cf}{c+dx} \right) \left( h + \frac{dg-ch}{c+dx} \right)} \right) + \\
 & \left( 35 \text{i } A b^2 c d^3 e f^3 h^4 \sqrt{1 - \frac{de+cf}{f(c+dx)}} \sqrt{1 - \frac{dg+ch}{h(c+dx)}} \right)
 \end{aligned}$$

$$\left( \text{EllipticF} \left[ \text{i ArcSinh} \left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) /$$

$$\left( \sqrt{-\frac{de+cf}{f}} \sqrt{\left(f + \frac{de-cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} \right) +$$

$$\left( 35 \text{i} a^2 c C d^3 e f^3 h^4 \sqrt{1 - \frac{de+cf}{f(c+dx)}} \sqrt{1 - \frac{dg+ch}{h(c+dx)}} \right)$$

$$\left( \text{EllipticF} \left[ \text{i ArcSinh} \left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) /$$

$$\left( \sqrt{-\frac{de+cf}{f}} \sqrt{\left(f + \frac{de-cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} \right) +$$

$$\left( 48 \text{i} b^2 c^4 C f^4 h^4 \sqrt{1 - \frac{de+cf}{f(c+dx)}} \sqrt{1 - \frac{dg+ch}{h(c+dx)}} \right)$$

$$\left( \text{EllipticF} \left[ \text{i ArcSinh} \left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) /$$

$$\left( \sqrt{-\frac{de+cf}{f}} \sqrt{\left(f + \frac{de-cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} \right) - \left( 112 \text{i} a b c^3 C d f^4 h^4 \sqrt{1 - \frac{de+cf}{f(c+dx)}} \right)$$

$$\left( \sqrt{1 - \frac{dg+ch}{h(c+dx)}} \text{EllipticF} \left[ \text{i ArcSinh} \left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) /$$

$$\left( \sqrt{-\frac{-de+cf}{f}} \sqrt{\left(f + \frac{de-cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} + \right. \\ \left. 70 i A b^2 c^2 d^2 f^4 h^4 \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \right. \\ \left. \text{EllipticF}\left[ i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}}\right], \frac{f(-dg+ch)}{(-de+cf)h}\right] \right) /$$

$$\left( \sqrt{-\frac{-de+cf}{f}} \sqrt{\left(f + \frac{de-cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} + \right. \\ \left. 70 i a^2 c^2 C d^2 f^4 h^4 \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \right. \\ \left. \text{EllipticF}\left[ i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}}\right], \frac{f(-dg+ch)}{(-de+cf)h}\right] \right) /$$

$$\left( \sqrt{-\frac{-de+cf}{f}} \sqrt{\left(f + \frac{de-cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} - \right. \\ \left. 210 i a A b c d^3 f^4 h^4 \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \right. \\ \left. \text{EllipticF}\left[ i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}}\right], \frac{f(-dg+ch)}{(-de+cf)h}\right] \right) /$$

$$\left( \sqrt{-\frac{-de+cf}{f}} \sqrt{\left(f + \frac{de-cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} + \right.$$

$$\left( 105 i a^2 A d^4 f^4 h^4 \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \right. \\ \left. \text{EllipticF}\left[ i \text{ArcSinh}\left[ \frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) / \\ \left( \sqrt{-\frac{-de+cf}{f}} \sqrt{\left( f + \frac{de-cf}{c+dx} \right) \left( h + \frac{dg-ch}{c+dx} \right)} \right) \right)$$

**Problem 27: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{(a+bx)(A+Cx^2)}{\sqrt{c+dx}\sqrt{e+fx}\sqrt{g+hx}} dx$$

Optimal (type 4, 611 leaves, 8 steps):

$$\begin{aligned}
 & \frac{4C(adfh - 2b(dfg + deh + cfh))\sqrt{c+dx}\sqrt{e+fx}\sqrt{g+hx}}{15d^2f^2h^2} + \\
 & \frac{2C(a+bx)\sqrt{c+dx}\sqrt{e+fx}\sqrt{g+hx}}{5dfh} - \left( 2\sqrt{-de+cf} (10aCdfh(dfg + deh + cfh) - \right. \\
 & \quad \left. b(15Ad^2f^2h^2 + C(8c^2f^2h^2 + 7cdfh(fg + eh) + d^2(8f^2g^2 + 7efgh + 8e^2h^2)))) \right) \\
 & \left. \sqrt{\frac{d(e+fx)}{de-cf}} \sqrt{g+hx} \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{f}\sqrt{c+dx}}{\sqrt{-de+cf}}\right], \frac{(de-cf)h}{f(dg-ch)}\right] \right) / \\
 & \left( 15d^3f^{5/2}h^3\sqrt{e+fx} \sqrt{\frac{d(g+hx)}{dg-ch}} \right) + \\
 & \left( 2\sqrt{-de+cf} (5adfh(3Adfh^2 + C(ch(fg-eh) + dg(2fg+eh))) - b(15Ad^2f^2gh^2 + \right. \\
 & \quad \left. C(4c^2fh^2(fg-eh) + cdh(3f^2g^2 + efgh - 4e^2h^2) + d^2g(8f^2g^2 + 3efgh + 4e^2h^2)))) \right) \\
 & \left. \sqrt{\frac{d(e+fx)}{de-cf}} \sqrt{\frac{d(g+hx)}{dg-ch}} \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{f}\sqrt{c+dx}}{\sqrt{-de+cf}}\right], \frac{(de-cf)h}{f(dg-ch)}\right] \right) / \\
 & (15d^3f^{5/2}h^3\sqrt{e+fx}\sqrt{g+hx})
 \end{aligned}$$

Result (type 4, 8828 leaves):

$$\begin{aligned}
 & \sqrt{c+dx}\sqrt{e+fx} \left( \frac{2C(-4bdfg - 4bdeh - 4bcfh + 5adfh)}{15d^2f^2h^2} + \frac{2bCx}{5dfh} \right) \sqrt{g+hx} - \\
 & \frac{1}{15d^4f^2h^2} 2 \left( \left( (-8bCd^2f^2g^2 - 7bCd^2efgh - 7bCcdf^2gh + 10aCd^2f^2gh - 8bCd^2e^2h^2 - \right. \right. \\
 & \quad \left. \left. 7bCcdefh^2 + 10aCd^2efh^2 - 8bc^2Cf^2h^2 + 10acCd^2f^2h^2 - 15Abd^2f^2h^2) \right) \right. \\
 & \quad \left. (c+dx)^{3/2} \left( f + \frac{de}{c+dx} - \frac{cf}{c+dx} \right) \left( h + \frac{dg}{c+dx} - \frac{ch}{c+dx} \right) \right) / \\
 & \left( fh \sqrt{e + \frac{(c+dx)(f - \frac{cf}{c+dx})}{d}} \sqrt{g + \frac{(c+dx)(h - \frac{ch}{c+dx})}{d}} \right) + \\
 & \frac{1}{fh \sqrt{e + \frac{(c+dx)(f - \frac{cf}{c+dx})}{d}} \sqrt{g + \frac{(c+dx)(h - \frac{ch}{c+dx})}{d}}}
 \end{aligned}$$

$$\begin{aligned}
 & (c+dx) \sqrt{\left(f + \frac{de}{c+dx} - \frac{cf}{c+dx}\right) \left(h + \frac{dg}{c+dx} - \frac{ch}{c+dx}\right)} \\
 & \left( \left( 8 \, i \, b \, C \, d^4 \, e \, f^2 \, g^3 \, h \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \left( \text{EllipticE} \left[ i \, \text{ArcSinh} \left[ \frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}} \right], \right. \right. \right. \right. \\
 & \left. \left. \left. \frac{f(-dg+ch)}{(-de+cf)h} \right] - \text{EllipticF} \left[ i \, \text{ArcSinh} \left[ \frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) \right) / \\
 & \left( \sqrt{-\frac{-de+cf}{f}} (-dg+ch) \sqrt{\left(f + \frac{de-cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} - 8 \, i \, b \, c \, C \, d^3 \right. \\
 & \left. f^3 \, g^3 \, h \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \left( \text{EllipticE} \left[ i \, \text{ArcSinh} \left[ \frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}} \right], \right. \right. \right. \right. \\
 & \left. \left. \left. \frac{f(-dg+ch)}{(-de+cf)h} \right] - \text{EllipticF} \left[ i \, \text{ArcSinh} \left[ \frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) \right) / \\
 & \left( \sqrt{-\frac{-de+cf}{f}} (-dg+ch) \sqrt{\left(f + \frac{de-cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} + 7 \, i \, b \, C \, d^4 \, e^2 \right. \\
 & \left. f \, g^2 \, h^2 \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \left( \text{EllipticE} \left[ i \, \text{ArcSinh} \left[ \frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}} \right], \right. \right. \right. \right. \\
 & \left. \left. \left. \frac{f(-dg+ch)}{(-de+cf)h} \right] - \text{EllipticF} \left[ i \, \text{ArcSinh} \left[ \frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) \right) /
 \end{aligned}$$

$$\left( \sqrt{-\frac{-de+cf}{f}} (-dg+ch) \sqrt{\left(f + \frac{de-cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} \right) - \left( 8 i b c C d^3 \right.$$

$$e f^2 g^2 h^2 \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \left( \text{EllipticE}\left[ i \text{ArcSinh}\left[ \frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}} \right], \right. \right.$$

$$\left. \left. \frac{f(-dg+ch)}{(-de+cf)h} \right] - \text{EllipticF}\left[ i \text{ArcSinh}\left[ \frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) \Bigg/$$

$$\left( \sqrt{-\frac{-de+cf}{f}} (-dg+ch) \sqrt{\left(f + \frac{de-cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} \right) -$$

$$\left( 10 i a C d^4 e f^2 g^2 h^2 \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \right.$$

$$\left( \text{EllipticE}\left[ i \text{ArcSinh}\left[ \frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] - \right.$$

$$\left. \left. \text{EllipticF}\left[ i \text{ArcSinh}\left[ \frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) \Bigg/$$

$$\left( \sqrt{-\frac{-de+cf}{f}} (-dg+ch) \sqrt{\left(f + \frac{de-cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} \right) +$$

$$\left( i b c^2 C d^2 f^3 g^2 h^2 \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \right)$$

$$\left( \text{EllipticE} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] - \right. \\
 \left. \text{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) / \\
 \left( \sqrt{-\frac{de+cf}{f}} (-dg+ch) \sqrt{\left( f + \frac{de-cf}{c+dx} \right) \left( h + \frac{dg-ch}{c+dx} \right)} \right) + \\
 \left( 10 i a c C d^3 f^3 g^2 h^2 \sqrt{1 - \frac{de+cf}{f(c+dx)}} \sqrt{1 - \frac{dg+ch}{h(c+dx)}} \right. \\
 \left. \left( \text{EllipticE} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] - \right. \right. \\
 \left. \left. \text{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) / \right. \\
 \left. \left( \sqrt{-\frac{de+cf}{f}} (-dg+ch) \sqrt{\left( f + \frac{de-cf}{c+dx} \right) \left( h + \frac{dg-ch}{c+dx} \right)} \right) + \right. \\
 \left. \left( 8 i b C d^4 e^3 g h^3 \sqrt{1 - \frac{de+cf}{f(c+dx)}} \sqrt{1 - \frac{dg+ch}{h(c+dx)}} \left( \text{EllipticE} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \right. \right. \right. \right. \\
 \left. \left. \left. \frac{f(-dg+ch)}{(-de+cf)h} \right] - \text{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) \right) / \right.$$

$$\begin{aligned}
 & \left( \sqrt{-\frac{-de+cf}{f}} (-dg+ch) \sqrt{\left(f + \frac{de-cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} \right) - \\
 & \left( 8 i b c C d^3 e^2 f g h^3 \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \right. \\
 & \left( \text{EllipticE}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}}\right], \frac{f(-dg+ch)}{(-de+cf)h}\right] - \right. \\
 & \left. \left. \text{EllipticF}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}}\right], \frac{f(-dg+ch)}{(-de+cf)h}\right] \right) \right) / \\
 & \left( \sqrt{-\frac{-de+cf}{f}} (-dg+ch) \sqrt{\left(f + \frac{de-cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} \right) - \\
 & \left( 10 i a C d^4 e^2 f g h^3 \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \right. \\
 & \left( \text{EllipticE}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}}\right], \frac{f(-dg+ch)}{(-de+cf)h}\right] - \right. \\
 & \left. \left. \text{EllipticF}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}}\right], \frac{f(-dg+ch)}{(-de+cf)h}\right] \right) \right) / \\
 & \left( \sqrt{-\frac{-de+cf}{f}} (-dg+ch) \sqrt{\left(f + \frac{de-cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} \right) +
 \end{aligned}$$

$$\left( \begin{aligned} & i b c^2 C d^2 e f^2 g h^3 \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \\ & \left( \begin{aligned} & \text{EllipticE} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] - \\ & \text{EllipticF} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) / \\ & \left( \sqrt{-\frac{-de+cf}{f}} (-dg+ch) \sqrt{\left( f + \frac{de-cf}{c+dx} \right) \left( h + \frac{dg-ch}{c+dx} \right)} \right) + \\ & 10 i a c C d^3 e f^2 g h^3 \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \\ & \left( \begin{aligned} & \text{EllipticE} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] - \\ & \text{EllipticF} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) / \\ & \left( \sqrt{-\frac{-de+cf}{f}} (-dg+ch) \sqrt{\left( f + \frac{de-cf}{c+dx} \right) \left( h + \frac{dg-ch}{c+dx} \right)} \right) + \\ & 15 i A b d^4 e f^2 g h^3 \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \end{aligned} \right)
 \end{aligned} \right)$$

$$\left( \text{EllipticE}\left[\text{i ArcSinh}\left[\frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}}\right], \frac{f(-dg+ch)}{(-de+cf)h}\right] - \right.$$

$$\left. \text{EllipticF}\left[\text{i ArcSinh}\left[\frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}}\right], \frac{f(-dg+ch)}{(-de+cf)h}\right] \right) /$$

$$\left( \sqrt{-\frac{de+cf}{f}} (-dg+ch) \sqrt{\left(f + \frac{de- cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} \right) -$$

$$\left( \text{i } b c^3 C d f^3 g h^3 \sqrt{1 - \frac{de+cf}{f(c+dx)}} \sqrt{1 - \frac{dg+ch}{h(c+dx)}} \left( \text{EllipticE}\left[\text{i ArcSinh}\left[\frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}}\right], \right. \right.$$

$$\left. \left. \frac{f(-dg+ch)}{(-de+cf)h} - \text{EllipticF}\left[\text{i ArcSinh}\left[\frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}}\right], \frac{f(-dg+ch)}{(-de+cf)h}\right] \right) \right) /$$

$$\left( \sqrt{-\frac{de+cf}{f}} (-dg+ch) \sqrt{\left(f + \frac{de- cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} \right) -$$

$$\left( 15 \text{i } A b c d^3 f^3 g h^3 \sqrt{1 - \frac{de+cf}{f(c+dx)}} \sqrt{1 - \frac{dg+ch}{h(c+dx)}} \right.$$

$$\left( \text{EllipticE}\left[\text{i ArcSinh}\left[\frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}}\right], \frac{f(-dg+ch)}{(-de+cf)h}\right] - \right.$$

$$\left. \left. \text{EllipticF}\left[\text{i ArcSinh}\left[\frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}}\right], \frac{f(-dg+ch)}{(-de+cf)h}\right] \right) \right) /$$

$$\begin{aligned}
 & \left( \sqrt{-\frac{-de+cf}{f}} (-dg+ch) \sqrt{\left(f+\frac{de-cf}{c+dx}\right) \left(h+\frac{dg-ch}{c+dx}\right)} \right) - \\
 & \left( 8 i b c C d^3 e^3 h^4 \sqrt{1-\frac{-de+cf}{f(c+dx)}} \sqrt{1-\frac{-dg+ch}{h(c+dx)}} \left( \text{EllipticE}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}}\right], \right. \right. \right. \\
 & \left. \left. \left. \frac{f(-dg+ch)}{(-de+cf)h}\right] - \text{EllipticF}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}}\right], \frac{f(-dg+ch)}{(-de+cf)h}\right] \right) \right) / \\
 & \left( \sqrt{-\frac{-de+cf}{f}} (-dg+ch) \sqrt{\left(f+\frac{de-cf}{c+dx}\right) \left(h+\frac{dg-ch}{c+dx}\right)} \right) + \\
 & \left( i b c^2 C d^2 e^2 f h^4 \sqrt{1-\frac{-de+cf}{f(c+dx)}} \sqrt{1-\frac{-dg+ch}{h(c+dx)}} \right. \\
 & \left. \left( \text{EllipticE}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}}\right], \frac{f(-dg+ch)}{(-de+cf)h}\right] - \right. \right. \\
 & \left. \left. \text{EllipticF}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}}\right], \frac{f(-dg+ch)}{(-de+cf)h}\right] \right) \right) / \\
 & \left( \sqrt{-\frac{-de+cf}{f}} (-dg+ch) \sqrt{\left(f+\frac{de-cf}{c+dx}\right) \left(h+\frac{dg-ch}{c+dx}\right)} \right) + \\
 & \left( 10 i a c C d^3 e^2 f h^4 \sqrt{1-\frac{-de+cf}{f(c+dx)}} \sqrt{1-\frac{-dg+ch}{h(c+dx)}} \right.
 \end{aligned}$$

$$\left( \text{EllipticE} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] - \right.$$

$$\left. \left. \text{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) \right) /$$

$$\left( \sqrt{-\frac{de+cf}{f}} (-dg+ch) \sqrt{\left( f + \frac{de-cf}{c+dx} \right) \left( h + \frac{dg-ch}{c+dx} \right)} \right) -$$

$$\left( i b c^3 C d e f^2 h^4 \sqrt{1 - \frac{de+cf}{f(c+dx)}} \sqrt{1 - \frac{dg+ch}{h(c+dx)}} \left( \text{EllipticE} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \right. \right. \right.$$

$$\left. \left. \left. \frac{f(-dg+ch)}{(-de+cf)h} \right] - \text{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) \right) /$$

$$\left( \sqrt{-\frac{de+cf}{f}} (-dg+ch) \sqrt{\left( f + \frac{de-cf}{c+dx} \right) \left( h + \frac{dg-ch}{c+dx} \right)} \right) -$$

$$\left( 15 i A b c d^3 e f^2 h^4 \sqrt{1 - \frac{de+cf}{f(c+dx)}} \sqrt{1 - \frac{dg+ch}{h(c+dx)}} \right.$$

$$\left. \left( \text{EllipticE} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] - \right. \right.$$

$$\left. \left. \left. \text{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) \right) /$$

$$\begin{aligned}
 & \left( \sqrt{-\frac{-de+cf}{f}} (-dg+ch) \sqrt{\left(f + \frac{de-cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} \right) + \\
 & \left( 8 i b c^4 C f^3 h^4 \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \left( \text{EllipticE}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}}\right], \right. \right. \right. \\
 & \left. \left. \left. \frac{f(-dg+ch)}{(-de+cf)h}\right] - \text{EllipticF}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}}\right], \frac{f(-dg+ch)}{(-de+cf)h}\right] \right) \right) / \\
 & \left( \sqrt{-\frac{-de+cf}{f}} (-dg+ch) \sqrt{\left(f + \frac{de-cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} \right) - \\
 & \left( 10 i a c^3 C d f^3 h^4 \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \right. \\
 & \left. \left( \text{EllipticE}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}}\right], \frac{f(-dg+ch)}{(-de+cf)h}\right] - \right. \right. \\
 & \left. \left. \text{EllipticF}\left[i \text{ArcSinh}\left[\frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}}\right], \frac{f(-dg+ch)}{(-de+cf)h}\right] \right) \right) / \\
 & \left( \sqrt{-\frac{-de+cf}{f}} (-dg+ch) \sqrt{\left(f + \frac{de-cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} \right) + \\
 & \left( 15 i A b c^2 d^2 f^3 h^4 \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \right.
 \end{aligned}$$

$$\left( \text{EllipticE} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] - \right.$$

$$\left. \left. \text{EllipticF} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) \right) /$$

$$\left( \sqrt{-\frac{de+cf}{f}} (-dg+ch) \sqrt{\left( f + \frac{de-cf}{c+dx} \right) \left( h + \frac{dg-ch}{c+dx} \right)} \right) -$$

$$\left( 4 i b c d^3 e f^2 g^2 h \sqrt{1 - \frac{de+cf}{f(c+dx)}} \sqrt{1 - \frac{dg+ch}{h(c+dx)}} \right.$$

$$\left. \left. \text{EllipticF} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) \right) /$$

$$\left( \sqrt{-\frac{de+cf}{f}} \sqrt{\left( f + \frac{de-cf}{c+dx} \right) \left( h + \frac{dg-ch}{c+dx} \right)} \right) + \left( 4 i b c c d^2 f^3 g^2 h \sqrt{1 - \frac{de+cf}{f(c+dx)}} \right.$$

$$\left. \left. \sqrt{1 - \frac{dg+ch}{h(c+dx)}} \text{EllipticF} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) \right) /$$

$$\left( \sqrt{-\frac{de+cf}{f}} \sqrt{\left( f + \frac{de-cf}{c+dx} \right) \left( h + \frac{dg-ch}{c+dx} \right)} \right) -$$

$$\left( 4 i b c d^3 e^2 f g h^2 \sqrt{1 - \frac{de+cf}{f(c+dx)}} \sqrt{1 - \frac{dg+ch}{h(c+dx)}} \right)$$

$$\left. \text{EllipticF}\left[\text{i ArcSinh}\left[\frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}}\right], \frac{f(-dg+ch)}{(-de+cf)h}\right]\right/$$

$$\left(\sqrt{-\frac{de+cf}{f}} \sqrt{\left(f+\frac{de-cf}{c+dx}\right)\left(h+\frac{dg-ch}{c+dx}\right)}\right) + \left(\text{i} b c C d^2 e f^2 g h^2 \sqrt{1-\frac{-de+cf}{f(c+dx)}}\right)$$

$$\left.\sqrt{1-\frac{-dg+ch}{h(c+dx)}} \text{EllipticF}\left[\text{i ArcSinh}\left[\frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}}\right], \frac{f(-dg+ch)}{(-de+cf)h}\right]\right/$$

$$\left(\sqrt{-\frac{de+cf}{f}} \sqrt{\left(f+\frac{de-cf}{c+dx}\right)\left(h+\frac{dg-ch}{c+dx}\right)}\right) +$$

$$\left(5 \text{i} a C d^3 e f^2 g h^2 \sqrt{1-\frac{-de+cf}{f(c+dx)}} \sqrt{1-\frac{-dg+ch}{h(c+dx)}}\right)$$

$$\left.\text{EllipticF}\left[\text{i ArcSinh}\left[\frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}}\right], \frac{f(-dg+ch)}{(-de+cf)h}\right]\right/$$

$$\left(\sqrt{-\frac{de+cf}{f}} \sqrt{\left(f+\frac{de-cf}{c+dx}\right)\left(h+\frac{dg-ch}{c+dx}\right)}\right) + \left(3 \text{i} b c^2 C d f^3 g h^2 \sqrt{1-\frac{-de+cf}{f(c+dx)}}\right)$$

$$\left.\sqrt{1-\frac{-dg+ch}{h(c+dx)}} \text{EllipticF}\left[\text{i ArcSinh}\left[\frac{\sqrt{-\frac{de+cf}{f}}}{\sqrt{c+dx}}\right], \frac{f(-dg+ch)}{(-de+cf)h}\right]\right/$$

$$\left(\sqrt{-\frac{de+cf}{f}} \sqrt{\left(f+\frac{de-cf}{c+dx}\right)\left(h+\frac{dg-ch}{c+dx}\right)}\right) -$$

$$\left( 5 i a c C d^2 f^3 g h^2 \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \right.$$

$$\left. \text{EllipticF}\left[ i \text{ArcSinh}\left[ \frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) /$$

$$\left( \sqrt{-\frac{-de+cf}{f}} \sqrt{\left( f + \frac{de-cf}{c+dx} \right) \left( h + \frac{dg-ch}{c+dx} \right)} \right) + \left( 4 i b c C d^2 e^2 f h^3 \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \right.$$

$$\left. \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \text{EllipticF}\left[ i \text{ArcSinh}\left[ \frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) /$$

$$\left( \sqrt{-\frac{-de+cf}{f}} \sqrt{\left( f + \frac{de-cf}{c+dx} \right) \left( h + \frac{dg-ch}{c+dx} \right)} \right) +$$

$$\left( 3 i b c^2 C d e f^2 h^3 \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \right.$$

$$\left. \text{EllipticF}\left[ i \text{ArcSinh}\left[ \frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) /$$

$$\left( \sqrt{-\frac{-de+cf}{f}} \sqrt{\left( f + \frac{de-cf}{c+dx} \right) \left( h + \frac{dg-ch}{c+dx} \right)} \right) - \left( 5 i a c C d^2 e f^2 h^3 \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \right.$$

$$\left. \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \text{EllipticF}\left[ i \text{ArcSinh}\left[ \frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) /$$

$$\begin{aligned}
 & \left( \sqrt{-\frac{-de+cf}{f}} \sqrt{\left(f + \frac{de-cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} + \left( 8 i b c^3 C f^3 h^3 \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \right. \right. \\
 & \left. \left. \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \operatorname{EllipticF}\left[ i \operatorname{ArcSinh}\left[ \frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) / \right. \\
 & \left( \sqrt{-\frac{-de+cf}{f}} \sqrt{\left(f + \frac{de-cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} - \left( 10 i a c^2 C d f^3 h^3 \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \right. \right. \\
 & \left. \left. \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \operatorname{EllipticF}\left[ i \operatorname{ArcSinh}\left[ \frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) / \right. \\
 & \left( \sqrt{-\frac{-de+cf}{f}} \sqrt{\left(f + \frac{de-cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} + \left( 15 i A b c d^2 f^3 h^3 \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \right. \right. \\
 & \left. \left. \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \operatorname{EllipticF}\left[ i \operatorname{ArcSinh}\left[ \frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}} \right], \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) / \right. \\
 & \left( \sqrt{-\frac{-de+cf}{f}} \sqrt{\left(f + \frac{de-cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} - \right. \\
 & \left. \left( 15 i a A d^3 f^3 h^3 \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \operatorname{EllipticF}\left[ i \operatorname{ArcSinh}\left[ \frac{\sqrt{-\frac{-de+cf}{f}}}{\sqrt{c+dx}} \right], \right. \right. \right. \\
 & \left. \left. \left. \frac{f(-dg+ch)}{(-de+cf)h} \right] \right) / \left( \sqrt{-\frac{-de+cf}{f}} \sqrt{\left(f + \frac{de-cf}{c+dx}\right) \left(h + \frac{dg-ch}{c+dx}\right)} \right) \right) \right)
 \end{aligned}$$

**Problem 28: Result unnecessarily involves imaginary or complex numbers.**

$$\int \frac{A + Cx^2}{\sqrt{c+dx} \sqrt{e+fx} \sqrt{g+hx}} dx$$

Optimal (type 4, 368 leaves, 7 steps):

$$\frac{2C\sqrt{c+dx}\sqrt{e+fx}\sqrt{g+hx}}{3dfh} - \left( 4C\sqrt{-de+cf} (dfg+deh+cfh) \sqrt{\frac{d(e+fx)}{de-cf}} \sqrt{g+hx} \right. \\ \left. \text{EllipticE}\left[\text{ArcSin}\left[\frac{\sqrt{f}\sqrt{c+dx}}{\sqrt{-de+cf}}\right], \frac{(de-cf)h}{f(dg-ch)}\right] \right) / \left( 3d^2 f^{3/2} h^2 \sqrt{e+fx} \sqrt{\frac{d(g+hx)}{dg-ch}} \right) + \\ \left( 2\sqrt{-de+cf} (3Adfh^2 + C(ch(fg-eh) + dg(2fg+eh))) \sqrt{\frac{d(e+fx)}{de-cf}} \sqrt{\frac{d(g+hx)}{dg-ch}} \right. \\ \left. \text{EllipticF}\left[\text{ArcSin}\left[\frac{\sqrt{f}\sqrt{c+dx}}{\sqrt{-de+cf}}\right], \frac{(de-cf)h}{f(dg-ch)}\right] \right) / (3d^2 f^{3/2} h^2 \sqrt{e+fx} \sqrt{g+hx})$$

Result (type 4, 390 leaves):

$$\left( \sqrt{c+dx} \left( 2Cd^2fh(e+fx)(g+hx) - \frac{4Cd^2(df g + de h + c f h)(e+fx)(g+hx)}{c+dx} - \right. \right. \\ \left. 4iC\sqrt{-c+\frac{de}{f}}fh(df g + de h + c f h)\sqrt{c+dx}\sqrt{\frac{d(e+fx)}{f(c+dx)}} \right. \\ \left. \sqrt{\frac{d(g+hx)}{h(c+dx)}} \text{EllipticE}\left[i \text{ArcSinh}\left[\frac{\sqrt{-c+\frac{de}{f}}}{\sqrt{c+dx}}\right], \frac{dfg-cfh}{deh-cfh}\right] + \frac{1}{\sqrt{-c+\frac{de}{f}}} \right. \\ \left. 2i dh (3Adf^2h + cCf(-fg+eh) + Cde(fg+2eh))\sqrt{c+dx}\sqrt{\frac{d(e+fx)}{f(c+dx)}}\sqrt{\frac{d(g+hx)}{h(c+dx)}} \right. \\ \left. \left. \text{EllipticF}\left[i \text{ArcSinh}\left[\frac{\sqrt{-c+\frac{de}{f}}}{\sqrt{c+dx}}\right], \frac{dfg-cfh}{deh-cfh}\right] \right) \right) / (3d^3 f^2 h^2 \sqrt{e+fx} \sqrt{g+hx})$$

**Problem 29: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{A + Cx^2}{(a + bx) \sqrt{c + dx} \sqrt{e + fx} \sqrt{g + hx}} dx$$

Optimal (type 4, 465 leaves, 11 steps):

$$\left( 2C \sqrt{-de + cf} \sqrt{\frac{d(e + fx)}{de - cf}} \sqrt{g + hx} \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{f} \sqrt{c + dx}}{\sqrt{-de + cf}}\right], \frac{(de - cf)h}{f(dg - ch)}\right] \right) /$$

$$\left( bd \sqrt{f} h \sqrt{e + fx} \sqrt{\frac{d(g + hx)}{dg - ch}} \right) - \left( 2C \sqrt{-de + cf} (bg + ah) \sqrt{\frac{d(e + fx)}{de - cf}} \sqrt{\frac{d(g + hx)}{dg - ch}} \right.$$

$$\left. \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{f} \sqrt{c + dx}}{\sqrt{-de + cf}}\right], \frac{(de - cf)h}{f(dg - ch)}\right] \right) / (b^2 d \sqrt{f} h \sqrt{e + fx} \sqrt{g + hx}) -$$

$$\left( 2 \left( A + \frac{a^2 C}{b^2} \right) \sqrt{-de + cf} \sqrt{\frac{d(e + fx)}{de - cf}} \sqrt{\frac{d(g + hx)}{dg - ch}} \operatorname{EllipticPi}\left[-\frac{b(de - cf)}{(bc - ad)f}, \right.$$

$$\left. \operatorname{ArcSin}\left[\frac{\sqrt{f} \sqrt{c + dx}}{\sqrt{-de + cf}}\right], \frac{(de - cf)h}{f(dg - ch)}\right] \right) / ((bc - ad) \sqrt{f} \sqrt{e + fx} \sqrt{g + hx})$$

Result (type 4, 13075 leaves):

$$-\frac{1}{d^2} 2 \left( -\frac{C(c + dx)^{3/2} \left( f + \frac{de}{c + dx} - \frac{cf}{c + dx} \right) \left( h + \frac{dg}{c + dx} - \frac{ch}{c + dx} \right)}{bfh \sqrt{e + \frac{(c + dx)(f - \frac{cf}{c + dx})}{d}} \sqrt{g + \frac{(c + dx)(h - \frac{ch}{c + dx})}{d}}} + \right.$$

$$\left( (c + dx) \left( b - \frac{bc}{c + dx} + \frac{ad}{c + dx} \right) \sqrt{f + \frac{de}{c + dx} - \frac{cf}{c + dx}} \sqrt{h + \frac{dg}{c + dx} - \frac{ch}{c + dx}} \right.$$

$$\left. \sqrt{\left( fh + \frac{d^2 eg}{(c + dx)^2} - \frac{cdfg}{(c + dx)^2} - \frac{cdeh}{(c + dx)^2} + \frac{c^2 fh}{(c + dx)^2} + \frac{dfg}{c + dx} + \frac{deh}{c + dx} - \frac{2cfh}{c + dx} \right)} \right.$$

$$\left. - \frac{d(bcEg + aCfg - aCeh + Abfh)}{bf(bg - ah) \sqrt{f + \frac{de}{c + dx} - \frac{cf}{c + dx}} \sqrt{h + \frac{dg}{c + dx} - \frac{ch}{c + dx}}} \right)$$

$$\begin{aligned}
 & \frac{a C d^3 e g \sqrt{h + \frac{d g}{c+d x} - \frac{c h}{c+d x}}}{b (b c - a d) f h (d g - c h) \sqrt{f + \frac{d e}{c+d x} - \frac{c f}{c+d x}}} - \frac{c^3 C \sqrt{h + \frac{d g}{c+d x} - \frac{c h}{c+d x}}}{(b c - a d) (-d g + c h) \sqrt{f + \frac{d e}{c+d x} - \frac{c f}{c+d x}}} + \\
 & \frac{a c^2 C d \sqrt{h + \frac{d g}{c+d x} - \frac{c h}{c+d x}}}{b (b c - a d) (-d g + c h) \sqrt{f + \frac{d e}{c+d x} - \frac{c f}{c+d x}}} + \frac{c^2 C d e \sqrt{h + \frac{d g}{c+d x} - \frac{c h}{c+d x}}}{(b c - a d) f (-d g + c h) \sqrt{f + \frac{d e}{c+d x} - \frac{c f}{c+d x}}} - \\
 & \frac{a c C d^2 e \sqrt{h + \frac{d g}{c+d x} - \frac{c h}{c+d x}}}{b (b c - a d) f (-d g + c h) \sqrt{f + \frac{d e}{c+d x} - \frac{c f}{c+d x}}} + \\
 & \frac{c^2 C d g \sqrt{h + \frac{d g}{c+d x} - \frac{c h}{c+d x}}}{(b c - a d) h (-d g + c h) \sqrt{f + \frac{d e}{c+d x} - \frac{c f}{c+d x}}} - \\
 & \frac{a c C d^2 g \sqrt{h + \frac{d g}{c+d x} - \frac{c h}{c+d x}}}{b (b c - a d) h (-d g + c h) \sqrt{f + \frac{d e}{c+d x} - \frac{c f}{c+d x}}} - \\
 & \frac{c C d^2 e g \sqrt{h + \frac{d g}{c+d x} - \frac{c h}{c+d x}}}{(b c - a d) f h (-d g + c h) \sqrt{f + \frac{d e}{c+d x} - \frac{c f}{c+d x}}} + \\
 & \left( \frac{(A b^2 + a^2 C) d \sqrt{h + \frac{d g}{c+d x} - \frac{c h}{c+d x}}}{b (b g - a h) \left( b - \frac{b c}{c+d x} + \frac{a d}{c+d x} \right) \sqrt{f + \frac{d e}{c+d x} - \frac{c f}{c+d x}}} \right) \\
 & \left( \left( i C d^2 e f g \sqrt{1 - \frac{-d e + c f}{f (c+d x)}} \sqrt{1 - \frac{-d g + c h}{h (c+d x)}} \right) \left( \text{EllipticE} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{-d g + c h}{h}}}{\sqrt{c+d x}} \right] \right) \right),
 \end{aligned}$$

$$\left. \left. \left. \frac{(-de+cf)h}{f(-dg+ch)} \right] - \text{EllipticF} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{dg+ch}{h}}}{\sqrt{c+dx}} \right], \frac{(-de+cf)h}{f(-dg+ch)} \right] \right) \right) /$$

$$\left( (-de+cf) \sqrt{-\frac{dg+ch}{h}} \sqrt{\left( fh + \frac{d^2eg - cdfg - cdeh + c^2fh}{(c+dx)^2} + \right.} \right.$$

$$\left. \left. \frac{dfg+deh-2cfh}{c+dx} \right) \right) - \left( i c C d f^2 g \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \right.$$

$$\left. \left. \left( \text{EllipticE} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{dg+ch}{h}}}{\sqrt{c+dx}} \right], \frac{(-de+cf)h}{f(-dg+ch)} \right] - \text{EllipticF} \left[ \right. \right. \right.$$

$$\left. \left. \left. i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{dg+ch}{h}}}{\sqrt{c+dx}} \right], \frac{(-de+cf)h}{f(-dg+ch)} \right] \right) \right) / \left( (-de+cf) \sqrt{-\frac{dg+ch}{h}} \right.$$

$$\left. \left. \sqrt{\left( fh + \frac{d^2eg - cdfg - cdeh + c^2fh}{(c+dx)^2} + \frac{dfg+deh-2cfh}{c+dx} \right) \right) \right) -$$

$$\left( i c C d e f h \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \left( \text{EllipticE} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{dg+ch}{h}}}{\sqrt{c+dx}} \right], \right. \right. \right.$$

$$\left. \left. \left. \frac{(-de+cf)h}{f(-dg+ch)} \right] - \text{EllipticF} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{dg+ch}{h}}}{\sqrt{c+dx}} \right], \frac{(-de+cf)h}{f(-dg+ch)} \right] \right) \right) /$$

$$\left( (-de+cf) \sqrt{-\frac{dg+ch}{h}} \sqrt{\left( fh + \frac{d^2eg - cdfg - cdeh + c^2fh}{(c+dx)^2} + \right.} \right.$$

$$\left. \frac{dfg+deh-2cfh}{c+dx} \right) + \left( i c^2 C f^2 h \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \right.$$

$$\left. \left( \text{EllipticE} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{-dg+ch}{h}}}{\sqrt{c+dx}} \right], \frac{(-de+cf)h}{f(-dg+ch)} \right] - \text{EllipticF} \left[ \right. \right. \right.$$

$$\left. \left. \left. i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{-dg+ch}{h}}}{\sqrt{c+dx}} \right], \frac{(-de+cf)h}{f(-dg+ch)} \right] \right) \right) / \left( (-de+cf) \sqrt{-\frac{-dg+ch}{h}} \right.$$

$$\left. \left. \left. \sqrt{\left( fh + \frac{d^2 eg - cdfg - cdeh + c^2 fh}{(c+dx)^2} + \frac{dfg+deh-2cfh}{c+dx} \right)} \right) \right) -$$

$$\left( i b^2 c C d^2 e g \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \text{EllipticF} \left[ \right. \right.$$

$$\left. \left. \left. i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{-dg+ch}{h}}}{\sqrt{c+dx}} \right], \frac{(-de+cf)h}{f(-dg+ch)} \right] \right) \right) / \left( (bc-ad)^2 \sqrt{-\frac{-dg+ch}{h}} \right.$$

$$\left. \left. \left. \sqrt{\left( fh + \frac{d^2 eg - cdfg - cdeh + c^2 fh}{(c+dx)^2} + \frac{dfg+deh-2cfh}{c+dx} \right)} \right) \right) +$$

$$\left( i a b C d^3 e g \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \text{EllipticF} \left[ \right. \right.$$

$$\left. \left. \left. i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{-dg+ch}{h}}}{\sqrt{c+dx}} \right], \frac{(-de+cf)h}{f(-dg+ch)} \right] \right) \right) / \left( (bc-ad)^2 \sqrt{-\frac{-dg+ch}{h}} \right.$$

$$\begin{aligned}
 & \sqrt{\left( fh + \frac{d^2 eg - cdfg - cdeh + c^2 fh}{(c+dx)^2} + \frac{dfg + deh - 2cfh}{c+dx} \right)} + \\
 & \left( \begin{aligned}
 & \text{i } b C d^2 e g \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \text{EllipticF}[ \\
 & \text{i ArcSinh}\left[\frac{\sqrt{-\frac{-dg+ch}{h}}}{\sqrt{c+dx}}\right], \frac{(-de+cf)h}{f(-dg+ch)} \right] \Big/ \left( (bc-ad) \sqrt{-\frac{-dg+ch}{h}} \right)
 \end{aligned} \right) \\
 & \sqrt{\left( fh + \frac{d^2 eg - cdfg - cdeh + c^2 fh}{(c+dx)^2} + \frac{dfg + deh - 2cfh}{c+dx} \right)} + \\
 & \left( \begin{aligned}
 & \text{i } b^2 c^2 C d f g \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \text{EllipticF}[ \\
 & \text{i ArcSinh}\left[\frac{\sqrt{-\frac{-dg+ch}{h}}}{\sqrt{c+dx}}\right], \frac{(-de+cf)h}{f(-dg+ch)} \right] \Big/ \left( (bc-ad)^2 \sqrt{-\frac{-dg+ch}{h}} \right)
 \end{aligned} \right) \\
 & \sqrt{\left( fh + \frac{d^2 eg - cdfg - cdeh + c^2 fh}{(c+dx)^2} + \frac{dfg + deh - 2cfh}{c+dx} \right)} - \\
 & \left( \begin{aligned}
 & \text{i } a b c C d^2 f g \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \text{EllipticF}[ \\
 & \text{i ArcSinh}\left[\frac{\sqrt{-\frac{-dg+ch}{h}}}{\sqrt{c+dx}}\right], \frac{(-de+cf)h}{f(-dg+ch)} \right] \Big/ \left( (bc-ad)^2 \sqrt{-\frac{-dg+ch}{h}} \right)
 \end{aligned} \right) \\
 & \sqrt{\left( fh + \frac{d^2 eg - cdfg - cdeh + c^2 fh}{(c+dx)^2} + \frac{dfg + deh - 2cfh}{c+dx} \right)} -
 \end{aligned}$$

$$\begin{aligned}
 & \left( i b c C d f g \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \text{EllipticF} \left[ \right. \right. \\
 & \quad \left. \left. i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{-dg+ch}{h}}}{\sqrt{c+dx}} \right], \frac{(-de+cf)h}{f(-dg+ch)} \right] \right) / \left( (bc-ad) \sqrt{-\frac{-dg+ch}{h}} \right) \\
 & \quad \sqrt{\left( fh + \frac{d^2 eg - cdfg - cdeh + c^2 fh}{(c+dx)^2} + \frac{dfg + deh - 2cfh}{c+dx} \right)} + \\
 & \left( i b^2 c^2 C de h \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \text{EllipticF} \left[ \right. \right. \\
 & \quad \left. \left. i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{-dg+ch}{h}}}{\sqrt{c+dx}} \right], \frac{(-de+cf)h}{f(-dg+ch)} \right] \right) / \left( (bc-ad)^2 \sqrt{-\frac{-dg+ch}{h}} \right) \\
 & \quad \sqrt{\left( fh + \frac{d^2 eg - cdfg - cdeh + c^2 fh}{(c+dx)^2} + \frac{dfg + deh - 2cfh}{c+dx} \right)} - \\
 & \left( i a b c C d^2 e h \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \text{EllipticF} \left[ \right. \right. \\
 & \quad \left. \left. i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{-dg+ch}{h}}}{\sqrt{c+dx}} \right], \frac{(-de+cf)h}{f(-dg+ch)} \right] \right) / \left( (bc-ad)^2 \sqrt{-\frac{-dg+ch}{h}} \right) \\
 & \quad \sqrt{\left( fh + \frac{d^2 eg - cdfg - cdeh + c^2 fh}{(c+dx)^2} + \frac{dfg + deh - 2cfh}{c+dx} \right)} -
 \end{aligned}$$

$$\left( \int b c C d e h \sqrt{1 - \frac{-d e + c f}{f (c + d x)}} \sqrt{1 - \frac{-d g + c h}{h (c + d x)}} \text{EllipticF} \left[ \right. \right.$$

$$\left. \int \text{ArcSinh} \left[ \frac{\sqrt{-\frac{-d g + c h}{h}}}{\sqrt{c + d x}} \right], \frac{(-d e + c f) h}{f (-d g + c h)} \right] \Big/ \left( (b c - a d) \sqrt{-\frac{-d g + c h}{h}} \right.$$

$$\left. \sqrt{\left( f h + \frac{d^2 e g - c d f g - c d e h + c^2 f h}{(c + d x)^2} + \frac{d f g + d e h - 2 c f h}{c + d x} \right)} \right) -$$

$$\left( \int b^2 c^3 C f h \sqrt{1 - \frac{-d e + c f}{f (c + d x)}} \sqrt{1 - \frac{-d g + c h}{h (c + d x)}} \text{EllipticF} \left[ \right. \right.$$

$$\left. \int \text{ArcSinh} \left[ \frac{\sqrt{-\frac{-d g + c h}{h}}}{\sqrt{c + d x}} \right], \frac{(-d e + c f) h}{f (-d g + c h)} \right] \Big/ \left( (b c - a d)^2 \sqrt{-\frac{-d g + c h}{h}} \right.$$

$$\left. \sqrt{\left( f h + \frac{d^2 e g - c d f g - c d e h + c^2 f h}{(c + d x)^2} + \frac{d f g + d e h - 2 c f h}{c + d x} \right)} \right) +$$

$$\left( \int a b c^2 C d f h \sqrt{1 - \frac{-d e + c f}{f (c + d x)}} \sqrt{1 - \frac{-d g + c h}{h (c + d x)}} \text{EllipticF} \left[ \right. \right.$$

$$\left. \int \text{ArcSinh} \left[ \frac{\sqrt{-\frac{-d g + c h}{h}}}{\sqrt{c + d x}} \right], \frac{(-d e + c f) h}{f (-d g + c h)} \right] \Big/ \left( (b c - a d)^2 \sqrt{-\frac{-d g + c h}{h}} \right.$$

$$\left. \sqrt{\left( f h + \frac{d^2 e g - c d f g - c d e h + c^2 f h}{(c + d x)^2} + \frac{d f g + d e h - 2 c f h}{c + d x} \right)} \right) +$$

$$\begin{aligned}
 & \left( 2 \, i \, b \, c^2 \, C \, f \, h \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \operatorname{EllipticF} \left[ \right. \right. \\
 & \quad \left. \left. i \operatorname{ArcSinh} \left[ \frac{\sqrt{-\frac{-dg+ch}{h}}}{\sqrt{c+dx}} \right], \frac{(-de+cf)h}{f(-dg+ch)} \right] \right) / \left( (bc-ad) \sqrt{-\frac{-dg+ch}{h}} \right. \\
 & \quad \left. \sqrt{\left( fh + \frac{d^2 eg - cdfg - cdeh + c^2 fh}{(c+dx)^2} + \frac{dfg + deh - 2cfh}{c+dx} \right)} \right) + \\
 & \left( i \, A \, b \, d^2 \, f \, h \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \operatorname{EllipticF} \left[ \right. \right. \\
 & \quad \left. \left. i \operatorname{ArcSinh} \left[ \frac{\sqrt{-\frac{-dg+ch}{h}}}{\sqrt{c+dx}} \right], \frac{(-de+cf)h}{f(-dg+ch)} \right] \right) / \left( (bc-ad) \sqrt{-\frac{-dg+ch}{h}} \right. \\
 & \quad \left. \sqrt{\left( fh + \frac{d^2 eg - cdfg - cdeh + c^2 fh}{(c+dx)^2} + \frac{dfg + deh - 2cfh}{c+dx} \right)} \right) + \\
 & \frac{1}{(bc-ad)^3} b^3 c C d^2 e g \left( \left( i \, c \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \right. \right. \\
 & \quad \left. \left. \operatorname{EllipticPi} \left[ \frac{(bc-ad)h}{b(-dg+ch)}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{-\frac{-dg+ch}{h}}}{\sqrt{c+dx}} \right], \frac{(-de+cf)h}{f(-dg+ch)} \right] \right) \right) / \\
 & \left( \sqrt{-\frac{-dg+ch}{h}} \sqrt{\left( fh + \frac{d^2 eg}{(c+dx)^2} - \frac{cdfg}{(c+dx)^2} - \frac{cdeh}{(c+dx)^2} + \frac{c^2 fh}{(c+dx)^2} \right)} \right) +
 \end{aligned}$$

$$\begin{aligned}
 & \left. \left( \frac{dfg}{c+dx} + \frac{deh}{c+dx} - \frac{2cfh}{c+dx} \right) \right) - \left( i a d \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \right. \\
 & \left. \text{EllipticPi} \left[ \frac{(bc-ad)h}{b(-dg+ch)}, i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{-dg+ch}{h}}}{\sqrt{c+dx}} \right], \frac{(-de+cf)h}{f(-dg+ch)} \right] \right) / \\
 & \left( b \sqrt{-\frac{-dg+ch}{h}} \sqrt{\left( fh + \frac{d^2eg}{(c+dx)^2} - \frac{cdfg}{(c+dx)^2} - \frac{cdeh}{(c+dx)^2} + \right. \right. \\
 & \left. \left. \frac{c^2fh}{(c+dx)^2} + \frac{dfg}{c+dx} + \frac{deh}{c+dx} - \frac{2cfh}{c+dx} \right)} \right) - \frac{1}{(bc-ad)^3} \\
 & a b^2 c d^3 e g \left( \left( i c \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \text{EllipticPi} \left[ \frac{(bc-ad)h}{b(-dg+ch)}, \right. \right. \right. \\
 & \left. \left. i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{-dg+ch}{h}}}{\sqrt{c+dx}} \right], \frac{(-de+cf)h}{f(-dg+ch)} \right] \right) / \left( \sqrt{-\frac{-dg+ch}{h}} \sqrt{\left( fh + \right. \right.} \\
 & \left. \left. \frac{d^2eg}{(c+dx)^2} - \frac{cdfg}{(c+dx)^2} - \frac{cdeh}{(c+dx)^2} + \frac{c^2fh}{(c+dx)^2} + \frac{dfg}{c+dx} + \frac{deh}{c+dx} - \frac{2cfh}{c+dx} \right)} \right) - \\
 & \left( i a d \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \text{EllipticPi} \left[ \frac{(bc-ad)h}{b(-dg+ch)}, i \text{ArcSinh} \left[ \right. \right. \right. \\
 & \left. \left. \frac{\sqrt{-\frac{-dg+ch}{h}}}{\sqrt{c+dx}} \right], \frac{(-de+cf)h}{f(-dg+ch)} \right] \right) / \left( b \sqrt{-\frac{-dg+ch}{h}} \sqrt{\left( fh + \frac{d^2eg}{(c+dx)^2} - \right. \right.}
 \end{aligned}$$

$$\left. \left( \frac{c d f g}{(c+dx)^2} - \frac{c d e h}{(c+dx)^2} + \frac{c^2 f h}{(c+dx)^2} + \frac{d f g}{c+dx} + \frac{d e h}{c+dx} - \frac{2 c f h}{c+dx} \right) \right) -$$

$$\frac{1}{(bc-ad)^2} b^2 c d^2 e g \left( \left( i c \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \operatorname{EllipticPi} \left[ \frac{(bc-ad)h}{b(-dg+ch)}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{-\frac{-dg+ch}{h}}}{\sqrt{c+dx}} \right], \frac{(-de+cf)h}{f(-dg+ch)} \right] \right) / \right.$$

$$\left( \sqrt{-\frac{-dg+ch}{h}} \sqrt{\left( f h + \frac{d^2 e g}{(c+dx)^2} - \frac{c d f g}{(c+dx)^2} - \frac{c d e h}{(c+dx)^2} + \frac{c^2 f h}{(c+dx)^2} + \frac{d f g}{c+dx} + \frac{d e h}{c+dx} - \frac{2 c f h}{c+dx} \right)} \right) - \left( i a d \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \operatorname{EllipticPi} \left[ \frac{(bc-ad)h}{b(-dg+ch)}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{-\frac{-dg+ch}{h}}}{\sqrt{c+dx}} \right], \frac{(-de+cf)h}{f(-dg+ch)} \right] \right) / \right.$$

$$\left( b \sqrt{-\frac{-dg+ch}{h}} \sqrt{\left( f h + \frac{d^2 e g}{(c+dx)^2} - \frac{c d f g}{(c+dx)^2} - \frac{c d e h}{(c+dx)^2} + \frac{c^2 f h}{(c+dx)^2} + \frac{d f g}{c+dx} + \frac{d e h}{c+dx} - \frac{2 c f h}{c+dx} \right)} \right) \right) - \frac{1}{(bc-ad)^3}$$

$$b^3 c^2 c d f g \left( \left( i c \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \operatorname{EllipticPi} \left[ \frac{(bc-ad)h}{b(-dg+ch)}, \right. \right.$$

$$\begin{aligned}
 & \left( i \operatorname{ArcSinh} \left[ \frac{\sqrt{-\frac{dg+ch}{h}}}{\sqrt{c+dx}}, \frac{(-de+cf)h}{f(-dg+ch)} \right] \right) / \left( \sqrt{-\frac{dg+ch}{h}} \sqrt{\left( fh + \right. \right.} \\
 & \left. \left. \frac{d^2 eg}{(c+dx)^2} - \frac{cdfg}{(c+dx)^2} - \frac{cdeh}{(c+dx)^2} + \frac{c^2 fh}{(c+dx)^2} + \frac{dfg}{c+dx} + \frac{deh}{c+dx} - \frac{2cfh}{c+dx} \right) \right) - \\
 & \left( i a d \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \operatorname{EllipticPi} \left[ \frac{(bc-ad)h}{b(-dg+ch)}, i \operatorname{ArcSinh} \left[ \right. \right. \right. \\
 & \left. \left. \left. \frac{\sqrt{-\frac{dg+ch}{h}}}{\sqrt{c+dx}}, \frac{(-de+cf)h}{f(-dg+ch)} \right] \right] \right) / \left( b \sqrt{-\frac{dg+ch}{h}} \sqrt{\left( fh + \frac{d^2 eg}{(c+dx)^2} - \right. \right.} \right. \\
 & \left. \left. \frac{cdfg}{(c+dx)^2} - \frac{cdeh}{(c+dx)^2} + \frac{c^2 fh}{(c+dx)^2} + \frac{dfg}{c+dx} + \frac{deh}{c+dx} - \frac{2cfh}{c+dx} \right) \right) + \\
 & \frac{1}{(bc-a)^3} a b^2 c C d^2 f g \left( \left( i c \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \right. \right. \\
 & \left. \left. \operatorname{EllipticPi} \left[ \frac{(bc-ad)h}{b(-dg+ch)}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{-\frac{dg+ch}{h}}}{\sqrt{c+dx}}, \frac{(-de+cf)h}{f(-dg+ch)} \right] \right] \right) / \right. \\
 & \left. \left( \sqrt{-\frac{dg+ch}{h}} \sqrt{\left( fh + \frac{d^2 eg}{(c+dx)^2} - \frac{cdfg}{(c+dx)^2} - \frac{cdeh}{(c+dx)^2} + \frac{c^2 fh}{(c+dx)^2} + \right. \right.} \right. \\
 & \left. \left. \frac{dfg}{c+dx} + \frac{deh}{c+dx} - \frac{2cfh}{c+dx} \right) \right) - \left( i a d \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \right)
 \end{aligned}$$

$$\left. \text{EllipticPi}\left[\frac{(bc-ad)h}{b(-dg+ch)}, \text{i ArcSinh}\left[\frac{\sqrt{-\frac{dg+ch}{h}}}{\sqrt{c+dx}}\right], \frac{(-de+cf)h}{f(-dg+ch)}\right]\right/$$

$$\left( b \sqrt{-\frac{dg+ch}{h}} \sqrt{\left( fh + \frac{d^2eg}{(c+dx)^2} - \frac{cdfg}{(c+dx)^2} - \frac{cdeh}{(c+dx)^2} + \frac{c^2fh}{(c+dx)^2} + \frac{dfg}{c+dx} + \frac{deh}{c+dx} - \frac{2cfh}{c+dx} \right)} \right) + \frac{1}{(bc-ad)^2}$$

$$b^2 c C d f g \left( \left( \text{i c} \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \text{EllipticPi}\left[\frac{(bc-ad)h}{b(-dg+ch)}, \text{i ArcSinh}\left[\frac{\sqrt{-\frac{dg+ch}{h}}}{\sqrt{c+dx}}\right], \frac{(-de+cf)h}{f(-dg+ch)}\right]\right) / \left( \sqrt{-\frac{dg+ch}{h}} \sqrt{\left( fh + \frac{d^2eg}{(c+dx)^2} - \frac{cdfg}{(c+dx)^2} - \frac{cdeh}{(c+dx)^2} + \frac{c^2fh}{(c+dx)^2} + \frac{dfg}{c+dx} + \frac{deh}{c+dx} - \frac{2cfh}{c+dx} \right)} \right) - \left( \text{i a d} \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \text{EllipticPi}\left[\frac{(bc-ad)h}{b(-dg+ch)}, \text{i ArcSinh}\left[\frac{\sqrt{-\frac{dg+ch}{h}}}{\sqrt{c+dx}}\right], \frac{(-de+cf)h}{f(-dg+ch)}\right]\right) / \left( b \sqrt{-\frac{dg+ch}{h}} \sqrt{\left( fh + \frac{d^2eg}{(c+dx)^2} - \frac{cdfg}{(c+dx)^2} - \frac{cdeh}{(c+dx)^2} + \frac{c^2fh}{(c+dx)^2} + \frac{dfg}{c+dx} + \frac{deh}{c+dx} - \frac{2cfh}{c+dx} \right)} \right) \right) -$$

$$\begin{aligned}
 & \frac{1}{(bc-ad)^3} b^3 c^2 C d e h \left( \left( i c \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \operatorname{EllipticPi} \left[ \right. \right. \right. \\
 & \left. \left. \left. \frac{(bc-ad)h}{b(-dg+ch)}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{-\frac{-dg+ch}{h}}}{\sqrt{c+dx}} \right], \frac{(-de+cf)h}{f(-dg+ch)} \right] \right) / \right. \\
 & \left( \sqrt{-\frac{-dg+ch}{h}} \sqrt{\left( fh + \frac{d^2 eg}{(c+dx)^2} - \frac{cdfg}{(c+dx)^2} - \frac{cdeh}{(c+dx)^2} + \frac{c^2 fh}{(c+dx)^2} + \right. \right. \\
 & \left. \left. \frac{dfg}{c+dx} + \frac{deh}{c+dx} - \frac{2cfh}{c+dx} \right)} \right) - \left( i a d \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \right. \\
 & \left. \operatorname{EllipticPi} \left[ \frac{(bc-ad)h}{b(-dg+ch)}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{-\frac{-dg+ch}{h}}}{\sqrt{c+dx}} \right], \frac{(-de+cf)h}{f(-dg+ch)} \right] \right) / \right. \\
 & \left( b \sqrt{-\frac{-dg+ch}{h}} \sqrt{\left( fh + \frac{d^2 eg}{(c+dx)^2} - \frac{cdfg}{(c+dx)^2} - \frac{cdeh}{(c+dx)^2} + \right. \right. \\
 & \left. \left. \frac{c^2 fh}{(c+dx)^2} + \frac{dfg}{c+dx} + \frac{deh}{c+dx} - \frac{2cfh}{c+dx} \right)} \right) \left. \right) + \frac{1}{(bc-ad)^3} \\
 & a b^2 c C d^2 e h \left( \left( i c \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \operatorname{EllipticPi} \left[ \frac{(bc-ad)h}{b(-dg+ch)}, \right. \right. \right. \\
 & \left. \left. \left. i \operatorname{ArcSinh} \left[ \frac{\sqrt{-\frac{-dg+ch}{h}}}{\sqrt{c+dx}} \right], \frac{(-de+cf)h}{f(-dg+ch)} \right] \right) / \left( \sqrt{-\frac{-dg+ch}{h}} \sqrt{\left( fh + \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left. \left( \frac{d^2 e g}{(c+dx)^2} - \frac{c d f g}{(c+dx)^2} - \frac{c d e h}{(c+dx)^2} + \frac{c^2 f h}{(c+dx)^2} + \frac{d f g}{c+dx} + \frac{d e h}{c+dx} - \frac{2 c f h}{c+dx} \right) \right) - \\
 & \left( i a d \sqrt{1 - \frac{-d e + c f}{f (c+dx)}} \sqrt{1 - \frac{-d g + c h}{h (c+dx)}} \text{EllipticPi} \left[ \frac{(b c - a d) h}{b (-d g + c h)}, i \text{ArcSinh} \left[ \right. \right. \right. \\
 & \left. \left. \left. \frac{\sqrt{\frac{-d g + c h}{h}}}{\sqrt{c+dx}} \right], \frac{(-d e + c f) h}{f (-d g + c h)} \right] \right) / \left( b \sqrt{\frac{-d g + c h}{h}} \sqrt{\left( f h + \frac{d^2 e g}{(c+dx)^2} - \right. \right. \right. \\
 & \left. \left. \left. \frac{c d f g}{(c+dx)^2} - \frac{c d e h}{(c+dx)^2} + \frac{c^2 f h}{(c+dx)^2} + \frac{d f g}{c+dx} + \frac{d e h}{c+dx} - \frac{2 c f h}{c+dx} \right) \right) \right) + \\
 & \frac{1}{(b c - a d)^2} b^2 c d e h \left( \left( i c \sqrt{1 - \frac{-d e + c f}{f (c+dx)}} \sqrt{1 - \frac{-d g + c h}{h (c+dx)}} \text{EllipticPi} \left[ \right. \right. \right. \\
 & \left. \left. \left. \frac{(b c - a d) h}{b (-d g + c h)}, i \text{ArcSinh} \left[ \frac{\sqrt{\frac{-d g + c h}{h}}}{\sqrt{c+dx}} \right], \frac{(-d e + c f) h}{f (-d g + c h)} \right] \right) / \right. \\
 & \left. \left( \sqrt{\frac{-d g + c h}{h}} \sqrt{\left( f h + \frac{d^2 e g}{(c+dx)^2} - \frac{c d f g}{(c+dx)^2} - \frac{c d e h}{(c+dx)^2} + \frac{c^2 f h}{(c+dx)^2} + \right. \right. \right. \\
 & \left. \left. \left. \frac{d f g}{c+dx} + \frac{d e h}{c+dx} - \frac{2 c f h}{c+dx} \right) \right) - \left( i a d \sqrt{1 - \frac{-d e + c f}{f (c+dx)}} \sqrt{1 - \frac{-d g + c h}{h (c+dx)}} \right. \right. \\
 & \left. \left. \text{EllipticPi} \left[ \frac{(b c - a d) h}{b (-d g + c h)}, i \text{ArcSinh} \left[ \frac{\sqrt{\frac{-d g + c h}{h}}}{\sqrt{c+dx}} \right], \frac{(-d e + c f) h}{f (-d g + c h)} \right] \right) / \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left( b \sqrt{-\frac{dg+ch}{h}} \sqrt{\left( fh + \frac{d^2 eg}{(c+dx)^2} - \frac{cdfg}{(c+dx)^2} - \frac{cdeh}{(c+dx)^2} + \right.} \right. \\
 & \quad \left. \left. \frac{c^2 fh}{(c+dx)^2} + \frac{dfg}{c+dx} + \frac{deh}{c+dx} - \frac{2cfh}{c+dx} \right) \right) + \frac{1}{(bc-ad)^3} \\
 & b^3 c^3 C f h \left( \left( i c \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \operatorname{EllipticPi}\left[\frac{(bc-ad)h}{b(-dg+ch)}, \right. \right. \right. \\
 & \quad \left. \left. \left. i \operatorname{ArcSinh}\left[\frac{\sqrt{-\frac{dg+ch}{h}}}{\sqrt{c+dx}}\right], \frac{(-de+cf)h}{f(-dg+ch)}\right] \right) / \left( \sqrt{-\frac{dg+ch}{h}} \sqrt{\left( fh + \right.} \right. \right. \\
 & \quad \left. \left. \frac{d^2 eg}{(c+dx)^2} - \frac{cdfg}{(c+dx)^2} - \frac{cdeh}{(c+dx)^2} + \frac{c^2 fh}{(c+dx)^2} + \frac{dfg}{c+dx} + \frac{deh}{c+dx} - \frac{2cfh}{c+dx} \right) \right) - \\
 & \left( i a d \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \operatorname{EllipticPi}\left[\frac{(bc-ad)h}{b(-dg+ch)}, i \operatorname{ArcSinh}\left[ \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{\sqrt{-\frac{dg+ch}{h}}}{\sqrt{c+dx}}\right], \frac{(-de+cf)h}{f(-dg+ch)}\right] \right) / \left( b \sqrt{-\frac{dg+ch}{h}} \sqrt{\left( fh + \frac{d^2 eg}{(c+dx)^2} - \right.} \right. \\
 & \quad \left. \left. \frac{cdfg}{(c+dx)^2} - \frac{cdeh}{(c+dx)^2} + \frac{c^2 fh}{(c+dx)^2} + \frac{dfg}{c+dx} + \frac{deh}{c+dx} - \frac{2cfh}{c+dx} \right) \right) - \\
 & \frac{1}{(bc-ad)^3} a b^2 c^2 C d f h \left( \left( i c \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left. \text{EllipticPi} \left[ \frac{(bc-ad)h}{b(-dg+ch)}, i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{dg+ch}{h}}}{\sqrt{c+dx}} \right], \frac{(-de+cf)h}{f(-dg+ch)} \right] \right/ \\
 & \left( \sqrt{-\frac{dg+ch}{h}} \sqrt{\left( fh + \frac{d^2 eg}{(c+dx)^2} - \frac{cdfg}{(c+dx)^2} - \frac{cdeh}{(c+dx)^2} + \frac{c^2 fh}{(c+dx)^2} \right.} \right. \\
 & \left. \left. + \frac{dfg}{c+dx} + \frac{deh}{c+dx} - \frac{2cfh}{c+dx} \right) \right) - \left( i ad \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \right. \\
 & \left. \text{EllipticPi} \left[ \frac{(bc-ad)h}{b(-dg+ch)}, i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{dg+ch}{h}}}{\sqrt{c+dx}} \right], \frac{(-de+cf)h}{f(-dg+ch)} \right] \right/ \\
 & \left( b \sqrt{-\frac{dg+ch}{h}} \sqrt{\left( fh + \frac{d^2 eg}{(c+dx)^2} - \frac{cdfg}{(c+dx)^2} - \frac{cdeh}{(c+dx)^2} + \right.} \right. \\
 & \left. \left. \frac{c^2 fh}{(c+dx)^2} + \frac{dfg}{c+dx} + \frac{deh}{c+dx} - \frac{2cfh}{c+dx} \right) \right) - \frac{1}{(bc-ad)^2} \\
 & 2b^2 c^2 c f h \left( \left( i c \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \text{EllipticPi} \left[ \frac{(bc-ad)h}{b(-dg+ch)}, \right. \right. \right. \\
 & \left. \left. i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{dg+ch}{h}}}{\sqrt{c+dx}} \right], \frac{(-de+cf)h}{f(-dg+ch)} \right] \right) / \left( \sqrt{-\frac{dg+ch}{h}} \sqrt{\left( fh + \right.} \right. \\
 & \left. \left. \frac{d^2 eg}{(c+dx)^2} - \frac{cdfg}{(c+dx)^2} - \frac{cdeh}{(c+dx)^2} + \frac{c^2 fh}{(c+dx)^2} + \frac{dfg}{c+dx} + \frac{deh}{c+dx} - \frac{2cfh}{c+dx} \right) \right) -
 \end{aligned}$$

$$\left( i a d \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \operatorname{EllipticPi} \left[ \frac{(bc-ad)h}{b(-dg+ch)}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{-\frac{-dg+ch}{h}}}{\sqrt{c+dx}} \right], \frac{(-de+cf)h}{f(-dg+ch)} \right] \right) / \left( b \sqrt{-\frac{-dg+ch}{h}} \sqrt{\left( fh + \frac{d^2 eg}{(c+dx)^2} - \frac{cdfg}{(c+dx)^2} - \frac{cdeh}{(c+dx)^2} + \frac{c^2 fh}{(c+dx)^2} + \frac{dfg}{c+dx} + \frac{deh}{c+dx} - \frac{2cfh}{c+dx} \right)} \right) - \left( \frac{cdfg}{(c+dx)^2} - \frac{cdeh}{(c+dx)^2} + \frac{c^2 fh}{(c+dx)^2} + \frac{dfg}{c+dx} + \frac{deh}{c+dx} - \frac{2cfh}{c+dx} \right) \right) - \frac{1}{(bc-ad)^2} A b^2 d^2 f h \left( i c \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \operatorname{EllipticPi} \left[ \frac{(bc-ad)h}{b(-dg+ch)}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{-\frac{-dg+ch}{h}}}{\sqrt{c+dx}} \right], \frac{(-de+cf)h}{f(-dg+ch)} \right] \right) / \left( \sqrt{-\frac{-dg+ch}{h}} \sqrt{\left( fh + \frac{d^2 eg}{(c+dx)^2} - \frac{cdfg}{(c+dx)^2} - \frac{cdeh}{(c+dx)^2} + \frac{c^2 fh}{(c+dx)^2} + \frac{dfg}{c+dx} + \frac{deh}{c+dx} - \frac{2cfh}{c+dx} \right)} \right) - \left( i a d \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \operatorname{EllipticPi} \left[ \frac{(bc-ad)h}{b(-dg+ch)}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{-\frac{-dg+ch}{h}}}{\sqrt{c+dx}} \right], \frac{(-de+cf)h}{f(-dg+ch)} \right] \right) / \left( b \sqrt{-\frac{-dg+ch}{h}} \sqrt{\left( fh + \frac{d^2 eg}{(c+dx)^2} - \frac{cdfg}{(c+dx)^2} - \frac{cdeh}{(c+dx)^2} + \frac{c^2 fh}{(c+dx)^2} + \frac{dfg}{c+dx} + \frac{deh}{c+dx} - \frac{2cfh}{c+dx} \right)} \right)$$

$$\left. \left( \frac{c^2 f h}{(c+dx)^2} + \frac{d f g}{c+dx} + \frac{d e h}{c+dx} - \frac{2 c f h}{c+dx} \right) \right) + \frac{1}{b c - a d}$$

$$b c C f h \left( \left( i c \sqrt{1 - \frac{-d e + c f}{f (c+dx)}} \sqrt{1 - \frac{-d g + c h}{h (c+dx)}} \operatorname{EllipticPi} \left[ \frac{(b c - a d) h}{b (-d g + c h)}, \right. \right. \right.$$

$$\left. \left. \left. i \operatorname{ArcSinh} \left[ \frac{\sqrt{-\frac{-d g + c h}{h}}}{\sqrt{c+dx}} \right], \frac{(-d e + c f) h}{f (-d g + c h)} \right] \right) / \left( \sqrt{-\frac{-d g + c h}{h}} \sqrt{f h +} \right. \right.$$

$$\left. \left. \frac{d^2 e g}{(c+dx)^2} - \frac{c d f g}{(c+dx)^2} - \frac{c d e h}{(c+dx)^2} + \frac{c^2 f h}{(c+dx)^2} + \frac{d f g}{c+dx} + \frac{d e h}{c+dx} - \frac{2 c f h}{c+dx} \right) \right) -$$

$$\left( i a d \sqrt{1 - \frac{-d e + c f}{f (c+dx)}} \sqrt{1 - \frac{-d g + c h}{h (c+dx)}} \operatorname{EllipticPi} \left[ \frac{(b c - a d) h}{b (-d g + c h)}, i \operatorname{ArcSinh} \left[ \right. \right. \right.$$

$$\left. \left. \left. \frac{\sqrt{-\frac{-d g + c h}{h}}}{\sqrt{c+dx}} \right], \frac{(-d e + c f) h}{f (-d g + c h)} \right] \right) / \left( b \sqrt{-\frac{-d g + c h}{h}} \sqrt{f h + \frac{d^2 e g}{(c+dx)^2} -} \right.$$

$$\left. \left. \frac{c d f g}{(c+dx)^2} - \frac{c d e h}{(c+dx)^2} + \frac{c^2 f h}{(c+dx)^2} + \frac{d f g}{c+dx} + \frac{d e h}{c+dx} - \frac{2 c f h}{c+dx} \right) \right) + \frac{1}{b c - a d}$$

$$a c d f h \left( \left( i c \sqrt{1 - \frac{-d e + c f}{f (c+dx)}} \sqrt{1 - \frac{-d g + c h}{h (c+dx)}} \operatorname{EllipticPi} \left[ \frac{(b c - a d) h}{b (-d g + c h)}, \right. \right. \right.$$

$$\left. \left. \left. i \operatorname{ArcSinh} \left[ \frac{\sqrt{-\frac{-d g + c h}{h}}}{\sqrt{c+dx}} \right], \frac{(-d e + c f) h}{f (-d g + c h)} \right] \right) / \left( \sqrt{-\frac{-d g + c h}{h}} \sqrt{f h +} \right.$$

$$\left( \frac{d^2 e g}{(c+dx)^2} - \frac{c d f g}{(c+dx)^2} - \frac{c d e h}{(c+dx)^2} + \frac{c^2 f h}{(c+dx)^2} + \frac{d f g}{c+dx} + \frac{d e h}{c+dx} - \frac{2 c f h}{c+dx} \right) -$$

$$\left( i a d \sqrt{1 - \frac{-d e + c f}{f (c+dx)}} \sqrt{1 - \frac{-d g + c h}{h (c+dx)}} \text{EllipticPi} \left[ \frac{(b c - a d) h}{b (-d g + c h)}, i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{-d g + c h}{h}}}{\sqrt{c+dx}} \right], \frac{(-d e + c f) h}{f (-d g + c h)} \right] \right) / \left( b \sqrt{-\frac{-d g + c h}{h}} \sqrt{\left( f h + \frac{d^2 e g}{(c+dx)^2} - \frac{c d f g}{(c+dx)^2} - \frac{c d e h}{(c+dx)^2} + \frac{c^2 f h}{(c+dx)^2} + \frac{d f g}{c+dx} + \frac{d e h}{c+dx} - \frac{2 c f h}{c+dx} \right)} \right)$$

$$\left( \left( -b c C f h - a C d f h - \frac{b c C d^2 e g}{(c+dx)^2} + \frac{a C d^3 e g}{(c+dx)^2} + \frac{b c^2 C d f g}{(c+dx)^2} - \frac{a c C d^2 f g}{(c+dx)^2} + \frac{b c^2 C d e h}{(c+dx)^2} - \frac{a c C d^2 e h}{(c+dx)^2} - \frac{b c^3 C f h}{(c+dx)^2} + \frac{a c^2 C d f h}{(c+dx)^2} + \frac{b C d^2 e g}{c+dx} - \frac{b c C d f g}{c+dx} - \frac{b c C d e h}{c+dx} + \frac{2 b c^2 C f h}{c+dx} + \frac{A b d^2 f h}{c+dx} \right) \sqrt{e + \frac{(c+dx) \left( f - \frac{c f}{c+dx} \right)}{d}} \sqrt{g + \frac{(c+dx) \left( h - \frac{c h}{c+dx} \right)}{d}} \right)$$

**Problem 30: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{A + C x^2}{(a + b x)^2 \sqrt{c + d x} \sqrt{e + f x} \sqrt{g + h x}} dx$$

Optimal (type 4, 738 leaves, 12 steps):

$$\begin{aligned}
 & - \frac{(Ab^2 + a^2C) \sqrt{c+dx} \sqrt{e+fx} \sqrt{g+hx}}{(bc-ad)(be-af)(bg-ah)(a+bx)} + \left( \left( Ab + \frac{a^2C}{b} \right) \sqrt{f} \sqrt{-de+cf} \right. \\
 & \quad \left. \sqrt{\frac{d(e+fx)}{de-cf}} \sqrt{g+hx} \operatorname{EllipticE} \left[ \operatorname{ArcSin} \left[ \frac{\sqrt{f} \sqrt{c+dx}}{\sqrt{-de+cf}} \right], \frac{(de-cf)h}{f(dg-ch)} \right] \right) / \\
 & \quad \left( (bc-ad)(be-af)(bg-ah) \sqrt{e+fx} \sqrt{\frac{d(g+hx)}{dg-ch}} \right) + \\
 & \quad \left( \sqrt{-de+cf} (a^2Cdf - 2abc(de+cf) + b^2(2cCe - Adf)) \sqrt{\frac{d(e+fx)}{de-cf}} \right. \\
 & \quad \left. \sqrt{\frac{d(g+hx)}{dg-ch}} \operatorname{EllipticF} \left[ \operatorname{ArcSin} \left[ \frac{\sqrt{f} \sqrt{c+dx}}{\sqrt{-de+cf}} \right], \frac{(de-cf)h}{f(dg-ch)} \right] \right) / \\
 & \quad (b^2d(bc-ad) \sqrt{f} (be-af) \sqrt{e+fx} \sqrt{g+hx}) - \\
 & \quad \left( \sqrt{-de+cf} (a^4Cdfh - Ab^4(deg+cfg+ceh) - 2a^3bc(dfg+deh+cfh) - 2ab^3 \right. \\
 & \quad \left. (2cCeg - Adfg - Adeh - Acfh) - 3a^2b^2(Adfh - C(deg+cfg+ceh))) \right) \sqrt{\frac{d(e+fx)}{de-cf}} \\
 & \quad \left. \sqrt{\frac{d(g+hx)}{dg-ch}} \operatorname{EllipticPi} \left[ -\frac{b(de-cf)}{(bc-ad)f}, \operatorname{ArcSin} \left[ \frac{\sqrt{f} \sqrt{c+dx}}{\sqrt{-de+cf}} \right], \frac{(de-cf)h}{f(dg-ch)} \right] \right) / \\
 & \quad (b^2(bc-ad)^2 \sqrt{f} (be-af)(bg-ah) \sqrt{e+fx} \sqrt{g+hx})
 \end{aligned}$$

Result (type 4, 17743 leaves):

$$\begin{aligned}
 & \frac{(-Ab^2 - a^2C) \sqrt{c+dx} \sqrt{e+fx} \sqrt{g+hx}}{(bc-ad)(be-af)(bg-ah)(a+bx)} - \\
 & \frac{1}{d(-bc+ad)(-be+af)(-bg+ah)} \left( \frac{(Ab^2 + a^2C)(c+dx)^{3/2} \left( f + \frac{de}{c+dx} - \frac{cf}{c+dx} \right) \left( h + \frac{dg}{c+dx} - \frac{ch}{c+dx} \right)}{b \sqrt{e + \frac{(c+dx)(f - \frac{cf}{c+dx})}{d}} \sqrt{g + \frac{(c+dx)(h - \frac{ch}{c+dx})}{d}}} \right. \\
 & \quad \left. \left( (c+dx) \left( -b + \frac{bc}{c+dx} - \frac{ad}{c+dx} \right) \sqrt{f + \frac{de}{c+dx} - \frac{cf}{c+dx}} \sqrt{h + \frac{dg}{c+dx} - \frac{ch}{c+dx}} \right) \right)
 \end{aligned}$$

$$\sqrt{\left( fh + \frac{d^2 eg}{(c+dx)^2} - \frac{cdfg}{(c+dx)^2} - \frac{cdeh}{(c+dx)^2} + \frac{c^2 fh}{(c+dx)^2} + \frac{dfg}{c+dx} + \frac{deh}{c+dx} - \frac{2cfh}{c+dx} \right)}$$

$$\left( \left( (bc-ad) (2b^2 C e g^2 - 2ab C f g^2 + Ab^2 f g h + a^2 C f g h + Ab^2 e h^2 - a^2 C e h^2 - 2aAbfh^2) \right) / \left( b(bg-ah) \sqrt{f + \frac{de}{c+dx} - \frac{cf}{c+dx}} \sqrt{h + \frac{dg}{c+dx} - \frac{ch}{c+dx}} \right) \right) -$$

$$\frac{(Ab^2 + a^2 C) (de - cf) \sqrt{h + \frac{dg}{c+dx} - \frac{ch}{c+dx}}}{b \sqrt{f + \frac{de}{c+dx} - \frac{cf}{c+dx}}} - \left( (-4ab^3 c C e g - Ab^4 d e g + 3a^2 b^2 C d e g - Ab^4 c f g + 3a^2 b^2 c C f g + 2aAb^3 d f g - 2a^3 b C d f g - Ab^4 c e h + 3a^2 b^2 c C e h + 2aAb^3 d e h - 2a^3 b C d e h + 2aAb^3 c f h - 2a^3 b c C f h - 3a^2 Ab^2 d f h + a^4 C d f h) \right.$$

$$\left. \sqrt{h + \frac{dg}{c+dx} - \frac{ch}{c+dx}} / \left( b(bg-ah) \left( b - \frac{bc}{c+dx} + \frac{ad}{c+dx} \right) \sqrt{f + \frac{de}{c+dx} - \frac{cf}{c+dx}} \right) \right)$$

$$\left( \left( i Ab^2 d^2 e f g \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \left( \text{EllipticE} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{-dg+ch}{h}}}{\sqrt{c+dx}} \right] \right), \right. \right. \right.$$

$$\left. \left. \frac{(-de+cf)h}{f(-dg+ch)} \right] - \text{EllipticF} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{-dg+ch}{h}}}{\sqrt{c+dx}} \right], \frac{(-de+cf)h}{f(-dg+ch)} \right] \right) \right) /$$

$$\left( (bc-ad) (-de+cf) \sqrt{-\frac{-dg+ch}{h}} \sqrt{\left( fh + \frac{d^2 eg - cdfg - cdeh + c^2 fh}{(c+dx)^2} + \frac{dfg + deh - 2cfh}{c+dx} \right)} \right) + \left( i a^2 C d^2 e f g \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \right.$$

$$\begin{aligned}
 & \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \left( \text{EllipticE} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{-dg+ch}{h}}}{\sqrt{c+dx}} \right], \frac{(-de+cf)h}{f(-dg+ch)} \right] - \right. \\
 & \left. \text{EllipticF} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{-dg+ch}{h}}}{\sqrt{c+dx}} \right], \frac{(-de+cf)h}{f(-dg+ch)} \right] \right) / \left( (bc-ad)(-de+cf) \right) \\
 & \sqrt{-\frac{-dg+ch}{h}} \sqrt{\left( fh + \frac{d^2eg - cdfg - cdeh + c^2fh}{(c+dx)^2} + \frac{dfg+deh-2cfh}{c+dx} \right)} - \\
 & \left( i Ab^2cdf^2g \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \left( \text{EllipticE} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{-dg+ch}{h}}}{\sqrt{c+dx}} \right], \right. \right. \right. \\
 & \left. \left. \left. \frac{(-de+cf)h}{f(-dg+ch)} \right] - \text{EllipticF} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{-dg+ch}{h}}}{\sqrt{c+dx}} \right], \frac{(-de+cf)h}{f(-dg+ch)} \right] \right) \right) / \\
 & \left( (bc-ad)(-de+cf) \sqrt{-\frac{-dg+ch}{h}} \sqrt{\left( fh + \frac{d^2eg - cdfg - cdeh + c^2fh}{(c+dx)^2} + \right. \right. \\
 & \left. \left. \frac{dfg+deh-2cfh}{c+dx} \right)} - \left( i a^2cCdf^2g \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \right. \right. \\
 & \left. \left. \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \left( \text{EllipticE} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{-dg+ch}{h}}}{\sqrt{c+dx}} \right], \frac{(-de+cf)h}{f(-dg+ch)} \right] - \right. \right. \right. \\
 & \left. \left. \left. \text{EllipticF} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{-dg+ch}{h}}}{\sqrt{c+dx}} \right], \frac{(-de+cf)h}{f(-dg+ch)} \right] \right) \right) / \left( (bc-ad)(-de+cf) \right)
 \end{aligned}$$

$$\begin{aligned}
 & \sqrt{-\frac{-dg+ch}{h}} \sqrt{\left( fh + \frac{d^2eg - cdfg - cdeh + c^2fh}{(c+dx)^2} + \frac{dfg+deh-2cfh}{c+dx} \right)} - \\
 & \left( \frac{1}{h} \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \left( \text{EllipticE} \left[ \frac{1}{h} \text{ArcSinh} \left[ \frac{\sqrt{-\frac{-dg+ch}{h}}}{\sqrt{c+dx}} \right], \right. \right. \right. \\
 & \left. \left. \left. \frac{(-de+cf)h}{f(-dg+ch)} \right] - \text{EllipticF} \left[ \frac{1}{h} \text{ArcSinh} \left[ \frac{\sqrt{-\frac{-dg+ch}{h}}}{\sqrt{c+dx}} \right], \frac{(-de+cf)h}{f(-dg+ch)} \right] \right) \right) / \\
 & \left( (bc-ad)(-de+cf) \sqrt{-\frac{-dg+ch}{h}} \sqrt{\left( fh + \frac{d^2eg - cdfg - cdeh + c^2fh}{(c+dx)^2} + \right. \right. \\
 & \left. \left. \frac{dfg+deh-2cfh}{c+dx} \right) \right) - \left( \frac{1}{h} \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \right. \\
 & \left. \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \left( \text{EllipticE} \left[ \frac{1}{h} \text{ArcSinh} \left[ \frac{\sqrt{-\frac{-dg+ch}{h}}}{\sqrt{c+dx}} \right], \frac{(-de+cf)h}{f(-dg+ch)} \right] - \right. \right. \\
 & \left. \left. \text{EllipticF} \left[ \frac{1}{h} \text{ArcSinh} \left[ \frac{\sqrt{-\frac{-dg+ch}{h}}}{\sqrt{c+dx}} \right], \frac{(-de+cf)h}{f(-dg+ch)} \right] \right) \right) / \left( (bc-ad)(-de+cf) \right. \\
 & \left. \sqrt{-\frac{-dg+ch}{h}} \sqrt{\left( fh + \frac{d^2eg - cdfg - cdeh + c^2fh}{(c+dx)^2} + \frac{dfg+deh-2cfh}{c+dx} \right) \right) + \\
 & \left( \frac{1}{h} \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \left( \text{EllipticE} \left[ \frac{1}{h} \text{ArcSinh} \left[ \frac{\sqrt{-\frac{-dg+ch}{h}}}{\sqrt{c+dx}} \right], \right. \right. \right.
 \end{aligned}$$

$$\left. \left. \left. \left. \frac{(-de+cf)h}{f(-dg+ch)} \right] - \text{EllipticF} \left[ \text{i ArcSinh} \left[ \frac{\sqrt{-\frac{dg+ch}{h}}}{\sqrt{c+dx}} \right], \frac{(-de+cf)h}{f(-dg+ch)} \right] \right) \right) \right) /$$

$$\left( (bc-ad)(-de+cf) \sqrt{-\frac{dg+ch}{h}} \sqrt{\left( fh + \frac{d^2eg - cd fg - cdeh + c^2fh}{(c+dx)^2} + \right.} \right.$$

$$\left. \left. \frac{dfg+deh-2cfh}{c+dx} \right) \right) + \left( \text{i} a^2 c^2 C f^2 h \sqrt{1 - \frac{de+cf}{f(c+dx)}} \right.$$

$$\left. \left. \sqrt{1 - \frac{dg+ch}{h(c+dx)}} \left( \text{EllipticE} \left[ \text{i ArcSinh} \left[ \frac{\sqrt{-\frac{dg+ch}{h}}}{\sqrt{c+dx}} \right], \frac{(-de+cf)h}{f(-dg+ch)} \right] - \right. \right. \right.$$

$$\left. \left. \left. \left. \text{EllipticF} \left[ \text{i ArcSinh} \left[ \frac{\sqrt{-\frac{dg+ch}{h}}}{\sqrt{c+dx}} \right], \frac{(-de+cf)h}{f(-dg+ch)} \right] \right) \right) \right) / \left( (bc-ad)(-de+cf) \right.$$

$$\left. \left. \sqrt{-\frac{dg+ch}{h}} \sqrt{\left( fh + \frac{d^2eg - cd fg - cdeh + c^2fh}{(c+dx)^2} + \frac{dfg+deh-2cfh}{c+dx} \right)} \right) -$$

$$\left( \text{i} A b^3 d^2 e g \sqrt{1 - \frac{de+cf}{f(c+dx)}} \sqrt{1 - \frac{dg+ch}{h(c+dx)}} \text{EllipticF} \left[ \right. \right.$$

$$\left. \left. \text{i ArcSinh} \left[ \frac{\sqrt{-\frac{dg+ch}{h}}}{\sqrt{c+dx}} \right], \frac{(-de+cf)h}{f(-dg+ch)} \right] \right) / \left( (bc-ad)^2 \sqrt{-\frac{dg+ch}{h}} \right.$$

$$\left. \left. \sqrt{\left( fh + \frac{d^2eg - cd fg - cdeh + c^2fh}{(c+dx)^2} + \frac{dfg+deh-2cfh}{c+dx} \right)} \right) -$$

$$\left( i a^2 b C d^2 e g \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \text{EllipticF}\left[ \right. \right.$$

$$\left. \left. i \text{ArcSinh}\left[ \frac{\sqrt{\frac{-dg+ch}{h}}}{\sqrt{c+dx}} \right], \frac{(-de+cf)h}{f(-dg+ch)} \right] \right) / \left( (bc-ad)^2 \sqrt{\frac{-dg+ch}{h}} \right.$$

$$\left. \sqrt{\left( fh + \frac{d^2 eg - cdfg - cdeh + c^2 fh}{(c+dx)^2} + \frac{dfg+deh-2cfh}{c+dx} \right)} \right) -$$

$$\left( 2 i b^2 c C e g \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \text{EllipticF}\left[ \right. \right.$$

$$\left. \left. i \text{ArcSinh}\left[ \frac{\sqrt{\frac{-dg+ch}{h}}}{\sqrt{c+dx}} \right], \frac{(-de+cf)h}{f(-dg+ch)} \right] \right) / \left( (bc-ad) \sqrt{\frac{-dg+ch}{h}} \right.$$

$$\left. \sqrt{\left( fh + \frac{d^2 eg - cdfg - cdeh + c^2 fh}{(c+dx)^2} + \frac{dfg+deh-2cfh}{c+dx} \right)} \right) -$$

$$\left( 2 i a b C d e g \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \text{EllipticF}\left[ \right. \right.$$

$$\left. \left. i \text{ArcSinh}\left[ \frac{\sqrt{\frac{-dg+ch}{h}}}{\sqrt{c+dx}} \right], \frac{(-de+cf)h}{f(-dg+ch)} \right] \right) / \left( (bc-ad) \sqrt{\frac{-dg+ch}{h}} \right.$$

$$\left. \sqrt{\left( fh + \frac{d^2 eg - cdfg - cdeh + c^2 fh}{(c+dx)^2} + \frac{dfg+deh-2cfh}{c+dx} \right)} \right) +$$

$$\begin{aligned}
 & \left( i A b^3 c d f g \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \operatorname{EllipticF} \left[ \right. \right. \\
 & \quad \left. \left. i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{-dg+ch}{h}}}{\sqrt{c+dx}}, \frac{(-de+cf)h}{f(-dg+ch)} \right] \right] / \left( (bc-ad)^2 \sqrt{\frac{-dg+ch}{h}} \right. \right. \\
 & \quad \left. \left. \sqrt{\left( fh + \frac{d^2 eg - cdfg - cdeh + c^2 fh}{(c+dx)^2} + \frac{dfg + deh - 2cfh}{c+dx} \right)} \right) + \right. \\
 & \left( i a^2 b c C d f g \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \operatorname{EllipticF} \left[ \right. \right. \\
 & \quad \left. \left. i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{-dg+ch}{h}}}{\sqrt{c+dx}}, \frac{(-de+cf)h}{f(-dg+ch)} \right] \right] / \left( (bc-ad)^2 \sqrt{\frac{-dg+ch}{h}} \right. \right. \\
 & \quad \left. \left. \sqrt{\left( fh + \frac{d^2 eg - cdfg - cdeh + c^2 fh}{(c+dx)^2} + \frac{dfg + deh - 2cfh}{c+dx} \right)} \right) + \right. \\
 & \left( 2 i a b c C f g \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \operatorname{EllipticF} \left[ \right. \right. \\
 & \quad \left. \left. i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{-dg+ch}{h}}}{\sqrt{c+dx}}, \frac{(-de+cf)h}{f(-dg+ch)} \right] \right] / \left( (bc-ad) \sqrt{\frac{-dg+ch}{h}} \right. \right. \\
 & \quad \left. \left. \sqrt{\left( fh + \frac{d^2 eg - cdfg - cdeh + c^2 fh}{(c+dx)^2} + \frac{dfg + deh - 2cfh}{c+dx} \right)} \right) - \right.
 \end{aligned}$$

$$\left( 2 i A b^2 d f g \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \text{EllipticF}\left[ \right. \right. \\ \left. \left. i \text{ArcSinh}\left[\frac{\sqrt{\frac{-dg+ch}{h}}}{\sqrt{c+dx}}\right], \frac{(-de+cf)h}{f(-dg+ch)}\right] \right) / \left( (bc-ad) \sqrt{-\frac{-dg+ch}{h}} \right) \\ \sqrt{\left( fh + \frac{d^2 eg - cd fg - cdeh + c^2 fh}{(c+dx)^2} + \frac{dfg + deh - 2cfh}{c+dx} \right)} +$$

$$\left( i A b^3 c de h \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \text{EllipticF}\left[ \right. \right. \\ \left. \left. i \text{ArcSinh}\left[\frac{\sqrt{\frac{-dg+ch}{h}}}{\sqrt{c+dx}}\right], \frac{(-de+cf)h}{f(-dg+ch)}\right] \right) / \left( (bc-ad)^2 \sqrt{-\frac{-dg+ch}{h}} \right) \\ \sqrt{\left( fh + \frac{d^2 eg - cd fg - cdeh + c^2 fh}{(c+dx)^2} + \frac{dfg + deh - 2cfh}{c+dx} \right)} +$$

$$\left( i a^2 b c C de h \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \text{EllipticF}\left[ \right. \right. \\ \left. \left. i \text{ArcSinh}\left[\frac{\sqrt{\frac{-dg+ch}{h}}}{\sqrt{c+dx}}\right], \frac{(-de+cf)h}{f(-dg+ch)}\right] \right) / \left( (bc-ad)^2 \sqrt{-\frac{-dg+ch}{h}} \right) \\ \sqrt{\left( fh + \frac{d^2 eg - cd fg - cdeh + c^2 fh}{(c+dx)^2} + \frac{dfg + deh - 2cfh}{c+dx} \right)} +$$

$$\begin{aligned}
 & \left( 2 i a b c C e h \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \operatorname{EllipticF} \left[ \right. \right. \\
 & \quad \left. \left. i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{-dg+ch}{h}}}{\sqrt{c+dx}}, \frac{(-de+cf)h}{f(-dg+ch)} \right] \right] / \left( (bc-ad) \sqrt{-\frac{-dg+ch}{h}} \right. \right. \\
 & \quad \left. \left. \sqrt{\left( fh + \frac{d^2 eg - cdfg - cdeh + c^2 fh}{(c+dx)^2} + \frac{dfg + deh - 2cfh}{c+dx} \right)} \right) \right) - \\
 & \left( 2 i A b^2 d e h \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \operatorname{EllipticF} \left[ \right. \right. \\
 & \quad \left. \left. i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{-dg+ch}{h}}}{\sqrt{c+dx}}, \frac{(-de+cf)h}{f(-dg+ch)} \right] \right] / \left( (bc-ad) \sqrt{-\frac{-dg+ch}{h}} \right. \right. \\
 & \quad \left. \left. \sqrt{\left( fh + \frac{d^2 eg - cdfg - cdeh + c^2 fh}{(c+dx)^2} + \frac{dfg + deh - 2cfh}{c+dx} \right)} \right) \right) - \\
 & \left( i A b^3 c^2 f h \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \operatorname{EllipticF} \left[ \right. \right. \\
 & \quad \left. \left. i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{-dg+ch}{h}}}{\sqrt{c+dx}}, \frac{(-de+cf)h}{f(-dg+ch)} \right] \right] / \left( (bc-ad)^2 \sqrt{-\frac{-dg+ch}{h}} \right. \right. \\
 & \quad \left. \left. \sqrt{\left( fh + \frac{d^2 eg - cdfg - cdeh + c^2 fh}{(c+dx)^2} + \frac{dfg + deh - 2cfh}{c+dx} \right)} \right) \right) -
 \end{aligned}$$

$$\left( i a^2 b c^2 C f h \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \text{EllipticF}\left[ \right. \right. \\ \left. \left. i \text{ArcSinh}\left[ \frac{\sqrt{\frac{-dg+ch}{h}}}{\sqrt{c+dx}} \right], \frac{(-de+cf)h}{f(-dg+ch)} \right] \right) / \left( (bc-ad)^2 \sqrt{\frac{-dg+ch}{h}} \right) \\ \sqrt{\left( fh + \frac{d^2 eg - cd fg - cde h + c^2 fh}{(c+dx)^2} + \frac{dfg + de h - 2cfh}{c+dx} \right)} + \\ \left( 2 i A b^2 c f h \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \text{EllipticF}\left[ \right. \right. \\ \left. \left. i \text{ArcSinh}\left[ \frac{\sqrt{\frac{-dg+ch}{h}}}{\sqrt{c+dx}} \right], \frac{(-de+cf)h}{f(-dg+ch)} \right] \right) / \left( (bc-ad) \sqrt{\frac{-dg+ch}{h}} \right) \\ \sqrt{\left( fh + \frac{d^2 eg - cd fg - cde h + c^2 fh}{(c+dx)^2} + \frac{dfg + de h - 2cfh}{c+dx} \right)} + \\ \left( 2 i a A b d f h \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \text{EllipticF}\left[ \right. \right. \\ \left. \left. i \text{ArcSinh}\left[ \frac{\sqrt{\frac{-dg+ch}{h}}}{\sqrt{c+dx}} \right], \frac{(-de+cf)h}{f(-dg+ch)} \right] \right) / \left( (bc-ad) \sqrt{\frac{-dg+ch}{h}} \right) \\ \sqrt{\left( fh + \frac{d^2 eg - cd fg - cde h + c^2 fh}{(c+dx)^2} + \frac{dfg + de h - 2cfh}{c+dx} \right)} + \frac{1}{(bc-ad)^3}$$

$$\begin{aligned}
 & A b^4 d^2 e g \left( \left( i c \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \operatorname{EllipticPi} \left[ \frac{(bc-ad)h}{b(-dg+ch)}, \right. \right. \right. \\
 & \left. \left. \left. i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{-dg+ch}{h}}}{\sqrt{c+dx}} \right], \frac{(-de+cf)h}{f(-dg+ch)} \right] \right) / \left( \sqrt{\frac{-dg+ch}{h}} \sqrt{\left( fh + \right. \right. \right. \\
 & \left. \left. \left. \frac{d^2 e g}{(c+dx)^2} - \frac{c d f g}{(c+dx)^2} - \frac{c d e h}{(c+dx)^2} + \frac{c^2 f h}{(c+dx)^2} + \frac{d f g}{c+dx} + \frac{d e h}{c+dx} - \frac{2 c f h}{c+dx} \right) \right) - \\
 & \left( i a d \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \operatorname{EllipticPi} \left[ \frac{(bc-ad)h}{b(-dg+ch)}, i \operatorname{ArcSinh} \left[ \right. \right. \right. \\
 & \left. \left. \left. \frac{\sqrt{\frac{-dg+ch}{h}}}{\sqrt{c+dx}} \right], \frac{(-de+cf)h}{f(-dg+ch)} \right] \right) / \left( b \sqrt{\frac{-dg+ch}{h}} \sqrt{\left( fh + \frac{d^2 e g}{(c+dx)^2} - \right. \right. \right. \\
 & \left. \left. \left. \frac{c d f g}{(c+dx)^2} - \frac{c d e h}{(c+dx)^2} + \frac{c^2 f h}{(c+dx)^2} + \frac{d f g}{c+dx} + \frac{d e h}{c+dx} - \frac{2 c f h}{c+dx} \right) \right) + \frac{1}{(bc-ad)^3} \\
 & a^2 b^2 C d^2 e g \left( \left( i c \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \operatorname{EllipticPi} \left[ \frac{(bc-ad)h}{b(-dg+ch)}, \right. \right. \right. \\
 & \left. \left. \left. i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{-dg+ch}{h}}}{\sqrt{c+dx}} \right], \frac{(-de+cf)h}{f(-dg+ch)} \right] \right) / \left( \sqrt{\frac{-dg+ch}{h}} \sqrt{\left( fh + \right. \right. \right. \\
 & \left. \left. \left. \frac{d^2 e g}{(c+dx)^2} - \frac{c d f g}{(c+dx)^2} - \frac{c d e h}{(c+dx)^2} + \frac{c^2 f h}{(c+dx)^2} + \frac{d f g}{c+dx} + \frac{d e h}{c+dx} - \frac{2 c f h}{c+dx} \right) \right) -
 \end{aligned}$$

$$\begin{aligned}
 & \left( i a d \sqrt{1 - \frac{-de + cf}{f(c+dx)}} \sqrt{1 - \frac{-dg + ch}{h(c+dx)}} \text{EllipticPi} \left[ \frac{(bc - ad)h}{b(-dg + ch)}, \right. \right. \\
 & \quad \left. \left. i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{-dg + ch}{h}}}{\sqrt{c+dx}} \right], \frac{(-de + cf)h}{f(-dg + ch)} \right] \right) / \left( b \sqrt{-\frac{-dg + ch}{h}} \sqrt{\left( fh + \right. \right.} \\
 & \quad \left. \left. \frac{d^2 eg}{(c+dx)^2} - \frac{cdfg}{(c+dx)^2} - \frac{cdeh}{(c+dx)^2} + \frac{c^2 fh}{(c+dx)^2} + \frac{dfg}{c+dx} + \frac{deh}{c+dx} - \frac{2cfh}{c+dx} \right) \right) + \\
 & \frac{1}{(bc - ad)^2} 2b^3 c C e g \left( \left( i c \sqrt{1 - \frac{-de + cf}{f(c+dx)}} \sqrt{1 - \frac{-dg + ch}{h(c+dx)}} \text{EllipticPi} \left[ \right. \right. \right. \\
 & \quad \left. \left. \frac{(bc - ad)h}{b(-dg + ch)}, i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{-dg + ch}{h}}}{\sqrt{c+dx}} \right], \frac{(-de + cf)h}{f(-dg + ch)} \right] \right) / \\
 & \left( \sqrt{-\frac{-dg + ch}{h}} \sqrt{\left( fh + \frac{d^2 eg}{(c+dx)^2} - \frac{cdfg}{(c+dx)^2} - \frac{cdeh}{(c+dx)^2} + \frac{c^2 fh}{(c+dx)^2} + \right. \right.} \\
 & \quad \left. \left. \frac{dfg}{c+dx} + \frac{deh}{c+dx} - \frac{2cfh}{c+dx} \right) \right) - \left( i a d \sqrt{1 - \frac{-de + cf}{f(c+dx)}} \sqrt{1 - \frac{-dg + ch}{h(c+dx)}} \right. \\
 & \quad \left. \text{EllipticPi} \left[ \frac{(bc - ad)h}{b(-dg + ch)}, i \text{ArcSinh} \left[ \frac{\sqrt{-\frac{-dg + ch}{h}}}{\sqrt{c+dx}} \right], \frac{(-de + cf)h}{f(-dg + ch)} \right] \right) / \\
 & \left( b \sqrt{-\frac{-dg + ch}{h}} \sqrt{\left( fh + \frac{d^2 eg}{(c+dx)^2} - \frac{cdfg}{(c+dx)^2} - \frac{cdeh}{(c+dx)^2} + \right. \right.}
 \end{aligned}$$

$$\left. \left. \left. \left. \frac{c^2 f h}{(c+dx)^2} + \frac{d f g}{c+dx} + \frac{d e h}{c+dx} - \frac{2 c f h}{c+dx} \right) \right) \right) + \frac{1}{(bc-ad)^2}$$

$$2 a b^2 C d e g \left( \left( i c \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \operatorname{EllipticPi} \left[ \frac{(bc-ad)h}{b(-dg+ch)}, \right. \right. \right.$$

$$\left. \left. \left. i \operatorname{ArcSinh} \left[ \frac{\sqrt{-\frac{-dg+ch}{h}}}{\sqrt{c+dx}} \right], \frac{(-de+cf)h}{f(-dg+ch)} \right] \right) / \left( \sqrt{-\frac{-dg+ch}{h}} \sqrt{fh+} \right. \right.$$

$$\left. \left. \left. \left. \frac{d^2 e g}{(c+dx)^2} - \frac{c d f g}{(c+dx)^2} - \frac{c d e h}{(c+dx)^2} + \frac{c^2 f h}{(c+dx)^2} + \frac{d f g}{c+dx} + \frac{d e h}{c+dx} - \frac{2 c f h}{c+dx} \right) \right) \right) -$$

$$\left( i a d \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \operatorname{EllipticPi} \left[ \frac{(bc-ad)h}{b(-dg+ch)}, \right. \right.$$

$$\left. \left. \left. i \operatorname{ArcSinh} \left[ \frac{\sqrt{-\frac{-dg+ch}{h}}}{\sqrt{c+dx}} \right], \frac{(-de+cf)h}{f(-dg+ch)} \right] \right) / \left( b \sqrt{-\frac{-dg+ch}{h}} \sqrt{fh+} \right. \right.$$

$$\left. \left. \left. \left. \frac{d^2 e g}{(c+dx)^2} - \frac{c d f g}{(c+dx)^2} - \frac{c d e h}{(c+dx)^2} + \frac{c^2 f h}{(c+dx)^2} + \frac{d f g}{c+dx} + \frac{d e h}{c+dx} - \frac{2 c f h}{c+dx} \right) \right) \right) -$$

$$\frac{1}{bc-ad} 2 b^2 C e g \left( \left( i c \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \operatorname{EllipticPi} \left[ \frac{(bc-ad)h}{b(-dg+ch)}, \right. \right. \right.$$

$$\left. \left. \left. i \operatorname{ArcSinh} \left[ \frac{\sqrt{-\frac{-dg+ch}{h}}}{\sqrt{c+dx}} \right], \frac{(-de+cf)h}{f(-dg+ch)} \right] \right) / \left( \sqrt{-\frac{-dg+ch}{h}} \sqrt{fh+} \right. \right.$$

$$\left. \left( \frac{d^2 e g}{(c+dx)^2} - \frac{c d f g}{(c+dx)^2} - \frac{c d e h}{(c+dx)^2} + \frac{c^2 f h}{(c+dx)^2} + \frac{d f g}{c+dx} + \frac{d e h}{c+dx} - \frac{2 c f h}{c+dx} \right) \right) -$$

$$\left( i a d \sqrt{1 - \frac{-d e + c f}{f (c+dx)}} \sqrt{1 - \frac{-d g + c h}{h (c+dx)}} \operatorname{EllipticPi} \left[ \frac{(b c - a d) h}{b (-d g + c h)}, \right. \right.$$

$$\left. \left. i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{-d g + c h}{h}}}{\sqrt{c+dx}} \right], \frac{(-d e + c f) h}{f (-d g + c h)} \right] \right) / \left( b \sqrt{\frac{-d g + c h}{h}} \sqrt{\left( f h + \right. \right.$$

$$\left. \left. \frac{d^2 e g}{(c+dx)^2} - \frac{c d f g}{(c+dx)^2} - \frac{c d e h}{(c+dx)^2} + \frac{c^2 f h}{(c+dx)^2} + \frac{d f g}{c+dx} + \frac{d e h}{c+dx} - \frac{2 c f h}{c+dx} \right) \right) \right) -$$

$$\frac{1}{(b c - a d)^3} A b^4 c d f g \left( \left( i c \sqrt{1 - \frac{-d e + c f}{f (c+dx)}} \sqrt{1 - \frac{-d g + c h}{h (c+dx)}} \operatorname{EllipticPi} \left[ \right. \right. \right.$$

$$\left. \left. \left. \frac{(b c - a d) h}{b (-d g + c h)}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{-d g + c h}{h}}}{\sqrt{c+dx}} \right], \frac{(-d e + c f) h}{f (-d g + c h)} \right] \right) / \right.$$

$$\left. \left( \sqrt{\frac{-d g + c h}{h}} \sqrt{\left( f h + \frac{d^2 e g}{(c+dx)^2} - \frac{c d f g}{(c+dx)^2} - \frac{c d e h}{(c+dx)^2} + \frac{c^2 f h}{(c+dx)^2} + \right. \right. \right.$$

$$\left. \left. \left. \frac{d f g}{c+dx} + \frac{d e h}{c+dx} - \frac{2 c f h}{c+dx} \right) \right) - \left( i a d \sqrt{1 - \frac{-d e + c f}{f (c+dx)}} \sqrt{1 - \frac{-d g + c h}{h (c+dx)}} \right.$$

$$\left. \left. \operatorname{EllipticPi} \left[ \frac{(b c - a d) h}{b (-d g + c h)}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{-d g + c h}{h}}}{\sqrt{c+dx}} \right], \frac{(-d e + c f) h}{f (-d g + c h)} \right] \right) / \right.$$

$$\begin{aligned}
 & \left( b \sqrt{-\frac{dg+ch}{h}} \sqrt{\left( fh + \frac{d^2 eg}{(c+dx)^2} - \frac{cdfg}{(c+dx)^2} - \frac{cdeh}{(c+dx)^2} + \right.} \right. \\
 & \quad \left. \left. \frac{c^2 fh}{(c+dx)^2} + \frac{dfg}{c+dx} + \frac{deh}{c+dx} - \frac{2cfh}{c+dx} \right) \right) - \frac{1}{(bc-ad)^3} \\
 & a^2 b^2 c C d f g \left( \left( i c \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \text{EllipticPi}\left[\frac{(bc-ad)h}{b(-dg+ch)}\right], \right. \right. \\
 & \quad \left. \left. i \text{ArcSinh}\left[\frac{\sqrt{-\frac{dg+ch}{h}}}{\sqrt{c+dx}}\right], \frac{(-de+cf)h}{f(-dg+ch)} \right] \right) / \left( \sqrt{-\frac{dg+ch}{h}} \sqrt{\left( fh + \right.} \right. \\
 & \quad \left. \left. \frac{d^2 eg}{(c+dx)^2} - \frac{cdfg}{(c+dx)^2} - \frac{cdeh}{(c+dx)^2} + \frac{c^2 fh}{(c+dx)^2} + \frac{dfg}{c+dx} + \frac{deh}{c+dx} - \frac{2cfh}{c+dx} \right) \right) - \\
 & \left( i a d \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \text{EllipticPi}\left[\frac{(bc-ad)h}{b(-dg+ch)}\right], \right. \\
 & \quad \left. i \text{ArcSinh}\left[\frac{\sqrt{-\frac{dg+ch}{h}}}{\sqrt{c+dx}}\right], \frac{(-de+cf)h}{f(-dg+ch)} \right] \right) / \left( b \sqrt{-\frac{dg+ch}{h}} \sqrt{\left( fh + \right.} \right. \\
 & \quad \left. \left. \frac{d^2 eg}{(c+dx)^2} - \frac{cdfg}{(c+dx)^2} - \frac{cdeh}{(c+dx)^2} + \frac{c^2 fh}{(c+dx)^2} + \frac{dfg}{c+dx} + \frac{deh}{c+dx} - \frac{2cfh}{c+dx} \right) \right) - \\
 & \frac{1}{(bc-ad)^2} 2 a b^2 c C f g \left( \left( i c \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \text{EllipticPi}\left[ \right. \right. \right.
 \end{aligned}$$

$$\left. \frac{(bc-ad)h}{b(-dg+ch)}, \operatorname{ArcSinh}\left[\frac{\sqrt{-\frac{dg+ch}{h}}}{\sqrt{c+dx}}\right], \frac{(-de+cf)h}{f(-dg+ch)}\right] /$$

$$\left( \sqrt{-\frac{dg+ch}{h}} \sqrt{\left( fh + \frac{d^2eg}{(c+dx)^2} - \frac{cdfg}{(c+dx)^2} - \frac{cdeh}{(c+dx)^2} + \frac{c^2fh}{(c+dx)^2} + \right.} \right.$$

$$\left. \frac{dfg}{c+dx} + \frac{deh}{c+dx} - \frac{2cfh}{c+dx} \right) - \left( i ad \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \right.$$

$$\left. \operatorname{EllipticPi}\left[\frac{(bc-ad)h}{b(-dg+ch)}, \operatorname{ArcSinh}\left[\frac{\sqrt{-\frac{dg+ch}{h}}}{\sqrt{c+dx}}\right], \frac{(-de+cf)h}{f(-dg+ch)}\right] \right) /$$

$$\left( b \sqrt{-\frac{dg+ch}{h}} \sqrt{\left( fh + \frac{d^2eg}{(c+dx)^2} - \frac{cdfg}{(c+dx)^2} - \frac{cdeh}{(c+dx)^2} + \right.} \right.$$

$$\left. \frac{c^2fh}{(c+dx)^2} + \frac{dfg}{c+dx} + \frac{deh}{c+dx} - \frac{2cfh}{c+dx} \right) \left. \right) + \frac{1}{(bc-ad)^2}$$

$$2Ab^3dfg \left( \left( i c \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \operatorname{EllipticPi}\left[\frac{(bc-ad)h}{b(-dg+ch)}, \right. \right. \right.$$

$$\left. \left. \operatorname{ArcSinh}\left[\frac{\sqrt{-\frac{dg+ch}{h}}}{\sqrt{c+dx}}\right], \frac{(-de+cf)h}{f(-dg+ch)}\right] \right) / \left( \sqrt{-\frac{dg+ch}{h}} \sqrt{\left( fh + \right.} \right.$$

$$\left. \frac{d^2eg}{(c+dx)^2} - \frac{cdfg}{(c+dx)^2} - \frac{cdeh}{(c+dx)^2} + \frac{c^2fh}{(c+dx)^2} + \frac{dfg}{c+dx} + \frac{deh}{c+dx} - \frac{2cfh}{c+dx} \right) \left. \right) -$$

$$\left( \begin{aligned} & \left( i a d \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \operatorname{EllipticPi} \left[ \frac{(bc-ad)h}{b(-dg+ch)}, \right. \right. \\ & \left. \left. i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{-dg+ch}{h}}}{\sqrt{c+dx}} \right], \frac{(-de+cf)h}{f(-dg+ch)} \right] \right) / \left( b \sqrt{\frac{-dg+ch}{h}} \sqrt{\left( fh + \right. \right. \right. \\ & \left. \left. \left. \frac{d^2 eg}{(c+dx)^2} - \frac{cdfg}{(c+dx)^2} - \frac{cdeh}{(c+dx)^2} + \frac{c^2 fh}{(c+dx)^2} + \frac{dfg}{c+dx} + \frac{deh}{c+dx} - \frac{2cfh}{c+dx} \right) \right) \right) + \\ & \frac{1}{bc-ad} 2abcf g \left( \left( i c \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \operatorname{EllipticPi} \left[ \frac{(bc-ad)h}{b(-dg+ch)}, \right. \right. \right. \\ & \left. \left. \left. i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{-dg+ch}{h}}}{\sqrt{c+dx}} \right], \frac{(-de+cf)h}{f(-dg+ch)} \right] \right) / \left( \sqrt{\frac{-dg+ch}{h}} \sqrt{\left( fh + \right. \right. \right. \\ & \left. \left. \left. \frac{d^2 eg}{(c+dx)^2} - \frac{cdfg}{(c+dx)^2} - \frac{cdeh}{(c+dx)^2} + \frac{c^2 fh}{(c+dx)^2} + \frac{dfg}{c+dx} + \frac{deh}{c+dx} - \frac{2cfh}{c+dx} \right) \right) \right) - \\ & \left( i a d \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \operatorname{EllipticPi} \left[ \frac{(bc-ad)h}{b(-dg+ch)}, \right. \right. \\ & \left. \left. i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{-dg+ch}{h}}}{\sqrt{c+dx}} \right], \frac{(-de+cf)h}{f(-dg+ch)} \right] \right) / \left( b \sqrt{\frac{-dg+ch}{h}} \sqrt{\left( fh + \right. \right. \right. \\ & \left. \left. \left. \frac{d^2 eg}{(c+dx)^2} - \frac{cdfg}{(c+dx)^2} - \frac{cdeh}{(c+dx)^2} + \frac{c^2 fh}{(c+dx)^2} + \frac{dfg}{c+dx} + \frac{deh}{c+dx} - \frac{2cfh}{c+dx} \right) \right) \right) - \end{aligned} \right)$$

$$\frac{1}{(bc-ad)^3} A b^4 c d e h \left( \left( i c \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \operatorname{EllipticPi} \left[ \frac{(bc-ad)h}{b(-dg+ch)}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{-dg+ch}{h}}}{\sqrt{c+dx}} \right], \frac{(-de+cf)h}{f(-dg+ch)} \right] \right) / \right.$$

$$\left( \sqrt{\frac{-dg+ch}{h}} \sqrt{\left( fh + \frac{d^2 eg}{(c+dx)^2} - \frac{cdfg}{(c+dx)^2} - \frac{cdeh}{(c+dx)^2} + \frac{c^2 fh}{(c+dx)^2} + \frac{dfg}{c+dx} + \frac{deh}{c+dx} - \frac{2cfh}{c+dx} \right)} \right) - \left( i a d \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \operatorname{EllipticPi} \left[ \frac{(bc-ad)h}{b(-dg+ch)}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{-dg+ch}{h}}}{\sqrt{c+dx}} \right], \frac{(-de+cf)h}{f(-dg+ch)} \right] \right) / \right.$$

$$\left( b \sqrt{\frac{-dg+ch}{h}} \sqrt{\left( fh + \frac{d^2 eg}{(c+dx)^2} - \frac{cdfg}{(c+dx)^2} - \frac{cdeh}{(c+dx)^2} + \frac{c^2 fh}{(c+dx)^2} + \frac{dfg}{c+dx} + \frac{deh}{c+dx} - \frac{2cfh}{c+dx} \right)} \right) \left. \right) - \frac{1}{(bc-ad)^3}$$

$$a^2 b^2 c C d e h \left( \left( i c \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \operatorname{EllipticPi} \left[ \frac{(bc-ad)h}{b(-dg+ch)}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{-dg+ch}{h}}}{\sqrt{c+dx}} \right], \frac{(-de+cf)h}{f(-dg+ch)} \right] \right) / \left( \sqrt{\frac{-dg+ch}{h}} \sqrt{\left( fh + \right.} \right.$$

$$\begin{aligned}
 & \left. \left( \frac{d^2 e g}{(c+dx)^2} - \frac{c d f g}{(c+dx)^2} - \frac{c d e h}{(c+dx)^2} + \frac{c^2 f h}{(c+dx)^2} + \frac{d f g}{c+dx} + \frac{d e h}{c+dx} - \frac{2 c f h}{c+dx} \right) \right) - \\
 & \left( i a d \sqrt{1 - \frac{-d e + c f}{f (c+dx)}} \sqrt{1 - \frac{-d g + c h}{h (c+dx)}} \text{EllipticPi} \left[ \frac{(b c - a d) h}{b (-d g + c h)}, \right. \right. \\
 & \left. \left. i \text{ArcSinh} \left[ \frac{\sqrt{\frac{-d g + c h}{h}}}{\sqrt{c+dx}} \right], \frac{(-d e + c f) h}{f (-d g + c h)} \right] \right) / \left( b \sqrt{\frac{-d g + c h}{h}} \sqrt{\left( f h + \right. \right. \\
 & \left. \left. \frac{d^2 e g}{(c+dx)^2} - \frac{c d f g}{(c+dx)^2} - \frac{c d e h}{(c+dx)^2} + \frac{c^2 f h}{(c+dx)^2} + \frac{d f g}{c+dx} + \frac{d e h}{c+dx} - \frac{2 c f h}{c+dx} \right) \right) \right) - \\
 & \frac{1}{(b c - a d)^2} 2 a b^2 c C e h \left( \left( i c \sqrt{1 - \frac{-d e + c f}{f (c+dx)}} \sqrt{1 - \frac{-d g + c h}{h (c+dx)}} \text{EllipticPi} \left[ \right. \right. \right. \\
 & \left. \left. \left. \frac{(b c - a d) h}{b (-d g + c h)}, i \text{ArcSinh} \left[ \frac{\sqrt{\frac{-d g + c h}{h}}}{\sqrt{c+dx}} \right], \frac{(-d e + c f) h}{f (-d g + c h)} \right] \right) / \right. \\
 & \left. \left( \sqrt{\frac{-d g + c h}{h}} \sqrt{\left( f h + \frac{d^2 e g}{(c+dx)^2} - \frac{c d f g}{(c+dx)^2} - \frac{c d e h}{(c+dx)^2} + \frac{c^2 f h}{(c+dx)^2} + \right. \right. \right. \\
 & \left. \left. \left. \frac{d f g}{c+dx} + \frac{d e h}{c+dx} - \frac{2 c f h}{c+dx} \right) \right) - \left( i a d \sqrt{1 - \frac{-d e + c f}{f (c+dx)}} \sqrt{1 - \frac{-d g + c h}{h (c+dx)}} \right. \\
 & \left. \left. \text{EllipticPi} \left[ \frac{(b c - a d) h}{b (-d g + c h)}, i \text{ArcSinh} \left[ \frac{\sqrt{\frac{-d g + c h}{h}}}{\sqrt{c+dx}} \right], \frac{(-d e + c f) h}{f (-d g + c h)} \right] \right) / \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left( b \sqrt{-\frac{dg+ch}{h}} \sqrt{\left( fh + \frac{d^2 eg}{(c+dx)^2} - \frac{cdfg}{(c+dx)^2} - \frac{cdeh}{(c+dx)^2} + \right. \right. \\
 & \quad \left. \left. \frac{c^2 fh}{(c+dx)^2} + \frac{dfg}{c+dx} + \frac{deh}{c+dx} - \frac{2cfh}{c+dx} \right)} \right) + \frac{1}{(bc-ad)^2} \\
 2Ab^3deh & \left( \left( i c \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \operatorname{EllipticPi}\left[\frac{(bc-ad)h}{b(-dg+ch)}\right], \right. \right. \\
 & \quad \left. \left. i \operatorname{ArcSinh}\left[\frac{\sqrt{-\frac{dg+ch}{h}}}{\sqrt{c+dx}}\right], \frac{(-de+cf)h}{f(-dg+ch)} \right] \right) / \left( \sqrt{-\frac{dg+ch}{h}} \sqrt{\left( fh + \right. \right. \\
 & \quad \left. \left. \frac{d^2 eg}{(c+dx)^2} - \frac{cdfg}{(c+dx)^2} - \frac{cdeh}{(c+dx)^2} + \frac{c^2 fh}{(c+dx)^2} + \frac{dfg}{c+dx} + \frac{deh}{c+dx} - \frac{2cfh}{c+dx} \right)} \right) - \\
 & \left( i ad \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \operatorname{EllipticPi}\left[\frac{(bc-ad)h}{b(-dg+ch)}\right], \right. \\
 & \quad \left. i \operatorname{ArcSinh}\left[\frac{\sqrt{-\frac{dg+ch}{h}}}{\sqrt{c+dx}}\right], \frac{(-de+cf)h}{f(-dg+ch)} \right] \right) / \left( b \sqrt{-\frac{dg+ch}{h}} \sqrt{\left( fh + \right. \right. \\
 & \quad \left. \left. \frac{d^2 eg}{(c+dx)^2} - \frac{cdfg}{(c+dx)^2} - \frac{cdeh}{(c+dx)^2} + \frac{c^2 fh}{(c+dx)^2} + \frac{dfg}{c+dx} + \frac{deh}{c+dx} - \frac{2cfh}{c+dx} \right)} \right) \Bigg) + \\
 \frac{1}{bc-ad} 2abcEh & \left( \left( i c \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \operatorname{EllipticPi}\left[\frac{(bc-ad)h}{b(-dg+ch)}\right], \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left( \int \operatorname{ArcSinh} \left[ \frac{\sqrt{-\frac{dg+ch}{h}}}{\sqrt{c+dx}} \right], \frac{(-de+cf)h}{f(-dg+ch)} \right] / \left( \sqrt{-\frac{dg+ch}{h}} \sqrt{\left( fh + \right. \right.} \\
 & \left. \left. \frac{d^2eg}{(c+dx)^2} - \frac{cdfg}{(c+dx)^2} - \frac{cdeh}{(c+dx)^2} + \frac{c^2fh}{(c+dx)^2} + \frac{dfg}{c+dx} + \frac{deh}{c+dx} - \frac{2cfh}{c+dx} \right) \right) - \\
 & \left( \int a d \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \operatorname{EllipticPi} \left[ \frac{(bc-ad)h}{b(-dg+ch)}, \right. \right. \\
 & \left. \left. \int \operatorname{ArcSinh} \left[ \frac{\sqrt{-\frac{dg+ch}{h}}}{\sqrt{c+dx}} \right], \frac{(-de+cf)h}{f(-dg+ch)} \right] / \left( b \sqrt{-\frac{dg+ch}{h}} \sqrt{\left( fh + \right. \right.} \right. \\
 & \left. \left. \frac{d^2eg}{(c+dx)^2} - \frac{cdfg}{(c+dx)^2} - \frac{cdeh}{(c+dx)^2} + \frac{c^2fh}{(c+dx)^2} + \frac{dfg}{c+dx} + \frac{deh}{c+dx} - \frac{2cfh}{c+dx} \right) \right) \right) + \\
 & \frac{1}{(bc-ad)^3} A b^4 c^2 f h \left( \left( \int c \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \operatorname{EllipticPi} \left[ \right. \right. \right. \\
 & \left. \left. \left. \frac{(bc-ad)h}{b(-dg+ch)}, \int \operatorname{ArcSinh} \left[ \frac{\sqrt{-\frac{dg+ch}{h}}}{\sqrt{c+dx}} \right], \frac{(-de+cf)h}{f(-dg+ch)} \right] / \right. \right. \\
 & \left. \left. \sqrt{-\frac{dg+ch}{h}} \sqrt{\left( fh + \frac{d^2eg}{(c+dx)^2} - \frac{cdfg}{(c+dx)^2} - \frac{cdeh}{(c+dx)^2} + \frac{c^2fh}{(c+dx)^2} + \right. \right. \right. \\
 & \left. \left. \left. \frac{dfg}{c+dx} + \frac{deh}{c+dx} - \frac{2cfh}{c+dx} \right) \right) - \left( \int a d \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \right) \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left. \text{EllipticPi}\left[\frac{(bc-ad)h}{b(-dg+ch)}, \text{ArcSinh}\left[\frac{\sqrt{-\frac{dg+ch}{h}}}{\sqrt{c+dx}}\right], \frac{(-de+cf)h}{f(-dg+ch)}\right] \right/ \\
 & \left( b \sqrt{-\frac{dg+ch}{h}} \sqrt{\left( fh + \frac{d^2eg}{(c+dx)^2} - \frac{cdfg}{(c+dx)^2} - \frac{cdeh}{(c+dx)^2} + \right.} \right. \\
 & \left. \left. \frac{c^2fh}{(c+dx)^2} + \frac{dfg}{c+dx} + \frac{deh}{c+dx} - \frac{2cfh}{c+dx} \right) \right) + \frac{1}{(bc-ad)^3} \\
 & a^2 b^2 c^2 c f h \left( \left( \text{ArcSinh}\left[\frac{\sqrt{-\frac{dg+ch}{h}}}{\sqrt{c+dx}}\right], \frac{(-de+cf)h}{f(-dg+ch)}\right] \right) \left( \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \text{EllipticPi}\left[\frac{(bc-ad)h}{b(-dg+ch)}, \right. \right. \\
 & \left. \left. \frac{d^2eg}{(c+dx)^2} - \frac{cdfg}{(c+dx)^2} - \frac{cdeh}{(c+dx)^2} + \frac{c^2fh}{(c+dx)^2} + \frac{dfg}{c+dx} + \frac{deh}{c+dx} - \frac{2cfh}{c+dx} \right) \right) - \\
 & \left( \text{ArcSinh}\left[\frac{\sqrt{-\frac{dg+ch}{h}}}{\sqrt{c+dx}}\right], \frac{(-de+cf)h}{f(-dg+ch)}\right] \left( \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \text{EllipticPi}\left[\frac{(bc-ad)h}{b(-dg+ch)}, \right. \right. \\
 & \left. \left. \frac{d^2eg}{(c+dx)^2} - \frac{cdfg}{(c+dx)^2} - \frac{cdeh}{(c+dx)^2} + \frac{c^2fh}{(c+dx)^2} + \frac{dfg}{c+dx} + \frac{deh}{c+dx} - \frac{2cfh}{c+dx} \right) \right) - \\
 & \left( \text{ArcSinh}\left[\frac{\sqrt{-\frac{dg+ch}{h}}}{\sqrt{c+dx}}\right], \frac{(-de+cf)h}{f(-dg+ch)}\right] \left( b \sqrt{-\frac{dg+ch}{h}} \sqrt{\left( fh + \frac{d^2eg}{(c+dx)^2} - \frac{cdfg}{(c+dx)^2} - \frac{cdeh}{(c+dx)^2} + \frac{c^2fh}{(c+dx)^2} + \frac{dfg}{c+dx} + \frac{deh}{c+dx} - \frac{2cfh}{c+dx} \right) \right) \right) -
 \end{aligned}$$

$$\begin{aligned}
 & \frac{1}{(bc-ad)^2} 2Ab^3cfh \left( \left( i c \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \operatorname{EllipticPi} \left[ \right. \right. \right. \\
 & \left. \left. \left. \frac{(bc-ad)h}{b(-dg+ch)}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{-\frac{-dg+ch}{h}}}{\sqrt{c+dx}} \right], \frac{(-de+cf)h}{f(-dg+ch)} \right] \right) / \right. \\
 & \left( \sqrt{-\frac{-dg+ch}{h}} \sqrt{\left( fh + \frac{d^2eg}{(c+dx)^2} - \frac{cdfg}{(c+dx)^2} - \frac{cdeh}{(c+dx)^2} + \frac{c^2fh}{(c+dx)^2} + \right. \right. \\
 & \left. \left. \frac{dfg}{c+dx} + \frac{deh}{c+dx} - \frac{2cfh}{c+dx} \right) \right) - \left( i ad \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \right. \\
 & \left. \operatorname{EllipticPi} \left[ \frac{(bc-ad)h}{b(-dg+ch)}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{-\frac{-dg+ch}{h}}}{\sqrt{c+dx}} \right], \frac{(-de+cf)h}{f(-dg+ch)} \right] \right) / \right. \\
 & \left( b \sqrt{-\frac{-dg+ch}{h}} \sqrt{\left( fh + \frac{d^2eg}{(c+dx)^2} - \frac{cdfg}{(c+dx)^2} - \frac{cdeh}{(c+dx)^2} + \right. \right. \\
 & \left. \left. \frac{c^2fh}{(c+dx)^2} + \frac{dfg}{c+dx} + \frac{deh}{c+dx} - \frac{2cfh}{c+dx} \right) \right) \left. \right) - \frac{1}{(bc-ad)^2} \\
 & 2aAb^2dfh \left( \left( i c \sqrt{1 - \frac{-de+cf}{f(c+dx)}} \sqrt{1 - \frac{-dg+ch}{h(c+dx)}} \operatorname{EllipticPi} \left[ \frac{(bc-ad)h}{b(-dg+ch)}, \right. \right. \right. \\
 & \left. \left. \left. i \operatorname{ArcSinh} \left[ \frac{\sqrt{-\frac{-dg+ch}{h}}}{\sqrt{c+dx}} \right], \frac{(-de+cf)h}{f(-dg+ch)} \right] \right) / \left( \sqrt{-\frac{-dg+ch}{h}} \sqrt{\left( fh + \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left. \left( \frac{d^2 e g}{(c+dx)^2} - \frac{c d f g}{(c+dx)^2} - \frac{c d e h}{(c+dx)^2} + \frac{c^2 f h}{(c+dx)^2} + \frac{d f g}{c+dx} + \frac{d e h}{c+dx} - \frac{2 c f h}{c+dx} \right) \right) - \\
 & \left( i a d \sqrt{1 - \frac{-d e + c f}{f (c+dx)}} \sqrt{1 - \frac{-d g + c h}{h (c+dx)}} \operatorname{EllipticPi} \left[ \frac{(b c - a d) h}{b (-d g + c h)}, \right. \right. \\
 & \left. \left. i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{-d g + c h}{h}}}{\sqrt{c+dx}} \right], \frac{(-d e + c f) h}{f (-d g + c h)} \right] \right) / \left( b \sqrt{\frac{-d g + c h}{h}} \sqrt{f h +} \right. \\
 & \left. \left. \frac{d^2 e g}{(c+dx)^2} - \frac{c d f g}{(c+dx)^2} - \frac{c d e h}{(c+dx)^2} + \frac{c^2 f h}{(c+dx)^2} + \frac{d f g}{c+dx} + \frac{d e h}{c+dx} - \frac{2 c f h}{c+dx} \right) \right) + \\
 & \frac{1}{b c - a d} A b^2 f h \left( \left( i c \sqrt{1 - \frac{-d e + c f}{f (c+dx)}} \sqrt{1 - \frac{-d g + c h}{h (c+dx)}} \operatorname{EllipticPi} \left[ \frac{(b c - a d) h}{b (-d g + c h)}, \right. \right. \right. \\
 & \left. \left. i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{-d g + c h}{h}}}{\sqrt{c+dx}} \right], \frac{(-d e + c f) h}{f (-d g + c h)} \right] \right) / \left( \sqrt{\frac{-d g + c h}{h}} \sqrt{f h +} \right. \\
 & \left. \left. \frac{d^2 e g}{(c+dx)^2} - \frac{c d f g}{(c+dx)^2} - \frac{c d e h}{(c+dx)^2} + \frac{c^2 f h}{(c+dx)^2} + \frac{d f g}{c+dx} + \frac{d e h}{c+dx} - \frac{2 c f h}{c+dx} \right) \right) - \\
 & \left( i a d \sqrt{1 - \frac{-d e + c f}{f (c+dx)}} \sqrt{1 - \frac{-d g + c h}{h (c+dx)}} \operatorname{EllipticPi} \left[ \frac{(b c - a d) h}{b (-d g + c h)}, \right. \right. \\
 & \left. \left. i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{-d g + c h}{h}}}{\sqrt{c+dx}} \right], \frac{(-d e + c f) h}{f (-d g + c h)} \right] \right) / \left( b \sqrt{\frac{-d g + c h}{h}} \sqrt{f h +} \right.
 \end{aligned}$$

$$\left. \left( \frac{d^2 e g}{(c+dx)^2} - \frac{c d f g}{(c+dx)^2} - \frac{c d e h}{(c+dx)^2} + \frac{c^2 f h}{(c+dx)^2} + \frac{d f g}{c+dx} + \frac{d e h}{c+dx} - \frac{2 c f h}{c+dx} \right) \right) -$$

$$\frac{1}{b c - a d} a^2 C f h \left( \left( i c \sqrt{1 - \frac{-d e + c f}{f (c+dx)}} \sqrt{1 - \frac{-d g + c h}{h (c+dx)}} \operatorname{EllipticPi} \left[ \frac{(b c - a d) h}{b (-d g + c h)}, \right. \right. \right.$$

$$\left. \left. i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{-d g + c h}{h}}}{\sqrt{c+dx}} \right], \frac{(-d e + c f) h}{f (-d g + c h)} \right] \right) / \left( \sqrt{\frac{-d g + c h}{h}} \sqrt{f h +} \right.$$

$$\left. \left. \left. \left. \left. \frac{d^2 e g}{(c+dx)^2} - \frac{c d f g}{(c+dx)^2} - \frac{c d e h}{(c+dx)^2} + \frac{c^2 f h}{(c+dx)^2} + \frac{d f g}{c+dx} + \frac{d e h}{c+dx} - \frac{2 c f h}{c+dx} \right) \right) - \right.$$

$$\left. \left( i a d \sqrt{1 - \frac{-d e + c f}{f (c+dx)}} \sqrt{1 - \frac{-d g + c h}{h (c+dx)}} \operatorname{EllipticPi} \left[ \frac{(b c - a d) h}{b (-d g + c h)}, i \operatorname{ArcSinh} \left[ \right. \right. \right. \right.$$

$$\left. \left. \left. \left. \left. \frac{\sqrt{\frac{-d g + c h}{h}}}{\sqrt{c+dx}} \right], \frac{(-d e + c f) h}{f (-d g + c h)} \right] \right) / \left( b \sqrt{\frac{-d g + c h}{h}} \sqrt{f h + \frac{d^2 e g}{(c+dx)^2}} - \right.$$

$$\left. \left. \left. \left. \left. \frac{c d f g}{(c+dx)^2} - \frac{c d e h}{(c+dx)^2} + \frac{c^2 f h}{(c+dx)^2} + \frac{d f g}{c+dx} + \frac{d e h}{c+dx} - \frac{2 c f h}{c+dx} \right) \right) \right) \right) \right) /$$

$$\left( \left( -2 b^2 C e g + 2 a b C f g + 2 a b C e h + A b^2 f h - a^2 C f h + \frac{A b^2 d^2 e g}{(c+dx)^2} + \frac{a^2 C d^2 e g}{(c+dx)^2} - \right. \right.$$

$$\frac{A b^2 c d f g}{(c+dx)^2} - \frac{a^2 c C d f g}{(c+dx)^2} -$$

$$\left. \frac{A b^2 c d e h}{(c+dx)^2} - \frac{a^2 c C d e h}{(c+dx)^2} + \right.$$

$$\left( \begin{aligned} & \frac{A b^2 c^2 f h}{(c+dx)^2} + \frac{a^2 c^2 C f h}{(c+dx)^2} + \\ & \frac{2 b^2 c C e g}{c+dx} + \frac{2 a b C d e g}{c+dx} - \\ & \frac{2 a b c C f g}{c+dx} + \frac{2 A b^2 d f g}{c+dx} - \\ & \frac{2 a b c C e h}{c+dx} + \frac{2 A b^2 d e h}{c+dx} - \\ & \frac{2 A b^2 c f h}{c+dx} - \frac{2 a A b d f h}{c+dx} \end{aligned} \right) \left( \sqrt{e + \frac{(c+dx) \left( f - \frac{cf}{c+dx} \right)}{d}} \sqrt{g + \frac{(c+dx) \left( h - \frac{ch}{c+dx} \right)}{d}} \right)$$

**Problem 31: Result more than twice size of optimal antiderivative.**

$$\int \frac{(a+bx)^{3/2} (A+Cx^2)}{\sqrt{c+dx} \sqrt{e+fx} \sqrt{g+hx}} dx$$

Optimal (type 4, 1395 leaves, 10 steps):

$$\begin{aligned}
 & \left( (C(3adfh - 5b(dfg + deh + cfh)) (adfh - 3b(dfg + deh + cfh)) + \right. \\
 & \quad \left. 8bdfh(3Abdfh - C(2b(deg + cfg + ceh) + a(dfg + deh + cfh)))) \right) \\
 & \quad \sqrt{a+bx} \sqrt{e+fx} \sqrt{g+hx} \Big/ \left( 24bd^2f^3h^3 \sqrt{c+dx} \right) + \frac{1}{12d^2f^2h^2} \\
 & \frac{C(3adfh - 5b(dfg + deh + cfh)) \sqrt{a+bx} \sqrt{c+dx} \sqrt{e+fx} \sqrt{g+hx} +}{3dfh} \\
 & \left( \sqrt{dg - ch} \sqrt{fg - eh} (C(3adfh - 5b(dfg + deh + cfh)) (adfh - 3b(dfg + deh + cfh)) + \right. \\
 & \quad \left. 8bdfh(3Abdfh - C(2b(deg + cfg + ceh) + a(dfg + deh + cfh)))) \sqrt{a+bx} \right. \\
 & \quad \left. \sqrt{-\frac{(de - cf)(g + hx)}{(fg - eh)(c + dx)}} \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{dg - ch} \sqrt{e + fx}}{\sqrt{fg - eh} \sqrt{c + dx}}\right], \frac{(bc - ad)(fg - eh)}{(be - af)(dg - ch)}\right] \right) \Big/ \\
 & \left( 24bd^3f^3h^3 \sqrt{\frac{(de - cf)(a + bx)}{(be - af)(c + dx)}} \sqrt{g + hx} \right) + \\
 & \left( (be - af) \sqrt{bg - ah} (3a^2Cd^2f^2h^2 + 6abCdfh(cf + 2d(fg + eh)) - \right. \\
 & \quad \left. b^2(24Ad^2f^2h^2 + C(5c^2f^2h^2 + 4cdfh(fg + eh) + d^2(15f^2g^2 + 14efgh + 15e^2h^2))) \right) \\
 & \quad \sqrt{\frac{(be - af)(c + dx)}{(de - cf)(a + bx)}} \sqrt{g + hx} \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{bg - ah} \sqrt{e + fx}}{\sqrt{fg - eh} \sqrt{a + bx}}\right], \right. \\
 & \quad \left. -\frac{(bc - ad)(fg - eh)}{(de - cf)(bg - ah)} \right] \Big/ \left( 24b^2d^2f^3h^3 \sqrt{fg - eh} \sqrt{c + dx} \sqrt{-\frac{(be - af)(g + hx)}{(fg - eh)(a + bx)}} \right) - \\
 & \frac{1}{24b^2d^3 \sqrt{bc - ad} f^3h^4 \sqrt{c + dx} \sqrt{e + fx} \sqrt{-dg + ch}} \\
 & \left( 4bdfh(C(b(deg + cfg + ceh) + a(dfg + deh + cfh)) (3adfh - 5b(dfg + deh + cfh)) + \right. \\
 & \quad \left. 2dfh(3b^2cCeg + 2a^2C(dfg + deh + cfh) - ab(12Adfh - 5C(deg + cfg + ceh)))) \right) + \\
 & \left( adfh + b(dfg + deh + cfh) \right) (C(3adfh - 5b(dfg + deh + cfh)) \\
 & \quad (adfh - 3b(dfg + deh + cfh)) + \\
 & \quad \left. 8bdfh(3Abdfh - C(2b(deg + cfg + ceh) + a(dfg + deh + cfh)))) \right) \\
 & (a + bx) \sqrt{\frac{(bg - ah)(c + dx)}{(dg - ch)(a + bx)}} \sqrt{\frac{(bg - ah)(e + fx)}{(fg - eh)(a + bx)}} \operatorname{EllipticPi}\left[-\frac{b(dg - ch)}{(bc - ad)h}, \right. \\
 & \quad \left. \operatorname{ArcSin}\left[\frac{\sqrt{bc - ad} \sqrt{g + hx}}{\sqrt{-dg + ch} \sqrt{a + bx}}\right], \frac{(be - af)(dg - ch)}{(bc - ad)(fg - eh)} \right]
 \end{aligned}$$

Result (type 4, 38310 leaves): Display of huge result suppressed!

**Problem 32: Result more than twice size of optimal antiderivative.**

$$\int \frac{\sqrt{a+bx} (A+Cx^2)}{\sqrt{c+dx} \sqrt{e+fx} \sqrt{g+hx}} dx$$

Optimal (type 4, 937 leaves, 9 steps):

$$\begin{aligned} & \frac{C (a d f h - 3 b (d f g + d e h + c f h)) \sqrt{a+bx} \sqrt{e+fx} \sqrt{g+hx}}{4 b d f^2 h^2 \sqrt{c+dx}} + \\ & \frac{C \sqrt{a+bx} \sqrt{c+dx} \sqrt{e+fx} \sqrt{g+hx}}{2 d f h} - \\ & \left( C \sqrt{d g - c h} \sqrt{f g - e h} (a d f h - 3 b (d f g + d e h + c f h)) \sqrt{a+bx} \sqrt{-\frac{(d e - c f) (g + h x)}{(f g - e h) (c + d x)}} \right. \\ & \quad \left. \text{EllipticE} \left[ \text{ArcSin} \left[ \frac{\sqrt{d g - c h} \sqrt{e + f x}}{\sqrt{f g - e h} \sqrt{c + d x}} \right], \frac{(b c - a d) (f g - e h)}{(b e - a f) (d g - c h)} \right] \right) / \\ & \left( 4 b d^2 f^2 h^2 \sqrt{\frac{(d e - c f) (a + b x)}{(b e - a f) (c + d x)}} \sqrt{g + h x} \right) + \\ & \left( C (b e - a f) \sqrt{b g - a h} (a d f h + b (c f h + 3 d (f g + e h))) \sqrt{\frac{(b e - a f) (c + d x)}{(d e - c f) (a + b x)}} \right. \\ & \quad \left. \sqrt{g + h x} \text{EllipticF} \left[ \text{ArcSin} \left[ \frac{\sqrt{b g - a h} \sqrt{e + f x}}{\sqrt{f g - e h} \sqrt{a + b x}} \right], -\frac{(b c - a d) (f g - e h)}{(d e - c f) (b g - a h)} \right] \right) / \\ & \left( 4 b^2 d f^2 h^2 \sqrt{f g - e h} \sqrt{c + d x} \sqrt{-\frac{(b e - a f) (g + h x)}{(f g - e h) (a + b x)}} \right) - \\ & \left( \sqrt{-d g + c h} (C (a d f h - 3 b (d f g + d e h + c f h)) (a d f h + b (d f g + d e h + c f h)) - \right. \\ & \quad \left. 4 b d f h (2 A b d f h - C (b (d e g + c f g + c e h) + a (d f g + d e h + c f h)))) \right) \\ & (a + b x) \sqrt{\frac{(b g - a h) (c + d x)}{(d g - c h) (a + b x)}} \sqrt{\frac{(b g - a h) (e + f x)}{(f g - e h) (a + b x)}} \\ & \left. \text{EllipticPi} \left[ -\frac{b (d g - c h)}{(b c - a d) h}, \text{ArcSin} \left[ \frac{\sqrt{b c - a d} \sqrt{g + h x}}{\sqrt{-d g + c h} \sqrt{a + b x}} \right], \frac{(b e - a f) (d g - c h)}{(b c - a d) (f g - e h)} \right] \right) / \\ & (4 b^2 d^2 \sqrt{b c - a d} f^2 h^3 \sqrt{c + d x} \sqrt{e + f x}) \end{aligned}$$

Result (type 4, 16659 leaves):

$$\begin{aligned}
 & \frac{c \sqrt{a+bx} \sqrt{c+dx} \sqrt{e+fx} \sqrt{g+hx}}{2dfh} + \\
 & \frac{1}{2b^3dfh} \left( C (-3bdfg - 3bdeh - 3bcfh + adfh) (a+bx)^{5/2} \right. \\
 & \quad \left. \left( d + \frac{bc}{a+bx} - \frac{ad}{a+bx} \right) \left( f + \frac{be}{a+bx} - \frac{af}{a+bx} \right) \left( h + \frac{bg}{a+bx} - \frac{ah}{a+bx} \right) \right) / \\
 & \left( 2dfh \sqrt{c + \frac{(a+bx) \left( d - \frac{ad}{a+bx} \right)}{b}} \sqrt{e + \frac{(a+bx) \left( f - \frac{af}{a+bx} \right)}{b}} \sqrt{g + \frac{(a+bx) \left( h - \frac{ah}{a+bx} \right)}{b}} \right) + \\
 & \left( 1 / \left( 2dfh \sqrt{c + \frac{(a+bx) \left( d - \frac{ad}{a+bx} \right)}{b}} \sqrt{e + \frac{(a+bx) \left( f - \frac{af}{a+bx} \right)}{b}} \sqrt{g + \frac{(a+bx) \left( h - \frac{ah}{a+bx} \right)}{b}} \right) \right) \\
 & (a+bx)^{3/2} \sqrt{\left( \left( d + \frac{bc}{a+bx} - \frac{ad}{a+bx} \right) \left( f + \frac{be}{a+bx} - \frac{af}{a+bx} \right) \left( h + \frac{bg}{a+bx} - \frac{ah}{a+bx} \right) \right)} \\
 & \left( \left( 3b^4 c C d e f g^2 \sqrt{\frac{(bc-ad)(bg-ah) \left( -\frac{d}{-bc+ad} + \frac{1}{a+bx} \right)}{bdg-bch}} \right. \right. \\
 & \quad \left. \left( -\frac{f}{-be+af} + \frac{1}{a+bx} \right) \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{\frac{f}{-be+af} - \frac{h}{-bg+ah}}} \right. \\
 & \quad \left. \left( - \left( (bdg-bch) \text{EllipticE} \left[ \text{ArcSin} \left[ \sqrt{\frac{(be-af) \left( h + \frac{bg}{a+bx} - \frac{ah}{a+bx} \right)}{b(-fg+eh)}} \right], \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right) / \left( (bc-ad)(bg-ah) \right) - \frac{1}{-bc+ad} \right. \\
 & \quad \left. \left. d \text{EllipticF} \left[ \text{ArcSin} \left[ \sqrt{\frac{(be-af) \left( h + \frac{bg}{a+bx} - \frac{ah}{a+bx} \right)}{b(-fg+eh)}} \right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right) \right) / \\
 & \left( \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \sqrt{\left( d + \frac{bc-ad}{a+bx} \right) \left( f + \frac{be-af}{a+bx} \right) \left( h + \frac{bg-ah}{a+bx} \right)} \right) - \left( 3ab^3 C d^2 e f \right)
 \end{aligned}$$

$$\begin{aligned}
 & g^2 \sqrt{\frac{(bc-ad)(bg-ah)\left(-\frac{d}{-bc+ad} + \frac{1}{a+bx}\right)}{bdg-bch}} \left(-\frac{f}{-be+af} + \frac{1}{a+bx}\right) \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{\frac{f}{-be+af} - \frac{h}{-bg+ah}}} \\
 & \left( - \left( \left( (bdg-bch) \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\sqrt{\frac{(be-af)\left(h + \frac{bg}{a+bx} - \frac{ah}{a+bx}\right)}{b(-fg+eh)}}\right], \right. \right. \right. \\
 & \left. \left. \left. \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right) / \left( (bc-ad)(bg-ah) \right) - \frac{1}{-bc+ad} \right. \\
 & \left. \left. \left. d \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\sqrt{\frac{(be-af)\left(h + \frac{bg}{a+bx} - \frac{ah}{a+bx}\right)}{b(-fg+eh)}}\right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right) \right) \right) / \\
 & \left( \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right) \left(h + \frac{bg-ah}{a+bx}\right)} \right) - \\
 & \left( 3ab^3cd f^2 g^2 \sqrt{\frac{(bc-ad)(bg-ah)\left(-\frac{d}{-bc+ad} + \frac{1}{a+bx}\right)}{bdg-bch}} \right. \\
 & \left. \left(-\frac{f}{-be+af} + \frac{1}{a+bx}\right) \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{\frac{f}{-be+af} - \frac{h}{-bg+ah}}} \right. \\
 & \left. \left( - \left( \left( (bdg-bch) \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\sqrt{\frac{(be-af)\left(h + \frac{bg}{a+bx} - \frac{ah}{a+bx}\right)}{b(-fg+eh)}}\right], \right. \right. \right. \right. \\
 & \left. \left. \left. \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right) / \left( (bc-ad)(bg-ah) \right) - \frac{1}{-bc+ad} \right. \right. \\
 & \left. \left. \left. d \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\sqrt{\frac{(be-af)\left(h + \frac{bg}{a+bx} - \frac{ah}{a+bx}\right)}{b(-fg+eh)}}\right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right) \right) \right) / \\
 & \left( \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right) \left(h + \frac{bg-ah}{a+bx}\right)} \right) +
 \end{aligned}$$

$$\begin{aligned}
 & \left( 3 a^2 b^2 c d^2 f^2 g^2 \sqrt{\frac{(bc-ad)(bg-ah)\left(-\frac{d}{-bc+ad} + \frac{1}{a+bx}\right)}{bdg-bch}} \right. \\
 & \left. \left( -\frac{f}{-be+af} + \frac{1}{a+bx} \right) \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{\frac{f}{-be+af} - \frac{h}{-bg+ah}}} \right. \\
 & \left. \left( -\left( (bdg-bch) \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\sqrt{\frac{(be-af)\left(h + \frac{bg}{a+bx} - \frac{ah}{a+bx}\right)}{b(-fg+eh)}}\right], \right. \right. \right. \\
 & \left. \left. \left. \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right) / \left( (bc-ad)(bg-ah) \right) - \frac{1}{-bc+ad} \right. \\
 & \left. \left. \left. d \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\sqrt{\frac{(be-af)\left(h + \frac{bg}{a+bx} - \frac{ah}{a+bx}\right)}{b(-fg+eh)}}\right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right) \right) \right) / \\
 & \left( \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right) \left(h + \frac{bg-ah}{a+bx}\right)} \right) + \\
 & \left( 3 b^4 c c d e^2 g h \sqrt{\frac{(bc-ad)(bg-ah)\left(-\frac{d}{-bc+ad} + \frac{1}{a+bx}\right)}{bdg-bch}} \right. \\
 & \left. \left( -\frac{f}{-be+af} + \frac{1}{a+bx} \right) \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{\frac{f}{-be+af} - \frac{h}{-bg+ah}}} \right. \\
 & \left. \left( -\left( (bdg-bch) \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\sqrt{\frac{(be-af)\left(h + \frac{bg}{a+bx} - \frac{ah}{a+bx}\right)}{b(-fg+eh)}}\right], \right. \right. \right. \\
 & \left. \left. \left. \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right) / \left( (bc-ad)(bg-ah) \right) - \frac{1}{-bc+ad} \right. \\
 & \left. \left. \left. d \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\sqrt{\frac{(be-af)\left(h + \frac{bg}{a+bx} - \frac{ah}{a+bx}\right)}{b(-fg+eh)}}\right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right) \right) \right) /
 \end{aligned}$$

$$\begin{aligned}
 & \left( \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right) \left(h + \frac{bg-ah}{a+bx}\right)} \right) - \\
 & \left( 3ab^3Cd^2e^2gh \sqrt{\frac{(bc-ad)(bg-ah)\left(-\frac{d}{-bc+ad} + \frac{1}{a+bx}\right)}{bdg-bch}} \right. \\
 & \left. \left(-\frac{f}{-be+af} + \frac{1}{a+bx}\right) \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{\frac{f}{-be+af} - \frac{h}{-bg+ah}}} \right. \\
 & \left. \left. - \left( (bdg-bch) \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\sqrt{\frac{(be-af)\left(h + \frac{bg}{a+bx} - \frac{ah}{a+bx}\right)}{b(-fg+eh)}}\right], \right. \right. \right. \\
 & \left. \left. \left. \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right) / \left( (bc-ad)(bg-ah) \right) \right) - \frac{1}{-bc+ad} \\
 & \left. d \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\sqrt{\frac{(be-af)\left(h + \frac{bg}{a+bx} - \frac{ah}{a+bx}\right)}{b(-fg+eh)}}\right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right) \Bigg) / \\
 & \left( \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right) \left(h + \frac{bg-ah}{a+bx}\right)} \right) + \\
 & \left( 3b^4c^2Cefgh \sqrt{\frac{(bc-ad)(bg-ah)\left(-\frac{d}{-bc+ad} + \frac{1}{a+bx}\right)}{bdg-bch}} \right. \\
 & \left. \left(-\frac{f}{-be+af} + \frac{1}{a+bx}\right) \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{\frac{f}{-be+af} - \frac{h}{-bg+ah}}} \right. \\
 & \left. \left. - \left( (bdg-bch) \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\sqrt{\frac{(be-af)\left(h + \frac{bg}{a+bx} - \frac{ah}{a+bx}\right)}{b(-fg+eh)}}\right], \right. \right. \right. \\
 & \left. \left. \left. \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right) \right) / \left( (bc-ad)(bg-ah) \right) - \frac{1}{-bc+ad}
 \end{aligned}$$

$$\left( d \operatorname{EllipticF} \left[ \operatorname{ArcSin} \left[ \sqrt{\frac{(be-af) \left( h + \frac{bg}{a+bx} - \frac{ah}{a+bx} \right)}{b(-fg+eh)}} \right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right) /$$

$$\left( \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \sqrt{\left( d + \frac{bc-ad}{a+bx} \right) \left( f + \frac{be-af}{a+bx} \right) \left( h + \frac{bg-ah}{a+bx} \right)} \right) -$$

$$\left( 10 a b^3 c d e f g h \sqrt{\frac{(bc-ad)(bg-ah) \left( -\frac{d}{-bc+ad} + \frac{1}{a+bx} \right)}{bdg-bch}} \right.$$

$$\left. \left( -\frac{f}{-be+af} + \frac{1}{a+bx} \right) \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{\frac{f}{-be+af} - \frac{h}{-bg+ah}}} \right.$$

$$\left. - \left( (bdg-bch) \operatorname{EllipticE} \left[ \operatorname{ArcSin} \left[ \sqrt{\frac{(be-af) \left( h + \frac{bg}{a+bx} - \frac{ah}{a+bx} \right)}{b(-fg+eh)}} \right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right) / \left( (bc-ad)(bg-ah) \right) - \frac{1}{-bc+ad} \right)$$

$$\left( d \operatorname{EllipticF} \left[ \operatorname{ArcSin} \left[ \sqrt{\frac{(be-af) \left( h + \frac{bg}{a+bx} - \frac{ah}{a+bx} \right)}{b(-fg+eh)}} \right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right) /$$

$$\left( \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \sqrt{\left( d + \frac{bc-ad}{a+bx} \right) \left( f + \frac{be-af}{a+bx} \right) \left( h + \frac{bg-ah}{a+bx} \right)} \right) +$$

$$\left( 7 a^2 b^2 c d^2 e f g h \sqrt{\frac{(bc-ad)(bg-ah) \left( -\frac{d}{-bc+ad} + \frac{1}{a+bx} \right)}{bdg-bch}} \right.$$

$$\left. \left( -\frac{f}{-be+af} + \frac{1}{a+bx} \right) \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{\frac{f}{-be+af} - \frac{h}{-bg+ah}}} \right.$$

$$\left. - \left( (bdg-bch) \operatorname{EllipticE} \left[ \operatorname{ArcSin} \left[ \sqrt{\frac{(be-af) \left( h + \frac{bg}{a+bx} - \frac{ah}{a+bx} \right)}{b(-fg+eh)}} \right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right) \right)$$

$$\left. \left. \left. \left. \left. \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right/ ((bc-ad)(bg-ah)) \right) - \frac{1}{-bc+ad} \right. \\ \left. \left. \left. \left. \left. d \operatorname{EllipticF} \left[ \operatorname{ArcSin} \left[ \sqrt{\frac{(be-af) \left( h + \frac{bg}{a+bx} - \frac{ah}{a+bx} \right)}{b(-fg+eh)}} \right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right] \right) \right/ \right. \\ \left. \left. \left. \left. \left. \left( \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \sqrt{\left( d + \frac{bc-ad}{a+bx} \right) \left( f + \frac{be-af}{a+bx} \right) \left( h + \frac{bg-ah}{a+bx} \right)} \right) - \right. \right. \right. \\ \left. \left. \left. \left. \left. 3ab^3c^2cf^2gh \sqrt{\frac{(bc-ad)(bg-ah) \left( -\frac{d}{-bc+ad} + \frac{1}{a+bx} \right)}{bdg-bch}} \right. \right. \right. \\ \left. \left. \left. \left. \left. \left( -\frac{f}{-be+af} + \frac{1}{a+bx} \right) \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{\frac{f}{-be+af} - \frac{h}{-bg+ah}}} \right. \right. \right. \\ \left. \left. \left. \left. \left. \left( -\left( (bdg-bch) \operatorname{EllipticE} \left[ \operatorname{ArcSin} \left[ \sqrt{\frac{(be-af) \left( h + \frac{bg}{a+bx} - \frac{ah}{a+bx} \right)}{b(-fg+eh)}} \right], \right. \right. \right. \right. \right. \\ \left. \left. \left. \left. \left. \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right) \right/ ((bc-ad)(bg-ah)) \right) - \frac{1}{-bc+ad} \right. \right. \right. \\ \left. \left. \left. \left. \left. \left. d \operatorname{EllipticF} \left[ \operatorname{ArcSin} \left[ \sqrt{\frac{(be-af) \left( h + \frac{bg}{a+bx} - \frac{ah}{a+bx} \right)}{b(-fg+eh)}} \right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right] \right) \right) \right/ \right. \\ \left. \left. \left. \left. \left. \left( \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \sqrt{\left( d + \frac{bc-ad}{a+bx} \right) \left( f + \frac{be-af}{a+bx} \right) \left( h + \frac{bg-ah}{a+bx} \right)} \right) + \right. \right. \right. \\ \left. \left. \left. \left. \left. \left. 7a^2b^2ccdf^2gh \sqrt{\frac{(bc-ad)(bg-ah) \left( -\frac{d}{-bc+ad} + \frac{1}{a+bx} \right)}{bdg-bch}} \right. \right. \right. \\ \left. \left. \left. \left. \left. \left( -\frac{f}{-be+af} + \frac{1}{a+bx} \right) \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{\frac{f}{-be+af} - \frac{h}{-bg+ah}}} \right. \right. \right. \right. \right.$$

$$\begin{aligned}
 & \left( - \left( \left( (bdg - bch) \operatorname{EllipticE} \left[ \operatorname{ArcSin} \left[ \sqrt{\frac{(be - af) \left( h + \frac{bg}{a+bx} - \frac{ah}{a+bx} \right)}{b(-fg + eh)}} \right] \right), \right. \right. \\
 & \quad \left. \left. \frac{(-bc + ad)(-fg + eh)}{(-be + af)(-dg + ch)} \right) \right) / \left( (bc - ad)(bg - ah) \right) - \frac{1}{-bc + ad} \right. \\
 & \quad \left. d \operatorname{EllipticF} \left[ \operatorname{ArcSin} \left[ \sqrt{\frac{(be - af) \left( h + \frac{bg}{a+bx} - \frac{ah}{a+bx} \right)}{b(-fg + eh)}} \right] \right], \frac{(-bc + ad)(-fg + eh)}{(-be + af)(-dg + ch)} \right] \right) / \\
 & \left( \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \sqrt{\left( d + \frac{bc - ad}{a + bx} \right) \left( f + \frac{be - af}{a + bx} \right) \left( h + \frac{bg - ah}{a + bx} \right)} \right) - \\
 & \left( 4a^3 b c d^2 f^2 g h \sqrt{\frac{(bc - ad)(bg - ah) \left( -\frac{d}{-bc+ad} + \frac{1}{a+bx} \right)}{bdg - bch}} \right. \\
 & \quad \left. \left( -\frac{f}{-be + af} + \frac{1}{a + bx} \right) \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{\frac{f}{-be+af} - \frac{h}{-bg+ah}}} \right. \\
 & \quad \left. - \left( \left( (bdg - bch) \operatorname{EllipticE} \left[ \operatorname{ArcSin} \left[ \sqrt{\frac{(be - af) \left( h + \frac{bg}{a+bx} - \frac{ah}{a+bx} \right)}{b(-fg + eh)}} \right] \right), \right. \right. \right. \\
 & \quad \left. \left. \frac{(-bc + ad)(-fg + eh)}{(-be + af)(-dg + ch)} \right) \right) / \left( (bc - ad)(bg - ah) \right) - \frac{1}{-bc + ad} \right. \\
 & \quad \left. d \operatorname{EllipticF} \left[ \operatorname{ArcSin} \left[ \sqrt{\frac{(be - af) \left( h + \frac{bg}{a+bx} - \frac{ah}{a+bx} \right)}{b(-fg + eh)}} \right] \right], \frac{(-bc + ad)(-fg + eh)}{(-be + af)(-dg + ch)} \right] \right) / \\
 & \left( \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \sqrt{\left( d + \frac{bc - ad}{a + bx} \right) \left( f + \frac{be - af}{a + bx} \right) \left( h + \frac{bg - ah}{a + bx} \right)} \right) - \\
 & \left( 3a b^3 c c d e^2 h^2 \sqrt{\frac{(bc - ad)(bg - ah) \left( -\frac{d}{-bc+ad} + \frac{1}{a+bx} \right)}{bdg - bch}} \right)
 \end{aligned}$$

$$\left( -\frac{f}{-be+af} + \frac{1}{a+bx} \right) \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{\frac{f}{-be+af} - \frac{h}{-bg+ah}}}$$

$$\left( -\left( (bdg - bch) \text{EllipticE}\left[\text{ArcSin}\left[\sqrt{\frac{(be-af)\left(h + \frac{bg}{a+bx} - \frac{ah}{a+bx}\right)}{b(-fg+eh)}}\right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)}}\right] \right) / \left( (bc-ad)(bg-ah) \right) - \frac{1}{-bc+ad} \right)$$

$$d \text{EllipticF}\left[\text{ArcSin}\left[\sqrt{\frac{(be-af)\left(h + \frac{bg}{a+bx} - \frac{ah}{a+bx}\right)}{b(-fg+eh)}}\right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)}\right] \right) /$$

$$\left( \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right) \left(h + \frac{bg-ah}{a+bx}\right)} \right) +$$

$$\left( 3a^2 b^2 c d^2 e^2 h^2 \sqrt{\frac{(bc-ad)(bg-ah)\left(-\frac{d}{-bc+ad} + \frac{1}{a+bx}\right)}{bdg-bch}} \right)$$

$$\left( -\frac{f}{-be+af} + \frac{1}{a+bx} \right) \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{\frac{f}{-be+af} - \frac{h}{-bg+ah}}}$$

$$\left( -\left( (bdg - bch) \text{EllipticE}\left[\text{ArcSin}\left[\sqrt{\frac{(be-af)\left(h + \frac{bg}{a+bx} - \frac{ah}{a+bx}\right)}{b(-fg+eh)}}\right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)}}\right] \right) / \left( (bc-ad)(bg-ah) \right) - \frac{1}{-bc+ad} \right)$$

$$d \text{EllipticF}\left[\text{ArcSin}\left[\sqrt{\frac{(be-af)\left(h + \frac{bg}{a+bx} - \frac{ah}{a+bx}\right)}{b(-fg+eh)}}\right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)}\right] \right) /$$

$$\left( \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right) \left(h + \frac{bg-ah}{a+bx}\right)} \right) -$$

$$\begin{aligned}
 & \left( 3 a b^3 c^2 C e f h^2 \sqrt{\frac{(b c - a d) (b g - a h) \left(-\frac{d}{-b c + a d} + \frac{1}{a + b x}\right)}{b d g - b c h}} \right. \\
 & \left. \left(-\frac{f}{-b e + a f} + \frac{1}{a + b x}\right) \sqrt{\frac{-\frac{h}{-b g + a h} + \frac{1}{a + b x}}{\frac{f}{-b e + a f} - \frac{h}{-b g + a h}}} \right. \\
 & \left. \left( - \left( \left( (b d g - b c h) \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\sqrt{\frac{(b e - a f) \left(h + \frac{b g}{a + b x} - \frac{a h}{a + b x}\right)}{b (-f g + e h)}\right] \right], \right. \right. \right. \right. \\
 & \left. \left. \left. \frac{(-b c + a d) (-f g + e h)}{(-b e + a f) (-d g + c h)} \right) \right) / \left( (b c - a d) (b g - a h) \right) - \frac{1}{-b c + a d} \right. \\
 & \left. \left. \left. d \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\sqrt{\frac{(b e - a f) \left(h + \frac{b g}{a + b x} - \frac{a h}{a + b x}\right)}{b (-f g + e h)}\right] \right], \frac{(-b c + a d) (-f g + e h)}{(-b e + a f) (-d g + c h)} \right] \right) \right) / \\
 & \left( \sqrt{\frac{-\frac{f}{-b e + a f} + \frac{1}{a + b x}}{-\frac{f}{-b e + a f} + \frac{h}{-b g + a h}}} \sqrt{\left(d + \frac{b c - a d}{a + b x}\right) \left(f + \frac{b e - a f}{a + b x}\right) \left(h + \frac{b g - a h}{a + b x}\right)} \right) + \\
 & \left( 7 a^2 b^2 c C d e f h^2 \sqrt{\frac{(b c - a d) (b g - a h) \left(-\frac{d}{-b c + a d} + \frac{1}{a + b x}\right)}{b d g - b c h}} \right. \\
 & \left. \left(-\frac{f}{-b e + a f} + \frac{1}{a + b x}\right) \sqrt{\frac{-\frac{h}{-b g + a h} + \frac{1}{a + b x}}{\frac{f}{-b e + a f} - \frac{h}{-b g + a h}}} \right. \\
 & \left. \left( - \left( \left( (b d g - b c h) \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\sqrt{\frac{(b e - a f) \left(h + \frac{b g}{a + b x} - \frac{a h}{a + b x}\right)}{b (-f g + e h)}\right] \right], \right. \right. \right. \right. \\
 & \left. \left. \left. \frac{(-b c + a d) (-f g + e h)}{(-b e + a f) (-d g + c h)} \right) \right) / \left( (b c - a d) (b g - a h) \right) - \frac{1}{-b c + a d} \right. \\
 & \left. \left. \left. d \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\sqrt{\frac{(b e - a f) \left(h + \frac{b g}{a + b x} - \frac{a h}{a + b x}\right)}{b (-f g + e h)}\right] \right], \frac{(-b c + a d) (-f g + e h)}{(-b e + a f) (-d g + c h)} \right] \right) \right) /
 \end{aligned}$$

$$\begin{aligned}
 & \left( \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right) \left(h + \frac{bg-ah}{a+bx}\right)} \right) - \\
 & \left( 4a^3 b c d^2 e f h^2 \sqrt{\frac{(bc-ad)(bg-ah)\left(-\frac{d}{-bc+ad} + \frac{1}{a+bx}\right)}{bdg-bch}} \right. \\
 & \left. \left(-\frac{f}{-be+af} + \frac{1}{a+bx}\right) \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{\frac{f}{-be+af} - \frac{h}{-bg+ah}}} \right. \\
 & \left. \left. - \left( (bdg-bch) \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\sqrt{\frac{(be-af)\left(h + \frac{bg}{a+bx} - \frac{ah}{a+bx}\right)}{b(-fg+eh)}}\right], \right. \right. \right. \\
 & \left. \left. \left. \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right) / \left( (bc-ad)(bg-ah) \right) - \frac{1}{-bc+ad} \right. \\
 & \left. \left. \left. d \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\sqrt{\frac{(be-af)\left(h + \frac{bg}{a+bx} - \frac{ah}{a+bx}\right)}{b(-fg+eh)}}\right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right) \right) \right) / \\
 & \left( \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right) \left(h + \frac{bg-ah}{a+bx}\right)} \right) + \\
 & \left( 3a^2 b^2 c^2 C f^2 h^2 \sqrt{\frac{(bc-ad)(bg-ah)\left(-\frac{d}{-bc+ad} + \frac{1}{a+bx}\right)}{bdg-bch}} \right. \\
 & \left. \left(-\frac{f}{-be+af} + \frac{1}{a+bx}\right) \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{\frac{f}{-be+af} - \frac{h}{-bg+ah}}} \right. \\
 & \left. \left. - \left( (bdg-bch) \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\sqrt{\frac{(be-af)\left(h + \frac{bg}{a+bx} - \frac{ah}{a+bx}\right)}{b(-fg+eh)}}\right], \right. \right. \right. \\
 & \left. \left. \left. \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right) / \left( (bc-ad)(bg-ah) \right) - \frac{1}{-bc+ad} \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left. d \operatorname{EllipticF} \left[ \operatorname{ArcSin} \left[ \sqrt{\frac{(be-af) \left( h + \frac{bg}{a+bx} - \frac{ah}{a+bx} \right)}{b(-fg+eh)}} \right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right) / \\
 & \left( \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \sqrt{\left( d + \frac{bc-ad}{a+bx} \right) \left( f + \frac{be-af}{a+bx} \right) \left( h + \frac{bg-ah}{a+bx} \right)} \right) - \\
 & \left( 4a^3 b c C d f^2 h^2 \sqrt{\frac{(bc-ad)(bg-ah) \left( -\frac{d}{-bc+ad} + \frac{1}{a+bx} \right)}{bdg-bch}} \right. \\
 & \left. \left( -\frac{f}{-be+af} + \frac{1}{a+bx} \right) \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{\frac{f}{-be+af} - \frac{h}{-bg+ah}}} \right. \\
 & \left. \left( - \left( (bdg-bch) \operatorname{EllipticE} \left[ \operatorname{ArcSin} \left[ \sqrt{\frac{(be-af) \left( h + \frac{bg}{a+bx} - \frac{ah}{a+bx} \right)}{b(-fg+eh)}} \right], \right. \right. \right. \\
 & \left. \left. \left. \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right) / ((bc-ad)(bg-ah)) \right) - \frac{1}{-bc+ad} \\
 & \left. d \operatorname{EllipticF} \left[ \operatorname{ArcSin} \left[ \sqrt{\frac{(be-af) \left( h + \frac{bg}{a+bx} - \frac{ah}{a+bx} \right)}{b(-fg+eh)}} \right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right) / \\
 & \left( \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \sqrt{\left( d + \frac{bc-ad}{a+bx} \right) \left( f + \frac{be-af}{a+bx} \right) \left( h + \frac{bg-ah}{a+bx} \right)} \right) + \\
 & \left( a^4 C d^2 f^2 h^2 \sqrt{\frac{(bc-ad)(bg-ah) \left( -\frac{d}{-bc+ad} + \frac{1}{a+bx} \right)}{bdg-bch}} \right. \\
 & \left. \left( -\frac{f}{-be+af} + \frac{1}{a+bx} \right) \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{\frac{f}{-be+af} - \frac{h}{-bg+ah}}} \right. \\
 & \left. \left( - \left( (bdg-bch) \operatorname{EllipticE} \left[ \operatorname{ArcSin} \left[ \sqrt{\frac{(be-af) \left( h + \frac{bg}{a+bx} - \frac{ah}{a+bx} \right)}{b(-fg+eh)}} \right], \right. \right. \right. \right.
 \end{aligned}$$

$$\left. \left. \left. \left. \left. \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right) \right/ \left( (bc-ad)(bg-ah) \right) \right) - \frac{1}{-bc+ad} \right. \\ \left. d \operatorname{EllipticF} \left[ \operatorname{ArcSin} \left[ \sqrt{\frac{(be-af) \left( h + \frac{bg}{a+bx} - \frac{ah}{a+bx} \right)}{b(-fg+eh)}} \right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right] \right/ \\ \left( \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \sqrt{\left( d + \frac{bc-ad}{a+bx} \right) \left( f + \frac{be-af}{a+bx} \right) \left( h + \frac{bg-ah}{a+bx} \right)} \right) + \\ \left( 2b^3 c d e f g h \sqrt{\frac{-\frac{d}{-bc+ad} + \frac{1}{a+bx}}{-\frac{d}{-bc+ad} + \frac{h}{-bg+ah}}} \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \left( -\frac{h}{-bg+ah} + \frac{1}{a+bx} \right) \right. \\ \left. \operatorname{EllipticF} \left[ \operatorname{ArcSin} \left[ \sqrt{\frac{(-be+af) \left( -h - \frac{bg}{a+bx} + \frac{ah}{a+bx} \right)}{b(-fg+eh)}} \right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right] \right/ \\ \left( \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{\frac{f}{-be+af} - \frac{h}{-bg+ah}}} \sqrt{\left( d + \frac{bc-ad}{a+bx} \right) \left( f + \frac{be-af}{a+bx} \right) \left( h + \frac{bg-ah}{a+bx} \right)} \right) - \\ \left( 2a b^2 C d^2 e f g h \sqrt{\frac{-\frac{d}{-bc+ad} + \frac{1}{a+bx}}{-\frac{d}{-bc+ad} + \frac{h}{-bg+ah}}} \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \left( -\frac{h}{-bg+ah} + \frac{1}{a+bx} \right) \right. \\ \left. \operatorname{EllipticF} \left[ \operatorname{ArcSin} \left[ \sqrt{\frac{(-be+af) \left( -h - \frac{bg}{a+bx} + \frac{ah}{a+bx} \right)}{b(-fg+eh)}} \right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right] \right/ \\ \left( \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{\frac{f}{-be+af} - \frac{h}{-bg+ah}}} \sqrt{\left( d + \frac{bc-ad}{a+bx} \right) \left( f + \frac{be-af}{a+bx} \right) \left( h + \frac{bg-ah}{a+bx} \right)} \right) - \\ \left( 2a b^2 c C d f^2 g h \sqrt{\frac{-\frac{d}{-bc+ad} + \frac{1}{a+bx}}{-\frac{d}{-bc+ad} + \frac{h}{-bg+ah}}} \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \left( -\frac{h}{-bg+ah} + \frac{1}{a+bx} \right) \right. \\ \left. \operatorname{EllipticF} \left[ \operatorname{ArcSin} \left[ \sqrt{\frac{(-be+af) \left( -h - \frac{bg}{a+bx} + \frac{ah}{a+bx} \right)}{b(-fg+eh)}} \right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right] \right/$$

$$\begin{aligned}
 & \left( \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{\frac{f}{-be+af} - \frac{h}{-bg+ah}}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right) \left(h + \frac{bg-ah}{a+bx}\right)} \right) + \\
 & \left( 2a^2 b c d^2 f^2 g h \sqrt{\frac{-\frac{d}{-bc+ad} + \frac{1}{a+bx}}{-\frac{d}{-bc+ad} + \frac{h}{-bg+ah}}} \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \left(-\frac{h}{-bg+ah} + \frac{1}{a+bx}\right) \right. \\
 & \quad \left. \text{EllipticF}\left[\text{ArcSin}\left[\sqrt{\frac{(-be+af) \left(-h - \frac{bg}{a+bx} + \frac{ah}{a+bx}\right)}{b(-fg+eh)}}\right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)}\right] \right) / \\
 & \left( \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{\frac{f}{-be+af} - \frac{h}{-bg+ah}}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right) \left(h + \frac{bg-ah}{a+bx}\right)} \right) - \\
 & \left( 2a b^2 c c d e f h^2 \sqrt{\frac{-\frac{d}{-bc+ad} + \frac{1}{a+bx}}{-\frac{d}{-bc+ad} + \frac{h}{-bg+ah}}} \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \left(-\frac{h}{-bg+ah} + \frac{1}{a+bx}\right) \right. \\
 & \quad \left. \text{EllipticF}\left[\text{ArcSin}\left[\sqrt{\frac{(-be+af) \left(-h - \frac{bg}{a+bx} + \frac{ah}{a+bx}\right)}{b(-fg+eh)}}\right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)}\right] \right) / \\
 & \left( \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{\frac{f}{-be+af} - \frac{h}{-bg+ah}}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right) \left(h + \frac{bg-ah}{a+bx}\right)} \right) + \\
 & \left( 2a^2 b c d^2 e f h^2 \sqrt{\frac{-\frac{d}{-bc+ad} + \frac{1}{a+bx}}{-\frac{d}{-bc+ad} + \frac{h}{-bg+ah}}} \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \left(-\frac{h}{-bg+ah} + \frac{1}{a+bx}\right) \right. \\
 & \quad \left. \text{EllipticF}\left[\text{ArcSin}\left[\sqrt{\frac{(-be+af) \left(-h - \frac{bg}{a+bx} + \frac{ah}{a+bx}\right)}{b(-fg+eh)}}\right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)}\right] \right) / \\
 & \left( \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{\frac{f}{-be+af} - \frac{h}{-bg+ah}}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right) \left(h + \frac{bg-ah}{a+bx}\right)} \right) + \\
 & \left( 2a^2 b c c d f^2 h^2 \sqrt{\frac{-\frac{d}{-bc+ad} + \frac{1}{a+bx}}{-\frac{d}{-bc+ad} + \frac{h}{-bg+ah}}} \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \left(-\frac{h}{-bg+ah} + \frac{1}{a+bx}\right) \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left. \text{EllipticF} \left[ \text{ArcSin} \left[ \sqrt{\frac{(-be+af) \left(-h - \frac{bg}{a+bx} + \frac{ah}{a+bx}\right)}{b(-fg+eh)}} \right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right/ \\
 & \left( \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{\frac{f}{-be+af} - \frac{h}{-bg+ah}}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right) \left(h + \frac{bg-ah}{a+bx}\right)} \right) - \\
 & \left( 2a^3 C d^2 f^2 h^2 \sqrt{\frac{-\frac{d}{-bc+ad} + \frac{1}{a+bx}}{\frac{d}{-bc+ad} + \frac{h}{-bg+ah}}} \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \left(-\frac{h}{-bg+ah} + \frac{1}{a+bx}\right) \right) \\
 & \left. \text{EllipticF} \left[ \text{ArcSin} \left[ \sqrt{\frac{(-be+af) \left(-h - \frac{bg}{a+bx} + \frac{ah}{a+bx}\right)}{b(-fg+eh)}} \right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right/ \\
 & \left( \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{\frac{f}{-be+af} - \frac{h}{-bg+ah}}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right) \left(h + \frac{bg-ah}{a+bx}\right)} \right) + \\
 & \left( 2b^2 C d^2 e f g (-bg+ah) \left(-\frac{f}{-be+af} + \frac{h}{-bg+ah}\right) \sqrt{\frac{-\frac{d}{-bc+ad} + \frac{1}{a+bx}}{\frac{d}{-bc+ad} + \frac{h}{-bg+ah}}} \right) \\
 & \sqrt{-\frac{\left(-\frac{f}{-be+af} + \frac{1}{a+bx}\right) \left(-\frac{h}{-bg+ah} + \frac{1}{a+bx}\right)}{\left(-\frac{f}{-be+af} + \frac{h}{-bg+ah}\right)^2}} \text{EllipticPi} \left[ -\frac{-bfg+beh}{(-be+af)h}, \right. \\
 & \left. \text{ArcSin} \left[ \sqrt{\frac{(-be+af) \left(-h - \frac{bg}{a+bx} + \frac{ah}{a+bx}\right)}{b(-fg+eh)}} \right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right/ \\
 & \left( \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right) \left(h + \frac{bg-ah}{a+bx}\right)} \right) + \\
 & \left( 2b^2 c C d f^2 g (-bg+ah) \left(-\frac{f}{-be+af} + \frac{h}{-bg+ah}\right) \sqrt{\frac{-\frac{d}{-bc+ad} + \frac{1}{a+bx}}{\frac{d}{-bc+ad} + \frac{h}{-bg+ah}}} \right) \\
 & \sqrt{-\frac{\left(-\frac{f}{-be+af} + \frac{1}{a+bx}\right) \left(-\frac{h}{-bg+ah} + \frac{1}{a+bx}\right)}{\left(-\frac{f}{-be+af} + \frac{h}{-bg+ah}\right)^2}} \text{EllipticPi} \left[ -\frac{-bfg+beh}{(-be+af)h}, \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left. \text{ArcSin} \left[ \sqrt{\frac{(-be+af) \left(-h - \frac{bg}{a+bx} + \frac{ah}{a+bx}\right)}{b(-fg+eh)}} \right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] / \\
 & \left( \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right) \left(h + \frac{bg-ah}{a+bx}\right)} \right) - \\
 & \left( 2abc d^2 f^2 g (-bg+ah) \left(-\frac{f}{-be+af} + \frac{h}{-bg+ah}\right) \sqrt{\frac{-\frac{d}{-bc+ad} + \frac{1}{a+bx}}{-\frac{d}{-bc+ad} + \frac{h}{-bg+ah}}} \right. \\
 & \left. \sqrt{-\frac{\left(-\frac{f}{-be+af} + \frac{1}{a+bx}\right) \left(-\frac{h}{-bg+ah} + \frac{1}{a+bx}\right)}{\left(-\frac{f}{-be+af} + \frac{h}{-bg+ah}\right)^2}} \text{EllipticPi} \left[-\frac{-bfg+beh}{(-be+af)h}, \right. \right. \\
 & \left. \left. \text{ArcSin} \left[ \sqrt{\frac{(-be+af) \left(-h - \frac{bg}{a+bx} + \frac{ah}{a+bx}\right)}{b(-fg+eh)}} \right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] / \right. \\
 & \left. \left( \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right) \left(h + \frac{bg-ah}{a+bx}\right)} \right) + \right. \\
 & \left( 3b^2 C d^2 f^2 g^2 (-bg+ah) \left(-\frac{f}{-be+af} + \frac{h}{-bg+ah}\right) \sqrt{\frac{-\frac{d}{-bc+ad} + \frac{1}{a+bx}}{-\frac{d}{-bc+ad} + \frac{h}{-bg+ah}}} \right. \\
 & \left. \sqrt{-\frac{\left(-\frac{f}{-be+af} + \frac{1}{a+bx}\right) \left(-\frac{h}{-bg+ah} + \frac{1}{a+bx}\right)}{\left(-\frac{f}{-be+af} + \frac{h}{-bg+ah}\right)^2}} \text{EllipticPi} \left[-\frac{-bfg+beh}{(-be+af)h}, \right. \right. \\
 & \left. \left. \text{ArcSin} \left[ \sqrt{\frac{(-be+af) \left(-h - \frac{bg}{a+bx} + \frac{ah}{a+bx}\right)}{b(-fg+eh)}} \right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] / \right. \\
 & \left. \left( h \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right) \left(h + \frac{bg-ah}{a+bx}\right)} \right) + \right. \\
 & \left( 3b^2 C d^2 e^2 h (-bg+ah) \left(-\frac{f}{-be+af} + \frac{h}{-bg+ah}\right) \sqrt{\frac{-\frac{d}{-bc+ad} + \frac{1}{a+bx}}{-\frac{d}{-bc+ad} + \frac{h}{-bg+ah}}} \right)
 \end{aligned}$$

$$\begin{aligned}
 & \sqrt{-\frac{\left(-\frac{f}{-be+af} + \frac{1}{a+bx}\right) \left(-\frac{h}{-bg+ah} + \frac{1}{a+bx}\right)}{\left(-\frac{f}{-be+af} + \frac{h}{-bg+ah}\right)^2}} \operatorname{EllipticPi}\left[-\frac{-bfg+beh}{(-be+af)h}, \right. \\
 & \left. \operatorname{ArcSin}\left[\sqrt{\frac{(-be+af)\left(-h-\frac{bg}{a+bx} + \frac{ah}{a+bx}\right)}{b(-fg+eh)}}, \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)}\right]\right] / \\
 & \left(\sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right) \left(h + \frac{bg-ah}{a+bx}\right)}\right) + \\
 & \left(2b^2 c C d e f h (-bg+ah) \left(-\frac{f}{-be+af} + \frac{h}{-bg+ah}\right) \sqrt{\frac{-\frac{d}{-bc+ad} + \frac{1}{a+bx}}{-\frac{d}{-bc+ad} + \frac{h}{-bg+ah}}}\right. \\
 & \left.\sqrt{-\frac{\left(-\frac{f}{-be+af} + \frac{1}{a+bx}\right) \left(-\frac{h}{-bg+ah} + \frac{1}{a+bx}\right)}{\left(-\frac{f}{-be+af} + \frac{h}{-bg+ah}\right)^2}} \operatorname{EllipticPi}\left[-\frac{-bfg+beh}{(-be+af)h}, \right. \right. \\
 & \left. \left. \operatorname{ArcSin}\left[\sqrt{\frac{(-be+af)\left(-h-\frac{bg}{a+bx} + \frac{ah}{a+bx}\right)}{b(-fg+eh)}}, \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)}\right]\right]\right) / \\
 & \left(\sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right) \left(h + \frac{bg-ah}{a+bx}\right)}\right) - \\
 & \left(2abCd^2efh(-bg+ah) \left(-\frac{f}{-be+af} + \frac{h}{-bg+ah}\right) \sqrt{\frac{-\frac{d}{-bc+ad} + \frac{1}{a+bx}}{-\frac{d}{-bc+ad} + \frac{h}{-bg+ah}}}\right. \\
 & \left.\sqrt{-\frac{\left(-\frac{f}{-be+af} + \frac{1}{a+bx}\right) \left(-\frac{h}{-bg+ah} + \frac{1}{a+bx}\right)}{\left(-\frac{f}{-be+af} + \frac{h}{-bg+ah}\right)^2}} \operatorname{EllipticPi}\left[-\frac{-bfg+beh}{(-be+af)h}, \right. \right. \\
 & \left. \left. \operatorname{ArcSin}\left[\sqrt{\frac{(-be+af)\left(-h-\frac{bg}{a+bx} + \frac{ah}{a+bx}\right)}{b(-fg+eh)}}, \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)}\right]\right]\right) / \\
 & \left(\sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right) \left(h + \frac{bg-ah}{a+bx}\right)}\right) +
 \end{aligned}$$

$$\left( 3 b^2 c^2 C f^2 h (-bg+ah) \left( -\frac{f}{-be+af} + \frac{h}{-bg+ah} \right) \sqrt{\frac{-\frac{d}{-bc+ad} + \frac{1}{a+bx}}{-\frac{d}{-bc+ad} + \frac{h}{-bg+ah}}} \right.$$

$$\sqrt{-\frac{\left(-\frac{f}{-be+af} + \frac{1}{a+bx}\right) \left(-\frac{h}{-bg+ah} + \frac{1}{a+bx}\right)}{\left(-\frac{f}{-be+af} + \frac{h}{-bg+ah}\right)^2}} \operatorname{EllipticPi}\left[-\frac{-bfg+beh}{(-be+af)h}, \right.$$

$$\left. \operatorname{ArcSin}\left[\sqrt{\frac{(-be+af)\left(-h-\frac{bg}{a+bx} + \frac{ah}{a+bx}\right)}{b(-fg+eh)}}, \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)}\right] \right) /$$

$$\left( \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right) \left(h + \frac{bg-ah}{a+bx}\right)} \right) -$$

$$\left( 2 a b c C d f^2 h (-bg+ah) \left( -\frac{f}{-be+af} + \frac{h}{-bg+ah} \right) \sqrt{\frac{-\frac{d}{-bc+ad} + \frac{1}{a+bx}}{-\frac{d}{-bc+ad} + \frac{h}{-bg+ah}}} \right.$$

$$\sqrt{-\frac{\left(-\frac{f}{-be+af} + \frac{1}{a+bx}\right) \left(-\frac{h}{-bg+ah} + \frac{1}{a+bx}\right)}{\left(-\frac{f}{-be+af} + \frac{h}{-bg+ah}\right)^2}} \operatorname{EllipticPi}\left[-\frac{-bfg+beh}{(-be+af)h}, \right.$$

$$\left. \operatorname{ArcSin}\left[\sqrt{\frac{(-be+af)\left(-h-\frac{bg}{a+bx} + \frac{ah}{a+bx}\right)}{b(-fg+eh)}}, \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)}\right] \right) /$$

$$\left( \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right) \left(h + \frac{bg-ah}{a+bx}\right)} \right) +$$

$$\left( 8 A b^2 d^2 f^2 h (-bg+ah) \left( -\frac{f}{-be+af} + \frac{h}{-bg+ah} \right) \sqrt{\frac{-\frac{d}{-bc+ad} + \frac{1}{a+bx}}{-\frac{d}{-bc+ad} + \frac{h}{-bg+ah}}} \right.$$

$$\sqrt{-\frac{\left(-\frac{f}{-be+af} + \frac{1}{a+bx}\right) \left(-\frac{h}{-bg+ah} + \frac{1}{a+bx}\right)}{\left(-\frac{f}{-be+af} + \frac{h}{-bg+ah}\right)^2}} \operatorname{EllipticPi}\left[-\frac{-bfg+beh}{(-be+af)h}, \right.$$

$$\left. \operatorname{ArcSin}\left[\sqrt{\frac{(-be+af)\left(-h-\frac{bg}{a+bx} + \frac{ah}{a+bx}\right)}{b(-fg+eh)}}, \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)}\right] \right) /$$

$$\left( \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right) \left(h + \frac{bg-ah}{a+bx}\right)} - \right. \\ \left. a^2 C d^2 f^2 h (-bg+ah) \left(-\frac{f}{-be+af} + \frac{h}{-bg+ah}\right) \sqrt{\frac{-\frac{d}{-bc+ad} + \frac{1}{a+bx}}{-\frac{d}{-bc+ad} + \frac{h}{-bg+ah}}} \right. \\ \left. \sqrt{-\frac{\left(-\frac{f}{-be+af} + \frac{1}{a+bx}\right) \left(-\frac{h}{-bg+ah} + \frac{1}{a+bx}\right)}{\left(-\frac{f}{-be+af} + \frac{h}{-bg+ah}\right)^2}} \text{EllipticPi}\left[-\frac{-bfg+beh}{(-be+af)h}, \right. \right. \\ \left. \left. \text{ArcSin}\left[\sqrt{\frac{(-be+af)\left(-h - \frac{bg}{a+bx} + \frac{ah}{a+bx}\right)}{b(-fg+eh)}}, \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)}\right]\right] \right) / \\ \left( \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right) \left(h + \frac{bg-ah}{a+bx}\right)} \right) \Bigg)$$

**Problem 33: Result more than twice size of optimal antiderivative.**

$$\int \frac{A + Cx^2}{\sqrt{a+bx} \sqrt{c+dx} \sqrt{e+fx} \sqrt{g+hx}} dx$$

Optimal (type 4, 757 leaves, 8 steps):

$$\frac{c \sqrt{a+bx} \sqrt{e+fx} \sqrt{g+hx}}{bfh \sqrt{c+dx}} - \left( c \sqrt{dg-ch} \sqrt{fg-eh} \sqrt{a+bx} \sqrt{-\frac{(de-cf)(g+hx)}{(fg-eh)(c+dx)}} \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{dg-ch} \sqrt{e+fx}}{\sqrt{fg-eh} \sqrt{c+dx}}\right]\right], \right. \\
 \left. \frac{(bc-ad)(fg-eh)}{(be-af)(dg-ch)} \right) / \left( bdfh \sqrt{\frac{(de-cf)(a+bx)}{(be-af)(c+dx)}} \sqrt{g+hx} \right) + \\
 \left( a^2 c f h + a b c (fg+eh) - b^2 (c e g - 2 a f h) \right) \sqrt{\frac{(be-af)(c+dx)}{(de-cf)(a+bx)}} \sqrt{g+hx} \\
 \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{bg-ah} \sqrt{e+fx}}{\sqrt{fg-eh} \sqrt{a+bx}}\right], -\frac{(bc-ad)(fg-eh)}{(de-cf)(bg-ah)}\right] / \\
 \left( b^2 f h \sqrt{bg-ah} \sqrt{fg-eh} \sqrt{c+dx} \sqrt{-\frac{(be-af)(g+hx)}{(fg-eh)(a+bx)}} \right) - \\
 \left( c \sqrt{-dg+ch} (adfh + b(dfg+deh+cfh)) (a+bx) \sqrt{\frac{(bg-ah)(c+dx)}{(dg-ch)(a+bx)}} \right. \\
 \left. \sqrt{\frac{(bg-ah)(e+fx)}{(fg-eh)(a+bx)}} \operatorname{EllipticPi}\left[-\frac{b(dg-ch)}{(bc-ad)h}, \operatorname{ArcSin}\left[\frac{\sqrt{bc-ad} \sqrt{g+hx}}{\sqrt{-dg+ch} \sqrt{a+bx}}\right]\right], \right. \\
 \left. \frac{(be-af)(dg-ch)}{(bc-ad)(fg-eh)} \right) / \left( b^2 d \sqrt{bc-ad} f h^2 \sqrt{c+dx} \sqrt{e+fx} \right)$$

Result(type 4, 6207 leaves):

$$-\frac{1}{b^3} 2 \left( \left( c (a+bx)^{5/2} \left( d + \frac{bc}{a+bx} - \frac{ad}{a+bx} \right) \left( f + \frac{be}{a+bx} - \frac{af}{a+bx} \right) \left( h + \frac{bg}{a+bx} - \frac{ah}{a+bx} \right) \right) / \right. \\
 \left. \left( 2 d f h \sqrt{c + \frac{(a+bx)(d - \frac{ad}{a+bx})}{b}} \sqrt{e + \frac{(a+bx)(f - \frac{af}{a+bx})}{b}} \sqrt{g + \frac{(a+bx)(h - \frac{ah}{a+bx})}{b}} \right) \right) + \\
 \left( 1 / \left( 2 d f h \sqrt{c + \frac{(a+bx)(d - \frac{ad}{a+bx})}{b}} \sqrt{e + \frac{(a+bx)(f - \frac{af}{a+bx})}{b}} \sqrt{g + \frac{(a+bx)(h - \frac{ah}{a+bx})}{b}} \right) \right) \\
 (a+bx)^{3/2} \sqrt{\left( \left( d + \frac{bc}{a+bx} - \frac{ad}{a+bx} \right) \left( f + \frac{be}{a+bx} - \frac{af}{a+bx} \right) \left( h + \frac{bg}{a+bx} - \frac{ah}{a+bx} \right) \right)}$$

$$\left( \left( b^3 c C e g \sqrt{\frac{(bc-ad)(bg-ah) \left(-\frac{d}{-bc+ad} + \frac{1}{a+bx}\right)}{bdg-bch}} \right. \right.$$

$$\left. \left. \left( -\frac{f}{-be+af} + \frac{1}{a+bx} \right) \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{\frac{f}{-be+af} - \frac{h}{-bg+ah}}} \left( - \left( (bdg-bch) \text{EllipticE} \left[ \right. \right. \right. \right.$$

$$\left. \left. \left. \text{ArcSin} \left[ \sqrt{\frac{(be-af) \left( h + \frac{bg}{a+bx} - \frac{ah}{a+bx} \right)}{b(-fg+eh)}} \right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right) \right) \right) /$$

$$\left( (bc-ad)(bg-ah) \right) \left. - \frac{1}{-bc+ad} d \text{EllipticF} \left[ \text{ArcSin} \left[ \right. \right. \right. \right.$$

$$\left. \left. \left. \sqrt{\frac{(be-af) \left( h + \frac{bg}{a+bx} - \frac{ah}{a+bx} \right)}{b(-fg+eh)}} \right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right) \right) /$$

$$\left( \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \sqrt{\left( d + \frac{bc-ad}{a+bx} \right) \left( f + \frac{be-af}{a+bx} \right) \left( h + \frac{bg-ah}{a+bx} \right)} \right) -$$

$$\left( a b^2 C d e g \sqrt{\frac{(bc-ad)(bg-ah) \left(-\frac{d}{-bc+ad} + \frac{1}{a+bx}\right)}{bdg-bch}} \left( -\frac{f}{-be+af} + \frac{1}{a+bx} \right) \right.$$

$$\left. \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{\frac{f}{-be+af} - \frac{h}{-bg+ah}}} \left( - \left( (bdg-bch) \text{EllipticE} \left[ \right. \right. \right. \right.$$

$$\left. \left. \left. \text{ArcSin} \left[ \sqrt{\frac{(be-af) \left( h + \frac{bg}{a+bx} - \frac{ah}{a+bx} \right)}{b(-fg+eh)}} \right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right) \right) \right) /$$

$$\left( (bc-ad)(bg-ah) \right) \left. - \frac{1}{-bc+ad} d \text{EllipticF} \left[ \text{ArcSin} \left[ \right. \right. \right. \right.$$

$$\left. \left. \left. \sqrt{\frac{(be-af) \left( h + \frac{bg}{a+bx} - \frac{ah}{a+bx} \right)}{b(-fg+eh)}} \right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right) \right) /$$

$$\begin{aligned}
 & \left( \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right) \left(h + \frac{bg-ah}{a+bx}\right)} \right) - \\
 & \left( ab^2 c C f g \sqrt{\frac{(bc-ad)(bg-ah) \left(-\frac{d}{-bc+ad} + \frac{1}{a+bx}\right)}{bdg-bch}} \left(-\frac{f}{-be+af} + \frac{1}{a+bx}\right) \right. \\
 & \left. \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{-\frac{f}{-be+af} - \frac{h}{-bg+ah}}} \left( \left( (bdg-bch) \text{EllipticE} \left[ \right. \right. \right. \right. \\
 & \left. \left. \left. \left. \text{ArcSin} \left[ \sqrt{\frac{(be-af) \left(h + \frac{bg}{a+bx} - \frac{ah}{a+bx}\right)}{b(-fg+eh)}} \right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right) / \right. \right. \\
 & \left. \left. \left( (bc-ad)(bg-ah) \right) \right) - \frac{1}{-bc+ad} d \text{EllipticF} \left[ \text{ArcSin} \left[ \right. \right. \right. \right. \\
 & \left. \left. \left. \left. \sqrt{\frac{(be-af) \left(h + \frac{bg}{a+bx} - \frac{ah}{a+bx}\right)}{b(-fg+eh)}} \right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right) / \right. \\
 & \left. \left( \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right) \left(h + \frac{bg-ah}{a+bx}\right)} \right) + \\
 & \left( a^2 b C d f g \sqrt{\frac{(bc-ad)(bg-ah) \left(-\frac{d}{-bc+ad} + \frac{1}{a+bx}\right)}{bdg-bch}} \left(-\frac{f}{-be+af} + \frac{1}{a+bx}\right) \right. \\
 & \left. \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{-\frac{f}{-be+af} - \frac{h}{-bg+ah}}} \left( \left( (bdg-bch) \text{EllipticE} \left[ \right. \right. \right. \right. \right. \\
 & \left. \left. \left. \left. \text{ArcSin} \left[ \sqrt{\frac{(be-af) \left(h + \frac{bg}{a+bx} - \frac{ah}{a+bx}\right)}{b(-fg+eh)}} \right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right) / \right. \\
 & \left. \left. \left( (bc-ad)(bg-ah) \right) \right) - \frac{1}{-bc+ad} d \text{EllipticF} \left[ \text{ArcSin} \left[ \right. \right. \right. \right.
 \end{aligned}$$

$$\left( \sqrt{\frac{(be-af) \left( h + \frac{bg}{a+bx} - \frac{ah}{a+bx} \right)}{b(-fg+eh)}} \right), \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \Bigg) /$$

$$\left( \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \sqrt{\left( d + \frac{bc-ad}{a+bx} \right) \left( f + \frac{be-af}{a+bx} \right) \left( h + \frac{bg-ah}{a+bx} \right)} \right) -$$

$$\left( ab^2cCeh \sqrt{\frac{(bc-ad)(bg-ah) \left( -\frac{d}{-bc+ad} + \frac{1}{a+bx} \right)}{bdg-bch}} \left( -\frac{f}{-be+af} + \frac{1}{a+bx} \right) \right.$$

$$\left. \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{\frac{f}{-be+af} - \frac{h}{-bg+ah}}} \left( \left( (bdg-bch) \text{EllipticE} \left[ \right. \right. \right. \right.$$

$$\left. \left. \left. \left. \text{ArcSin} \left[ \sqrt{\frac{(be-af) \left( h + \frac{bg}{a+bx} - \frac{ah}{a+bx} \right)}{b(-fg+eh)}} \right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right) \right. \right.$$

$$\left. \left. \left. \left. \left( (bc-ad)(bg-ah) \right) \right) \right) - \frac{1}{-bc+ad} d \text{EllipticF} \left[ \text{ArcSin} \left[ \right. \right. \right. \right.$$

$$\left. \left. \left. \left. \sqrt{\frac{(be-af) \left( h + \frac{bg}{a+bx} - \frac{ah}{a+bx} \right)}{b(-fg+eh)}} \right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right) \right) \right) /$$

$$\left( \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \sqrt{\left( d + \frac{bc-ad}{a+bx} \right) \left( f + \frac{be-af}{a+bx} \right) \left( h + \frac{bg-ah}{a+bx} \right)} \right) +$$

$$\left( a^2bCd eh \sqrt{\frac{(bc-ad)(bg-ah) \left( -\frac{d}{-bc+ad} + \frac{1}{a+bx} \right)}{bdg-bch}} \left( -\frac{f}{-be+af} + \frac{1}{a+bx} \right) \right.$$

$$\left. \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{\frac{f}{-be+af} - \frac{h}{-bg+ah}}} \left( \left( (bdg-bch) \text{EllipticE} \left[ \right. \right. \right. \right.$$

$$\left. \left. \left. \left. \text{ArcSin} \left[ \sqrt{\frac{(be-af) \left( h + \frac{bg}{a+bx} - \frac{ah}{a+bx} \right)}{b(-fg+eh)}} \right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right) \right) \right) /$$

$$\begin{aligned}
 & \left( (bc-ad)(bg-ah) \right) - \frac{1}{-bc+ad} d \text{EllipticF} \left[ \text{ArcSin} \left[ \sqrt{\frac{(be-af) \left( h + \frac{bg}{a+bx} - \frac{ah}{a+bx} \right)}{b(-fg+eh)}}, \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right] / \\
 & \left( \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \sqrt{\left( d + \frac{bc-ad}{a+bx} \right) \left( f + \frac{be-af}{a+bx} \right) \left( h + \frac{bg-ah}{a+bx} \right)} \right) + \\
 & \left( a^2 b c c f h \sqrt{\frac{(bc-ad)(bg-ah) \left( -\frac{d}{-bc+ad} + \frac{1}{a+bx} \right)}{bdg-bch}} \left( -\frac{f}{-be+af} + \frac{1}{a+bx} \right) \right. \\
 & \left. \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{\frac{f}{-be+af} - \frac{h}{-bg+ah}}} \left( \left( (bdg-bch) \text{EllipticE} \left[ \text{ArcSin} \left[ \sqrt{\frac{(be-af) \left( h + \frac{bg}{a+bx} - \frac{ah}{a+bx} \right)}{b(-fg+eh)}}, \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right] \right) / \right. \right. \\
 & \left. \left. (bc-ad)(bg-ah) \right) - \frac{1}{-bc+ad} d \text{EllipticF} \left[ \text{ArcSin} \left[ \sqrt{\frac{(be-af) \left( h + \frac{bg}{a+bx} - \frac{ah}{a+bx} \right)}{b(-fg+eh)}}, \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right] / \right. \\
 & \left. \left( \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \sqrt{\left( d + \frac{bc-ad}{a+bx} \right) \left( f + \frac{be-af}{a+bx} \right) \left( h + \frac{bg-ah}{a+bx} \right)} \right) - \\
 & \left( a^3 C d f h \sqrt{\frac{(bc-ad)(bg-ah) \left( -\frac{d}{-bc+ad} + \frac{1}{a+bx} \right)}{bdg-bch}} \left( -\frac{f}{-be+af} + \frac{1}{a+bx} \right) \right. \\
 & \left. \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{\frac{f}{-be+af} - \frac{h}{-bg+ah}}} \left( \left( (bdg-bch) \text{EllipticE} \left[ \right. \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left. \text{ArcSin} \left[ \sqrt{\frac{(be-af) \left( h + \frac{bg}{a+bx} - \frac{ah}{a+bx} \right)}{b(-fg+eh)}}, \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right/ \\
 & \left. \left( (bc-ad)(bg-ah) \right) - \frac{1}{-bc+ad} d \text{EllipticF} \left[ \text{ArcSin} \left[ \sqrt{\frac{(be-af) \left( h + \frac{bg}{a+bx} - \frac{ah}{a+bx} \right)}{b(-fg+eh)}}, \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right] \right/ \\
 & \left( \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \sqrt{\left( d + \frac{bc-ad}{a+bx} \right) \left( f + \frac{be-af}{a+bx} \right) \left( h + \frac{bg-ah}{a+bx} \right)} \right) + \\
 & \left( 2Ab^2dfh \sqrt{\frac{-\frac{d}{-bc+ad} + \frac{1}{a+bx}}{-\frac{d}{-bc+ad} + \frac{h}{-bg+ah}}} \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \left( -\frac{h}{-bg+ah} + \frac{1}{a+bx} \right) \right) \\
 & \left. \text{EllipticF} \left[ \text{ArcSin} \left[ \sqrt{\frac{(-be+af) \left( -h - \frac{bg}{a+bx} + \frac{ah}{a+bx} \right)}{b(-fg+eh)}}, \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right] \right/ \\
 & \left( \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{\frac{f}{-be+af} - \frac{h}{-bg+ah}}} \sqrt{\left( d + \frac{bc-ad}{a+bx} \right) \left( f + \frac{be-af}{a+bx} \right) \left( h + \frac{bg-ah}{a+bx} \right)} \right) + \\
 & \left( 2a^2Cdfh \sqrt{\frac{-\frac{d}{-bc+ad} + \frac{1}{a+bx}}{-\frac{d}{-bc+ad} + \frac{h}{-bg+ah}}} \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \left( -\frac{h}{-bg+ah} + \frac{1}{a+bx} \right) \right) \\
 & \left. \text{EllipticF} \left[ \text{ArcSin} \left[ \sqrt{\frac{(-be+af) \left( -h - \frac{bg}{a+bx} + \frac{ah}{a+bx} \right)}{b(-fg+eh)}}, \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right] \right/ \\
 & \left( \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{\frac{f}{-be+af} - \frac{h}{-bg+ah}}} \sqrt{\left( d + \frac{bc-ad}{a+bx} \right) \left( f + \frac{be-af}{a+bx} \right) \left( h + \frac{bg-ah}{a+bx} \right)} \right) + \\
 & \left( bCde(-bg+ah) \left( -\frac{f}{-be+af} + \frac{h}{-bg+ah} \right) \sqrt{\frac{-\frac{d}{-bc+ad} + \frac{1}{a+bx}}{-\frac{d}{-bc+ad} + \frac{h}{-bg+ah}}} \right)
 \end{aligned}$$

$$\begin{aligned}
 & \sqrt{-\frac{\left(-\frac{f}{-be+af} + \frac{1}{a+bx}\right) \left(-\frac{h}{-bg+ah} + \frac{1}{a+bx}\right)}{\left(-\frac{f}{-be+af} + \frac{h}{-bg+ah}\right)^2}} \operatorname{EllipticPi}\left[-\frac{-bfg+beh}{(-be+af)h}, \right. \\
 & \left. \operatorname{ArcSin}\left[\sqrt{\frac{(-be+af)\left(-h-\frac{bg}{a+bx} + \frac{ah}{a+bx}\right)}{b(-fg+eh)}}, \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)}\right]\right] / \\
 & \left(\sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right) \left(h + \frac{bg-ah}{a+bx}\right)}\right) + \\
 & \left(bccf(-bg+ah) \left(-\frac{f}{-be+af} + \frac{h}{-bg+ah}\right) \sqrt{\frac{-\frac{d}{-bc+ad} + \frac{1}{a+bx}}{-\frac{d}{-bc+ad} + \frac{h}{-bg+ah}}}}\right) \\
 & \sqrt{-\frac{\left(-\frac{f}{-be+af} + \frac{1}{a+bx}\right) \left(-\frac{h}{-bg+ah} + \frac{1}{a+bx}\right)}{\left(-\frac{f}{-be+af} + \frac{h}{-bg+ah}\right)^2}} \operatorname{EllipticPi}\left[-\frac{-bfg+beh}{(-be+af)h}, \right. \\
 & \left. \operatorname{ArcSin}\left[\sqrt{\frac{(-be+af)\left(-h-\frac{bg}{a+bx} + \frac{ah}{a+bx}\right)}{b(-fg+eh)}}, \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)}\right]\right] / \\
 & \left(\sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right) \left(h + \frac{bg-ah}{a+bx}\right)}\right) + \\
 & \left(acdf(-bg+ah) \left(-\frac{f}{-be+af} + \frac{h}{-bg+ah}\right) \sqrt{\frac{-\frac{d}{-bc+ad} + \frac{1}{a+bx}}{-\frac{d}{-bc+ad} + \frac{h}{-bg+ah}}}}\right) \\
 & \sqrt{-\frac{\left(-\frac{f}{-be+af} + \frac{1}{a+bx}\right) \left(-\frac{h}{-bg+ah} + \frac{1}{a+bx}\right)}{\left(-\frac{f}{-be+af} + \frac{h}{-bg+ah}\right)^2}} \operatorname{EllipticPi}\left[-\frac{-bfg+beh}{(-be+af)h}, \right. \\
 & \left. \operatorname{ArcSin}\left[\sqrt{\frac{(-be+af)\left(-h-\frac{bg}{a+bx} + \frac{ah}{a+bx}\right)}{b(-fg+eh)}}, \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)}\right]\right] / \\
 & \left(\sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right) \left(h + \frac{bg-ah}{a+bx}\right)}\right) +
 \end{aligned}$$

$$\left( b C d f g (-b g + a h) \left( -\frac{f}{-b e + a f} + \frac{h}{-b g + a h} \right) \sqrt{\frac{-\frac{d}{-b c + a d} + \frac{1}{a + b x}}{-\frac{d}{-b c + a d} + \frac{h}{-b g + a h}}} \right. \\ \left. \sqrt{-\frac{\left( -\frac{f}{-b e + a f} + \frac{1}{a + b x} \right) \left( -\frac{h}{-b g + a h} + \frac{1}{a + b x} \right)}{\left( -\frac{f}{-b e + a f} + \frac{h}{-b g + a h} \right)^2}} \text{EllipticPi} \left[ -\frac{-b f g + b e h}{(-b e + a f) h}, \right. \right. \\ \left. \left. \text{ArcSin} \left[ \sqrt{\frac{(-b e + a f) \left( -h - \frac{b g}{a + b x} + \frac{a h}{a + b x} \right)}{b (-f g + e h)}}, \frac{(-b c + a d) (-f g + e h)}{(-b e + a f) (-d g + c h)} \right] \right] \right) / \\ \left( h \sqrt{\left( d + \frac{b c - a d}{a + b x} \right) \left( f + \frac{b e - a f}{a + b x} \right) \left( h + \frac{b g - a h}{a + b x} \right)} \right) \right)$$

**Problem 34: Result more than twice size of optimal antiderivative.**

$$\int \frac{A + C x^2}{(a + b x)^{3/2} \sqrt{c + d x} \sqrt{e + f x} \sqrt{g + h x}} dx$$

Optimal (type 4, 867 leaves, 9 steps):

$$\begin{aligned}
 & \frac{2 (A b^2 + a^2 C) d \sqrt{a+bx} \sqrt{e+fx} \sqrt{g+hx}}{b (bc-ad) (be-af) (bg-ah) \sqrt{c+dx}} - \frac{2 (A b^2 + a^2 C) \sqrt{c+dx} \sqrt{e+fx} \sqrt{g+hx}}{(bc-ad) (be-af) (bg-ah) \sqrt{a+bx}} - \\
 & \left( 2 (A b^2 + a^2 C) \sqrt{dg-ch} \sqrt{fg-eh} \sqrt{a+bx} \sqrt{-\frac{(de-cf)(g+hx)}{(fg-eh)(c+dx)}} \right. \\
 & \quad \left. \text{EllipticE}\left[\text{ArcSin}\left[\frac{\sqrt{dg-ch} \sqrt{e+fx}}{\sqrt{fg-eh} \sqrt{c+dx}}\right], \frac{(bc-ad)(fg-eh)}{(be-af)(dg-ch)}\right] \right) / \\
 & \left( b (bc-ad) (be-af) (bg-ah) \sqrt{\frac{(de-cf)(a+bx)}{(be-af)(c+dx)}} \sqrt{g+hx} \right) - \\
 & \left( 2 (2abcC + Ab^2d - a^2Cd) \sqrt{\frac{(be-af)(c+dx)}{(de-cf)(a+bx)}} \sqrt{g+hx} \right. \\
 & \quad \left. \text{EllipticF}\left[\text{ArcSin}\left[\frac{\sqrt{bg-ah} \sqrt{e+fx}}{\sqrt{fg-eh} \sqrt{a+bx}}\right], -\frac{(bc-ad)(fg-eh)}{(de-cf)(bg-ah)}\right] \right) / \\
 & \left( b^2 (bc-ad) \sqrt{bg-ah} \sqrt{fg-eh} \sqrt{c+dx} \sqrt{-\frac{(be-af)(g+hx)}{(fg-eh)(a+bx)}} \right) + \\
 & \left( 2C \sqrt{-dg+ch} (a+bx) \sqrt{\frac{(bg-ah)(c+dx)}{(dg-ch)(a+bx)}} \sqrt{\frac{(bg-ah)(e+fx)}{(fg-eh)(a+bx)}} \text{EllipticPi}\left[-\frac{b(dg-ch)}{(bc-ad)h}, \right. \right. \\
 & \quad \left. \left. \text{ArcSin}\left[\frac{\sqrt{bc-ad} \sqrt{g+hx}}{\sqrt{-dg+ch} \sqrt{a+bx}}\right], \frac{(be-af)(dg-ch)}{(bc-ad)(fg-eh)}\right] \right) / (b^2 \sqrt{bc-ad} h \sqrt{c+dx} \sqrt{e+fx})
 \end{aligned}$$

Result (type 4, 2103 leaves):

$$\begin{aligned}
 & \frac{2 (A b^2 + a^2 C) \sqrt{c+dx} \sqrt{e+fx} \sqrt{g+hx}}{(bc-ad) (be-af) (bg-ah) \sqrt{a+bx}} + \frac{1}{b^3 (-bc+ad) (-be+af) (-bg+ah)} \\
 & 2 \left( \left( (-A b^2 - a^2 C) (a+bx)^{5/2} \left( d + \frac{bc}{a+bx} - \frac{ad}{a+bx} \right) \left( f + \frac{be}{a+bx} - \frac{af}{a+bx} \right) \left( h + \frac{bg}{a+bx} - \frac{ah}{a+bx} \right) \right) / \right. \\
 & \quad \left. \left( \sqrt{c + \frac{(a+bx) \left( d - \frac{ad}{a+bx} \right)}{b}} \sqrt{e + \frac{(a+bx) \left( f - \frac{af}{a+bx} \right)}{b}} \sqrt{g + \frac{(a+bx) \left( h - \frac{ah}{a+bx} \right)}{b}} \right) + \right.
 \end{aligned}$$

$$\begin{aligned}
 & \frac{1}{\sqrt{c + \frac{(a+bx)(d-\frac{ad}{a+bx})}{b}} \sqrt{e + \frac{(a+bx)(f-\frac{af}{a+bx})}{b}} \sqrt{g + \frac{(a+bx)(h-\frac{ah}{a+bx})}{b}}} (bc-ad)(be-af) \\
 & (bg-ah)(a+bx)^{3/2} \sqrt{\left( \left( d + \frac{bc}{a+bx} - \frac{ad}{a+bx} \right) \left( f + \frac{be}{a+bx} - \frac{af}{a+bx} \right) \left( h + \frac{bg}{a+bx} - \frac{ah}{a+bx} \right) \right)} \\
 & \left( \left( A b^2 \sqrt{\frac{(bc-ad)(bg-ah)\left(-\frac{d}{-bc+ad} + \frac{1}{a+bx}\right)}{bdg-bch}} \left( -\frac{f}{-be+af} + \frac{1}{a+bx} \right) \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{\frac{f}{-be+af} - \frac{h}{-bg+ah}}} \right. \right. \right. \\
 & \left. \left. \left. - \left( (bdg-bch) \operatorname{EllipticE} \left[ \operatorname{ArcSin} \left[ \sqrt{\frac{(be-af)\left(h + \frac{bg}{a+bx} - \frac{ah}{a+bx}\right)}{b(-fg+eh)}} \right], \right. \right. \right. \right. \\
 & \left. \left. \left. \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right) / ((bc-ad)(bg-ah)) \right) - \right. \\
 & \left. \frac{1}{-bc+ad} d \operatorname{EllipticF} \left[ \operatorname{ArcSin} \left[ \sqrt{\frac{(be-af)\left(h + \frac{bg}{a+bx} - \frac{ah}{a+bx}\right)}{b(-fg+eh)}} \right], \right. \right. \\
 & \left. \left. \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right) \Bigg) / \\
 & \left( \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \sqrt{\left( d + \frac{bc-ad}{a+bx} \right) \left( f + \frac{be-af}{a+bx} \right) \left( h + \frac{bg-ah}{a+bx} \right)} \right) + \\
 & \left( a^2 c \sqrt{\frac{(bc-ad)(bg-ah)\left(-\frac{d}{-bc+ad} + \frac{1}{a+bx}\right)}{bdg-bch}} \left( -\frac{f}{-be+af} + \frac{1}{a+bx} \right) \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{\frac{f}{-be+af} - \frac{h}{-bg+ah}}} \right. \right. \\
 & \left. \left. \left. - \left( (bdg-bch) \operatorname{EllipticE} \left[ \operatorname{ArcSin} \left[ \sqrt{\frac{(be-af)\left(h + \frac{bg}{a+bx} - \frac{ah}{a+bx}\right)}{b(-fg+eh)}} \right], \right. \right. \right. \right. \\
 & \left. \left. \left. \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right) / ((bc-ad)(bg-ah)) \right) - \right. \\
 & \left. \frac{1}{-bc+ad} d \operatorname{EllipticF} \left[ \operatorname{ArcSin} \left[ \sqrt{\frac{(be-af)\left(h + \frac{bg}{a+bx} - \frac{ah}{a+bx}\right)}{b(-fg+eh)}} \right], \right. \right.
 \end{aligned}$$

$$\left. \left. \left. \left. \left. \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right) \right) \right) \right) \Big/$$

$$\left( \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right) \left(h + \frac{bg-ah}{a+bx}\right)} \right) -$$

$$\left( 2ac \sqrt{\frac{-\frac{d}{-bc+ad} + \frac{1}{a+bx}}{-\frac{d}{-bc+ad} + \frac{h}{-bg+ah}}} \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \left(-\frac{h}{-bg+ah} + \frac{1}{a+bx}\right) \right)$$

$$\text{EllipticF}\left[\text{ArcSin}\left[\sqrt{\frac{(-be+af)\left(-h - \frac{bg}{a+bx} + \frac{ah}{a+bx}\right)}{b(-fg+eh)}}\right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)}\right] \Big/$$

$$\left( \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{-\frac{f}{-be+af} - \frac{h}{-bg+ah}}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right) \left(h + \frac{bg-ah}{a+bx}\right)} \right) -$$

$$\left( c(-bg+ah) \left(-\frac{f}{-be+af} + \frac{h}{-bg+ah}\right) \sqrt{\frac{-\frac{d}{-bc+ad} + \frac{1}{a+bx}}{-\frac{d}{-bc+ad} + \frac{h}{-bg+ah}}} \right)$$

$$\sqrt{-\frac{\left(-\frac{f}{-be+af} + \frac{1}{a+bx}\right)\left(-\frac{h}{-bg+ah} + \frac{1}{a+bx}\right)}{\left(-\frac{f}{-be+af} + \frac{h}{-bg+ah}\right)^2}} \text{EllipticPi}\left[-\frac{-bfg+beh}{(-be+af)h}, \right.$$

$$\left. \text{ArcSin}\left[\sqrt{\frac{(-be+af)\left(-h - \frac{bg}{a+bx} + \frac{ah}{a+bx}\right)}{b(-fg+eh)}}\right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)}\right] \Big/$$

$$\left( h \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right) \left(h + \frac{bg-ah}{a+bx}\right)} \right) \Big)$$

**Problem 35: Result more than twice size of optimal antiderivative.**

$$\int \frac{A+Cx^2}{(a+bx)^{5/2} \sqrt{c+dx} \sqrt{e+fx} \sqrt{g+hx}} dx$$

Optimal (type 4, 1070 leaves, 8 steps):

$$\begin{aligned}
 & - \left( \left( 4d (Ab^3 (deg+cfg+ceh) + a^3 C (dfg+deh+cfh) + \right. \right. \\
 & \quad \left. \left. a^2 b (3Adfh - 2C (deg+cfg+ceh)) - ab^2 (2Ad (fg+eh) - c (3Ceg - 2Afh)) \right) \right. \\
 & \quad \left. \sqrt{a+bx} \sqrt{e+fx} \sqrt{g+hx} \right) / \left( 3 (bc-ad)^2 (be-af)^2 (bg-ah)^2 \sqrt{c+dx} \right) - \\
 & \quad \frac{2 (Ab^2 + a^2 C) \sqrt{c+dx} \sqrt{e+fx} \sqrt{g+hx}}{3 (bc-ad) (be-af) (bg-ah) (a+bx)^{3/2}} + \\
 & \quad \left( 4b (Ab^3 (deg+cfg+ceh) + a^3 C (dfg+deh+cfh) + a^2 b (3Adfh - 2C (deg+cfg+ceh)) - \right. \\
 & \quad \left. ab^2 (2Ad (fg+eh) - c (3Ceg - 2Afh))) \sqrt{c+dx} \sqrt{e+fx} \sqrt{g+hx} \right) / \\
 & \quad \left( 3 (bc-ad)^2 (be-af)^2 (bg-ah)^2 \sqrt{a+bx} \right) + \left( 4 \sqrt{dg-ch} \sqrt{fg-eh} \right. \\
 & \quad \left. (Ab^3 (deg+cfg+ceh) + a^3 C (dfg+deh+cfh) + a^2 b (3Adfh - 2C (deg+cfg+ceh)) - \right. \\
 & \quad \left. ab^2 (2Ad (fg+eh) - c (3Ceg - 2Afh))) \sqrt{a+bx} \sqrt{-\frac{(de-cf)(g+hx)}{(fg-eh)(c+dx)}} \right. \\
 & \quad \left. \text{EllipticE} \left[ \text{ArcSin} \left[ \frac{\sqrt{dg-ch} \sqrt{e+fx}}{\sqrt{fg-eh} \sqrt{c+dx}} \right], \frac{(bc-ad)(fg-eh)}{(be-af)(dg-ch)} \right] \right) / \\
 & \quad \left( 3 (bc-ad)^2 (be-af)^2 (bg-ah)^2 \sqrt{\frac{(de-cf)(a+bx)}{(be-af)(c+dx)}} \sqrt{g+hx} \right) - \\
 & \quad \left( 2 (3ab (c^2 C + Ad^2) (fg+eh) - b^2 (2Ad^2 eg + Acd (fg+eh) + c^2 (3Ceg - Afh)) - \right. \\
 & \quad \left. a^2 (3Ad^2 fh - C (d^2 eg - cd fg - cdeh - 2c^2 fh))) \sqrt{\frac{(be-af)(c+dx)}{(de-cf)(a+bx)}} \right. \\
 & \quad \left. \sqrt{g+hx} \text{EllipticF} \left[ \text{ArcSin} \left[ \frac{\sqrt{bg-ah} \sqrt{e+fx}}{\sqrt{fg-eh} \sqrt{a+bx}} \right], -\frac{(bc-ad)(fg-eh)}{(de-cf)(bg-ah)} \right] \right) / \\
 & \quad \left( 3 (bc-ad)^2 (be-af) (bg-ah)^{3/2} \sqrt{fg-eh} \sqrt{c+dx} \sqrt{-\frac{(be-af)(g+hx)}{(fg-eh)(a+bx)}} \right)
 \end{aligned}$$

Result (type 4, 11160 leaves):

$$\begin{aligned}
 & \sqrt{a+bx} \sqrt{c+dx} \sqrt{e+fx} \sqrt{g+hx} \left( -\frac{2 (Ab^2 + a^2 C)}{3 (bc-ad) (be-af) (bg-ah) (a+bx)^2} + \right. \\
 & \quad \left( 4b (3ab^2 c C eg + Ab^3 deg - 2a^2 b C deg + Ab^3 c fg - 2a^2 bc C fg - 2aAb^2 d fg + a^3 C d fg + \right. \\
 & \quad \left. Ab^3 c eh - 2a^2 bc C eh - 2aAb^2 deh + a^3 C deh - 2aAb^2 cfh + a^3 c C fh + 3a^2 A b d fh) \right) / \\
 & \quad \left. \left( 3 (bc-ad)^2 (be-af)^2 (bg-ah)^2 (a+bx) \right) \right) + \frac{1}{3b^2 (-bc+ad)^2 (-be+af)^2 (-bg+ah)^2}
 \end{aligned}$$

$$\begin{aligned}
 & 2 \left( - \left( 2 (3 a b^2 c C e g + A b^3 d e g - 2 a^2 b C d e g + A b^3 c f g - 2 a^2 b c C f g - 2 a A b^2 d f g + a^3 C d f g + A \right. \right. \\
 & \quad \left. \left. b^3 c e h - 2 a^2 b c C e h - 2 a A b^2 d e h + a^3 C d e h - 2 a A b^2 c f h + a^3 c C f h + 3 a^2 A b d f h) \right. \right. \\
 & \quad \left. (a+b x)^{5/2} \left( d + \frac{b c}{a+b x} - \frac{a d}{a+b x} \right) \left( f + \frac{b e}{a+b x} - \frac{a f}{a+b x} \right) \left( h + \frac{b g}{a+b x} - \frac{a h}{a+b x} \right) \right) / \\
 & \quad \left( \sqrt{c + \frac{(a+b x) \left( d - \frac{a d}{a+b x} \right)}{b}} \sqrt{e + \frac{(a+b x) \left( f - \frac{a f}{a+b x} \right)}{b}} \sqrt{g + \frac{(a+b x) \left( h - \frac{a h}{a+b x} \right)}{b}} \right) + \\
 & \quad \frac{1}{\sqrt{c + \frac{(a+b x) \left( d - \frac{a d}{a+b x} \right)}{b}} \sqrt{e + \frac{(a+b x) \left( f - \frac{a f}{a+b x} \right)}{b}} \sqrt{g + \frac{(a+b x) \left( h - \frac{a h}{a+b x} \right)}{b}}} (b c - a d) (b e - a f) \\
 & \quad (b g - a h) (a+b x)^{3/2} \sqrt{\left( \left( d + \frac{b c}{a+b x} - \frac{a d}{a+b x} \right) \left( f + \frac{b e}{a+b x} - \frac{a f}{a+b x} \right) \left( h + \frac{b g}{a+b x} - \frac{a h}{a+b x} \right) \right)} \\
 & \quad \left( \left( 6 a b^2 c C e g \sqrt{\frac{(b c - a d) (b g - a h) \left( -\frac{d}{-b c + a d} + \frac{1}{a+b x} \right)}{b d g - b c h}} \right. \right. \\
 & \quad \left. \left( -\frac{f}{-b e + a f} + \frac{1}{a+b x} \right) \sqrt{\frac{-\frac{h}{-b g + a h} + \frac{1}{a+b x}}{\frac{f}{-b e + a f} - \frac{h}{-b g + a h}}} \left( - \left( (b d g - b c h) \text{EllipticE} \left[ \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \text{ArcSin} \left[ \sqrt{\frac{(b e - a f) \left( h + \frac{b g}{a+b x} - \frac{a h}{a+b x} \right)}{b (-f g + e h)}} \right], \frac{(-b c + a d) (-f g + e h)}{(-b e + a f) (-d g + c h)} \right] \right) \right) / \\
 & \quad \left. \left. \left. \left. (b c - a d) (b g - a h) \right) \right) - \frac{1}{-b c + a d} d \text{EllipticF} \left[ \text{ArcSin} \left[ \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \sqrt{\frac{(b e - a f) \left( h + \frac{b g}{a+b x} - \frac{a h}{a+b x} \right)}{b (-f g + e h)}} \right], \frac{(-b c + a d) (-f g + e h)}{(-b e + a f) (-d g + c h)} \right] \right) \right) / \\
 & \quad \left( \sqrt{\frac{-\frac{f}{-b e + a f} + \frac{1}{a+b x}}{-\frac{f}{-b e + a f} + \frac{h}{-b g + a h}}} \sqrt{\left( d + \frac{b c - a d}{a+b x} \right) \left( f + \frac{b e - a f}{a+b x} \right) \left( h + \frac{b g - a h}{a+b x} \right)} \right) +
 \end{aligned}$$

$$\begin{aligned}
 & \left( 2 A b^3 d e g \sqrt{\frac{(b c - a d) (b g - a h) \left(-\frac{d}{-b c + a d} + \frac{1}{a + b x}\right)}{b d g - b c h}} \left(-\frac{f}{-b e + a f} + \frac{1}{a + b x}\right) \right. \\
 & \left. \sqrt{\frac{-\frac{h}{-b g + a h} + \frac{1}{a + b x}}{\frac{f}{-b e + a f} - \frac{h}{-b g + a h}}} \left( \left( (b d g - b c h) \text{EllipticE} \left[ \right. \right. \right. \right. \\
 & \left. \left. \left. \left. \text{ArcSin} \left[ \sqrt{\frac{(b e - a f) \left(h + \frac{b g}{a + b x} - \frac{a h}{a + b x}\right)}{b (-f g + e h)}}, \frac{(-b c + a d) (-f g + e h)}{(-b e + a f) (-d g + c h)} \right] \right) \right) \right) / \\
 & \left. \left( (b c - a d) (b g - a h) \right) \right) - \frac{1}{-b c + a d} d \text{EllipticF} \left[ \text{ArcSin} \left[ \right. \right. \\
 & \left. \left. \sqrt{\frac{(b e - a f) \left(h + \frac{b g}{a + b x} - \frac{a h}{a + b x}\right)}{b (-f g + e h)}}, \frac{(-b c + a d) (-f g + e h)}{(-b e + a f) (-d g + c h)} \right] \right) \right) / \\
 & \left( \sqrt{\frac{-\frac{f}{-b e + a f} + \frac{1}{a + b x}}{-\frac{f}{-b e + a f} + \frac{h}{-b g + a h}}} \sqrt{\left(d + \frac{b c - a d}{a + b x}\right) \left(f + \frac{b e - a f}{a + b x}\right) \left(h + \frac{b g - a h}{a + b x}\right)} \right) - \\
 & \left( 4 a^2 b c d e g \sqrt{\frac{(b c - a d) (b g - a h) \left(-\frac{d}{-b c + a d} + \frac{1}{a + b x}\right)}{b d g - b c h}} \left(-\frac{f}{-b e + a f} + \frac{1}{a + b x}\right) \right. \\
 & \left. \sqrt{\frac{-\frac{h}{-b g + a h} + \frac{1}{a + b x}}{\frac{f}{-b e + a f} - \frac{h}{-b g + a h}}} \left( \left( (b d g - b c h) \text{EllipticE} \left[ \right. \right. \right. \right. \\
 & \left. \left. \left. \left. \text{ArcSin} \left[ \sqrt{\frac{(b e - a f) \left(h + \frac{b g}{a + b x} - \frac{a h}{a + b x}\right)}{b (-f g + e h)}}, \frac{(-b c + a d) (-f g + e h)}{(-b e + a f) (-d g + c h)} \right] \right) \right) \right) / \\
 & \left. \left( (b c - a d) (b g - a h) \right) \right) - \frac{1}{-b c + a d} d \text{EllipticF} \left[ \text{ArcSin} \left[ \right. \right. \\
 & \left. \left. \sqrt{\frac{(b e - a f) \left(h + \frac{b g}{a + b x} - \frac{a h}{a + b x}\right)}{b (-f g + e h)}}, \frac{(-b c + a d) (-f g + e h)}{(-b e + a f) (-d g + c h)} \right] \right) \right) /
 \end{aligned}$$

$$\begin{aligned}
 & \left( \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right) \left(h + \frac{bg-ah}{a+bx}\right)} \right) + \\
 & \left( 2Ab^3c f g \sqrt{\frac{(bc-ad)(bg-ah) \left(-\frac{d}{-bc+ad} + \frac{1}{a+bx}\right)}{bdg-bch}} \left(-\frac{f}{-be+af} + \frac{1}{a+bx}\right) \right. \\
 & \left. \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{-\frac{f}{-be+af} - \frac{h}{-bg+ah}}} \left( \left( (bdg-bch) \text{EllipticE} \left[ \right. \right. \right. \right. \\
 & \left. \left. \left. \left. \text{ArcSin} \left[ \sqrt{\frac{(be-af) \left(h + \frac{bg}{a+bx} - \frac{ah}{a+bx}\right)}{b(-fg+eh)}} \right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right) / \right. \right. \\
 & \left. \left. \left( (bc-ad)(bg-ah) \right) \right) - \frac{1}{-bc+ad} d \text{EllipticF} \left[ \text{ArcSin} \left[ \right. \right. \right. \right. \\
 & \left. \left. \left. \left. \sqrt{\frac{(be-af) \left(h + \frac{bg}{a+bx} - \frac{ah}{a+bx}\right)}{b(-fg+eh)}} \right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right) / \right. \\
 & \left. \left( \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right) \left(h + \frac{bg-ah}{a+bx}\right)} \right) - \\
 & \left( 4a^2bc C f g \sqrt{\frac{(bc-ad)(bg-ah) \left(-\frac{d}{-bc+ad} + \frac{1}{a+bx}\right)}{bdg-bch}} \left(-\frac{f}{-be+af} + \frac{1}{a+bx}\right) \right. \\
 & \left. \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{-\frac{f}{-be+af} - \frac{h}{-bg+ah}}} \left( \left( (bdg-bch) \text{EllipticE} \left[ \right. \right. \right. \right. \right. \\
 & \left. \left. \left. \left. \text{ArcSin} \left[ \sqrt{\frac{(be-af) \left(h + \frac{bg}{a+bx} - \frac{ah}{a+bx}\right)}{b(-fg+eh)}} \right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right) / \right. \\
 & \left. \left. \left( (bc-ad)(bg-ah) \right) \right) - \frac{1}{-bc+ad} d \text{EllipticF} \left[ \text{ArcSin} \left[ \right. \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left( \sqrt{\frac{(be-af) \left( h + \frac{bg}{a+bx} - \frac{ah}{a+bx} \right)}{b(-fg+eh)}}, \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right) / \\
 & \left( \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \sqrt{\left( d + \frac{bc-ad}{a+bx} \right) \left( f + \frac{be-af}{a+bx} \right) \left( h + \frac{bg-ah}{a+bx} \right)} \right) - \\
 & \left( 4aAb^2dfg \sqrt{\frac{(bc-ad)(bg-ah) \left( -\frac{d}{-bc+ad} + \frac{1}{a+bx} \right)}{bdg-bch}} \left( -\frac{f}{-be+af} + \frac{1}{a+bx} \right) \right. \\
 & \left. \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{\frac{f}{-be+af} - \frac{h}{-bg+ah}}} \left( \left( (bdg-bch) \text{EllipticE} \left[ \right. \right. \right. \right. \\
 & \left. \left. \left. \left. \text{ArcSin} \left[ \sqrt{\frac{(be-af) \left( h + \frac{bg}{a+bx} - \frac{ah}{a+bx} \right)}{b(-fg+eh)}}, \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right) \right) \right) / \\
 & \left( (bc-ad)(bg-ah) \right) \left. - \frac{1}{-bc+ad} d \text{EllipticF} \left[ \text{ArcSin} \left[ \right. \right. \right. \right. \right. \\
 & \left. \left. \left. \left. \sqrt{\frac{(be-af) \left( h + \frac{bg}{a+bx} - \frac{ah}{a+bx} \right)}{b(-fg+eh)}}, \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right) \right) \right) / \\
 & \left( \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \sqrt{\left( d + \frac{bc-ad}{a+bx} \right) \left( f + \frac{be-af}{a+bx} \right) \left( h + \frac{bg-ah}{a+bx} \right)} \right) + \\
 & \left( 2a^3Cdfg \sqrt{\frac{(bc-ad)(bg-ah) \left( -\frac{d}{-bc+ad} + \frac{1}{a+bx} \right)}{bdg-bch}} \left( -\frac{f}{-be+af} + \frac{1}{a+bx} \right) \right. \\
 & \left. \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{\frac{f}{-be+af} - \frac{h}{-bg+ah}}} \left( \left( (bdg-bch) \text{EllipticE} \left[ \right. \right. \right. \right. \right. \\
 & \left. \left. \left. \left. \text{ArcSin} \left[ \sqrt{\frac{(be-af) \left( h + \frac{bg}{a+bx} - \frac{ah}{a+bx} \right)}{b(-fg+eh)}}, \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right) \right) \right) \right) /
 \end{aligned}$$

$$\begin{aligned}
 & \left( (bc-ad)(bg-ah) \right) - \frac{1}{-bc+ad} d \operatorname{EllipticF} \left[ \operatorname{ArcSin} \left[ \sqrt{\frac{(be-af) \left( h + \frac{bg}{a+bx} - \frac{ah}{a+bx} \right)}{b(-fg+eh)}}, \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right] / \\
 & \left( \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \sqrt{\left( d + \frac{bc-ad}{a+bx} \right) \left( f + \frac{be-af}{a+bx} \right) \left( h + \frac{bg-ah}{a+bx} \right)} \right) + \\
 & \left( 2Ab^3ceh \sqrt{\frac{(bc-ad)(bg-ah) \left( -\frac{d}{-bc+ad} + \frac{1}{a+bx} \right)}{bdg-bch}} \left( -\frac{f}{-be+af} + \frac{1}{a+bx} \right) \right. \\
 & \left. \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{\frac{f}{-be+af} - \frac{h}{-bg+ah}}} \left( \left( (bdg-bch) \operatorname{EllipticE} \left[ \operatorname{ArcSin} \left[ \sqrt{\frac{(be-af) \left( h + \frac{bg}{a+bx} - \frac{ah}{a+bx} \right)}{b(-fg+eh)}}, \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right) \right) \right) / \\
 & \left( (bc-ad)(bg-ah) \right) - \frac{1}{-bc+ad} d \operatorname{EllipticF} \left[ \operatorname{ArcSin} \left[ \sqrt{\frac{(be-af) \left( h + \frac{bg}{a+bx} - \frac{ah}{a+bx} \right)}{b(-fg+eh)}}, \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right] / \\
 & \left( \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \sqrt{\left( d + \frac{bc-ad}{a+bx} \right) \left( f + \frac{be-af}{a+bx} \right) \left( h + \frac{bg-ah}{a+bx} \right)} \right) - \\
 & \left( 4a^2bcceh \sqrt{\frac{(bc-ad)(bg-ah) \left( -\frac{d}{-bc+ad} + \frac{1}{a+bx} \right)}{bdg-bch}} \left( -\frac{f}{-be+af} + \frac{1}{a+bx} \right) \right. \\
 & \left. \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{\frac{f}{-be+af} - \frac{h}{-bg+ah}}} \left( \left( (bdg-bch) \operatorname{EllipticE} \left[ \right. \right. \right) \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left. \text{ArcSin} \left[ \sqrt{\frac{(be-af) \left( h + \frac{bg}{a+bx} - \frac{ah}{a+bx} \right)}{b(-fg+eh)}}, \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right/ \\
 & \left. \left( (bc-ad)(bg-ah) \right) - \frac{1}{-bc+ad} d \text{EllipticF} \left[ \text{ArcSin} \left[ \sqrt{\frac{(be-af) \left( h + \frac{bg}{a+bx} - \frac{ah}{a+bx} \right)}{b(-fg+eh)}}, \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right] \right/ \\
 & \left( \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \sqrt{\left( d + \frac{bc-ad}{a+bx} \right) \left( f + \frac{be-af}{a+bx} \right) \left( h + \frac{bg-ah}{a+bx} \right)} \right) - \\
 & \left( 4aAb^2deh \sqrt{\frac{(bc-ad)(bg-ah) \left( -\frac{d}{-bc+ad} + \frac{1}{a+bx} \right)}{bdg-bch}} \left( -\frac{f}{-be+af} + \frac{1}{a+bx} \right) \right. \\
 & \left. \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{\frac{f}{-be+af} - \frac{h}{-bg+ah}}} \left( - \left( (bdg-bch) \text{EllipticE} \left[ \right. \right. \right. \right. \right. \\
 & \left. \left. \left. \left. \left. \text{ArcSin} \left[ \sqrt{\frac{(be-af) \left( h + \frac{bg}{a+bx} - \frac{ah}{a+bx} \right)}{b(-fg+eh)}}, \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right] \right) \right) \right/ \\
 & \left. \left( (bc-ad)(bg-ah) \right) - \frac{1}{-bc+ad} d \text{EllipticF} \left[ \text{ArcSin} \left[ \sqrt{\frac{(be-af) \left( h + \frac{bg}{a+bx} - \frac{ah}{a+bx} \right)}{b(-fg+eh)}}, \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)} \right] \right] \right) \right/ \\
 & \left( \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \sqrt{\left( d + \frac{bc-ad}{a+bx} \right) \left( f + \frac{be-af}{a+bx} \right) \left( h + \frac{bg-ah}{a+bx} \right)} \right) + \\
 & \left( 2a^3Cdeh \sqrt{\frac{(bc-ad)(bg-ah) \left( -\frac{d}{-bc+ad} + \frac{1}{a+bx} \right)}{bdg-bch}} \left( -\frac{f}{-be+af} + \frac{1}{a+bx} \right) \right)
 \end{aligned}$$

$$\begin{aligned}
 & \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{\frac{f}{-be+af} - \frac{h}{-bg+ah}}} \left( - \left( \left( (bdg - bch) \text{EllipticE} \left[ \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \left. \text{ArcSin} \left[ \sqrt{\frac{(be - af) \left( h + \frac{bg}{a+bx} - \frac{ah}{a+bx} \right)}{b(-fg + eh)}} \right], \frac{(-bc + ad)(-fg + eh)}{(-be + af)(-dg + ch)} \right] \right) / \right. \\
 & \quad \left. \left. \left. \left. (bc - ad)(bg - ah) \right) - \frac{1}{-bc + ad} d \text{EllipticF} \left[ \text{ArcSin} \left[ \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \left. \sqrt{\frac{(be - af) \left( h + \frac{bg}{a+bx} - \frac{ah}{a+bx} \right)}{b(-fg + eh)}} \right], \frac{(-bc + ad)(-fg + eh)}{(-be + af)(-dg + ch)} \right] \right] \right) / \right. \\
 & \quad \left. \left( \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \sqrt{\left( d + \frac{bc - ad}{a + bx} \right) \left( f + \frac{be - af}{a + bx} \right) \left( h + \frac{bg - ah}{a + bx} \right)} \right) - \right. \\
 & \quad \left. \left( 4aAb^2cfh \sqrt{\frac{(bc - ad)(bg - ah) \left( -\frac{d}{-bc + ad} + \frac{1}{a + bx} \right)}{bdg - bch}} \left( -\frac{f}{-be + af} + \frac{1}{a + bx} \right) \right) \right. \\
 & \quad \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{\frac{f}{-be+af} - \frac{h}{-bg+ah}}} \left( - \left( \left( (bdg - bch) \text{EllipticE} \left[ \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \left. \text{ArcSin} \left[ \sqrt{\frac{(be - af) \left( h + \frac{bg}{a+bx} - \frac{ah}{a+bx} \right)}{b(-fg + eh)}} \right], \frac{(-bc + ad)(-fg + eh)}{(-be + af)(-dg + ch)} \right] \right) / \right. \\
 & \quad \left. \left. \left. \left. (bc - ad)(bg - ah) \right) - \frac{1}{-bc + ad} d \text{EllipticF} \left[ \text{ArcSin} \left[ \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \left. \sqrt{\frac{(be - af) \left( h + \frac{bg}{a+bx} - \frac{ah}{a+bx} \right)}{b(-fg + eh)}} \right], \frac{(-bc + ad)(-fg + eh)}{(-be + af)(-dg + ch)} \right] \right] \right) / \right. \\
 & \quad \left. \left( \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \sqrt{\left( d + \frac{bc - ad}{a + bx} \right) \left( f + \frac{be - af}{a + bx} \right) \left( h + \frac{bg - ah}{a + bx} \right)} \right) + \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left( 2 a^3 c c f h \sqrt{\frac{(b c - a d) (b g - a h) \left(-\frac{d}{-b c + a d} + \frac{1}{a + b x}\right)}{b d g - b c h}} \left(-\frac{f}{-b e + a f} + \frac{1}{a + b x}\right) \right. \\
 & \sqrt{\frac{-\frac{h}{-b g + a h} + \frac{1}{a + b x}}{\frac{f}{-b e + a f} - \frac{h}{-b g + a h}}} \left( - \left( \left( (b d g - b c h) \text{EllipticE} \left[ \right. \right. \right. \right. \\
 & \left. \left. \left. \left. \text{ArcSin} \left[ \sqrt{\frac{(b e - a f) \left(h + \frac{b g}{a + b x} - \frac{a h}{a + b x}\right)}{b (-f g + e h)} \right], \frac{(-b c + a d) (-f g + e h)}{(-b e + a f) (-d g + c h)} \right] \right) \right) \right) / \\
 & \left. \left( (b c - a d) (b g - a h) \right) \right) - \frac{1}{-b c + a d} d \text{EllipticF} \left[ \text{ArcSin} \left[ \right. \right. \\
 & \left. \left. \sqrt{\frac{(b e - a f) \left(h + \frac{b g}{a + b x} - \frac{a h}{a + b x}\right)}{b (-f g + e h)} \right], \frac{(-b c + a d) (-f g + e h)}{(-b e + a f) (-d g + c h)} \right] \right) \right) / \\
 & \left( \sqrt{\frac{-\frac{f}{-b e + a f} + \frac{1}{a + b x}}{-\frac{f}{-b e + a f} + \frac{h}{-b g + a h}}} \sqrt{\left(d + \frac{b c - a d}{a + b x}\right) \left(f + \frac{b e - a f}{a + b x}\right) \left(h + \frac{b g - a h}{a + b x}\right)} \right) + \\
 & \left( 6 a^2 A b d f h \sqrt{\frac{(b c - a d) (b g - a h) \left(-\frac{d}{-b c + a d} + \frac{1}{a + b x}\right)}{b d g - b c h}} \left(-\frac{f}{-b e + a f} + \frac{1}{a + b x}\right) \right. \\
 & \sqrt{\frac{-\frac{h}{-b g + a h} + \frac{1}{a + b x}}{\frac{f}{-b e + a f} - \frac{h}{-b g + a h}}} \left( - \left( \left( (b d g - b c h) \text{EllipticE} \left[ \right. \right. \right. \right. \\
 & \left. \left. \left. \left. \text{ArcSin} \left[ \sqrt{\frac{(b e - a f) \left(h + \frac{b g}{a + b x} - \frac{a h}{a + b x}\right)}{b (-f g + e h)} \right], \frac{(-b c + a d) (-f g + e h)}{(-b e + a f) (-d g + c h)} \right] \right) \right) \right) / \\
 & \left. \left( (b c - a d) (b g - a h) \right) \right) - \frac{1}{-b c + a d} d \text{EllipticF} \left[ \text{ArcSin} \left[ \right. \right. \\
 & \left. \left. \sqrt{\frac{(b e - a f) \left(h + \frac{b g}{a + b x} - \frac{a h}{a + b x}\right)}{b (-f g + e h)} \right], \frac{(-b c + a d) (-f g + e h)}{(-b e + a f) (-d g + c h)} \right] \right) \right) /
 \end{aligned}$$

$$\begin{aligned}
 & \left( \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right) \left(h + \frac{bg-ah}{a+bx}\right)} \right) - \\
 & \left( 3b^2 c C e g \sqrt{\frac{-\frac{d}{-bc+ad} + \frac{1}{a+bx}}{-\frac{d}{-bc+ad} + \frac{h}{-bg+ah}}} \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \left(-\frac{h}{-bg+ah} + \frac{1}{a+bx}\right) \right. \\
 & \quad \left. \text{EllipticF}\left[\text{ArcSin}\left[\sqrt{\frac{(-be+af)\left(-h - \frac{bg}{a+bx} + \frac{ah}{a+bx}\right)}{b(-fg+eh)}}\right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)}\right] \right) / \\
 & \left( \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{\frac{f}{-be+af} - \frac{h}{-bg+ah}}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right) \left(h + \frac{bg-ah}{a+bx}\right)} \right) + \\
 & \left( 3ab C d e g \sqrt{\frac{-\frac{d}{-bc+ad} + \frac{1}{a+bx}}{-\frac{d}{-bc+ad} + \frac{h}{-bg+ah}}} \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \left(-\frac{h}{-bg+ah} + \frac{1}{a+bx}\right) \right. \\
 & \quad \left. \text{EllipticF}\left[\text{ArcSin}\left[\sqrt{\frac{(-be+af)\left(-h - \frac{bg}{a+bx} + \frac{ah}{a+bx}\right)}{b(-fg+eh)}}\right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)}\right] \right) / \\
 & \left( \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{\frac{f}{-be+af} - \frac{h}{-bg+ah}}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right) \left(h + \frac{bg-ah}{a+bx}\right)} \right) + \\
 & \left( 3ab c C f g \sqrt{\frac{-\frac{d}{-bc+ad} + \frac{1}{a+bx}}{-\frac{d}{-bc+ad} + \frac{h}{-bg+ah}}} \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \left(-\frac{h}{-bg+ah} + \frac{1}{a+bx}\right) \right. \\
 & \quad \left. \text{EllipticF}\left[\text{ArcSin}\left[\sqrt{\frac{(-be+af)\left(-h - \frac{bg}{a+bx} + \frac{ah}{a+bx}\right)}{b(-fg+eh)}}\right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)}\right] \right) / \\
 & \left( \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{\frac{f}{-be+af} - \frac{h}{-bg+ah}}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right) \left(h + \frac{bg-ah}{a+bx}\right)} \right) + \\
 & \left( Ab^2 d f g \sqrt{\frac{-\frac{d}{-bc+ad} + \frac{1}{a+bx}}{-\frac{d}{-bc+ad} + \frac{h}{-bg+ah}}} \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-\frac{f}{-be+af} + \frac{h}{-bg+ah}}} \left(-\frac{h}{-bg+ah} + \frac{1}{a+bx}\right) \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left. \text{EllipticF}\left[\text{ArcSin}\left[\sqrt{\frac{(-be+af)\left(-h-\frac{bg}{a+bx}+\frac{ah}{a+bx}\right)}{b(-fg+eh)}}\right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)}\right]\right) / \\
 & \left(\sqrt{\frac{-\frac{h}{-bg+ah}+\frac{1}{a+bx}}{\frac{f}{-be+af}-\frac{h}{-bg+ah}}}\sqrt{\left(d+\frac{bc-ad}{a+bx}\right)\left(f+\frac{be-af}{a+bx}\right)\left(h+\frac{bg-ah}{a+bx}\right)}\right) - \\
 & \left(2a^2Cdfg\sqrt{\frac{-\frac{d}{-bc+ad}+\frac{1}{a+bx}}{-\frac{d}{-bc+ad}+\frac{h}{-bg+ah}}}\sqrt{\frac{-\frac{f}{-be+af}+\frac{1}{a+bx}}{-\frac{f}{-be+af}+\frac{h}{-bg+ah}}}\left(-\frac{h}{-bg+ah}+\frac{1}{a+bx}\right)\right) \\
 & \left. \text{EllipticF}\left[\text{ArcSin}\left[\sqrt{\frac{(-be+af)\left(-h-\frac{bg}{a+bx}+\frac{ah}{a+bx}\right)}{b(-fg+eh)}}\right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)}\right]\right) / \\
 & \left(\sqrt{\frac{-\frac{h}{-bg+ah}+\frac{1}{a+bx}}{\frac{f}{-be+af}-\frac{h}{-bg+ah}}}\sqrt{\left(d+\frac{bc-ad}{a+bx}\right)\left(f+\frac{be-af}{a+bx}\right)\left(h+\frac{bg-ah}{a+bx}\right)}\right) + \\
 & \left(3abcCeh\sqrt{\frac{-\frac{d}{-bc+ad}+\frac{1}{a+bx}}{-\frac{d}{-bc+ad}+\frac{h}{-bg+ah}}}\sqrt{\frac{-\frac{f}{-be+af}+\frac{1}{a+bx}}{-\frac{f}{-be+af}+\frac{h}{-bg+ah}}}\left(-\frac{h}{-bg+ah}+\frac{1}{a+bx}\right)\right) \\
 & \left. \text{EllipticF}\left[\text{ArcSin}\left[\sqrt{\frac{(-be+af)\left(-h-\frac{bg}{a+bx}+\frac{ah}{a+bx}\right)}{b(-fg+eh)}}\right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)}\right]\right) / \\
 & \left(\sqrt{\frac{-\frac{h}{-bg+ah}+\frac{1}{a+bx}}{\frac{f}{-be+af}-\frac{h}{-bg+ah}}}\sqrt{\left(d+\frac{bc-ad}{a+bx}\right)\left(f+\frac{be-af}{a+bx}\right)\left(h+\frac{bg-ah}{a+bx}\right)}\right) + \\
 & \left(Ab^2deh\sqrt{\frac{-\frac{d}{-bc+ad}+\frac{1}{a+bx}}{-\frac{d}{-bc+ad}+\frac{h}{-bg+ah}}}\sqrt{\frac{-\frac{f}{-be+af}+\frac{1}{a+bx}}{-\frac{f}{-be+af}+\frac{h}{-bg+ah}}}\left(-\frac{h}{-bg+ah}+\frac{1}{a+bx}\right)\right) \\
 & \left. \text{EllipticF}\left[\text{ArcSin}\left[\sqrt{\frac{(-be+af)\left(-h-\frac{bg}{a+bx}+\frac{ah}{a+bx}\right)}{b(-fg+eh)}}\right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)}\right]\right) / \\
 & \left(\sqrt{\frac{-\frac{h}{-bg+ah}+\frac{1}{a+bx}}{\frac{f}{-be+af}-\frac{h}{-bg+ah}}}\sqrt{\left(d+\frac{bc-ad}{a+bx}\right)\left(f+\frac{be-af}{a+bx}\right)\left(h+\frac{bg-ah}{a+bx}\right)}\right) -
 \end{aligned}$$

$$\left( 2 a^2 C d e h \sqrt{\frac{-\frac{d}{-bc+ad} + \frac{1}{a+bx}}{-bc+ad} + \frac{h}{-bg+ah}} \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-be+af} + \frac{h}{-bg+ah}} \left( -\frac{h}{-bg+ah} + \frac{1}{a+bx} \right) \right. \\ \left. \text{EllipticF}\left[\text{ArcSin}\left[\sqrt{\frac{(-be+af)\left(-h - \frac{bg}{a+bx} + \frac{ah}{a+bx}\right)}{b(-fg+eh)}}\right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)}\right] \right) /$$

$$\left( \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{-be+af} - \frac{h}{-bg+ah}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right) \left(h + \frac{bg-ah}{a+bx}\right)} \right) +$$

$$\left( A b^2 c f h \sqrt{\frac{-\frac{d}{-bc+ad} + \frac{1}{a+bx}}{-bc+ad} + \frac{h}{-bg+ah}} \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-be+af} + \frac{h}{-bg+ah}} \left( -\frac{h}{-bg+ah} + \frac{1}{a+bx} \right) \right.$$

$$\left. \text{EllipticF}\left[\text{ArcSin}\left[\sqrt{\frac{(-be+af)\left(-h - \frac{bg}{a+bx} + \frac{ah}{a+bx}\right)}{b(-fg+eh)}}\right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)}\right] \right) /$$

$$\left( \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{-be+af} - \frac{h}{-bg+ah}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right) \left(h + \frac{bg-ah}{a+bx}\right)} \right) -$$

$$\left( 2 a^2 c C f h \sqrt{\frac{-\frac{d}{-bc+ad} + \frac{1}{a+bx}}{-bc+ad} + \frac{h}{-bg+ah}} \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-be+af} + \frac{h}{-bg+ah}} \left( -\frac{h}{-bg+ah} + \frac{1}{a+bx} \right) \right.$$

$$\left. \text{EllipticF}\left[\text{ArcSin}\left[\sqrt{\frac{(-be+af)\left(-h - \frac{bg}{a+bx} + \frac{ah}{a+bx}\right)}{b(-fg+eh)}}\right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)}\right] \right) /$$

$$\left( \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{-be+af} - \frac{h}{-bg+ah}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right) \left(h + \frac{bg-ah}{a+bx}\right)} \right) -$$

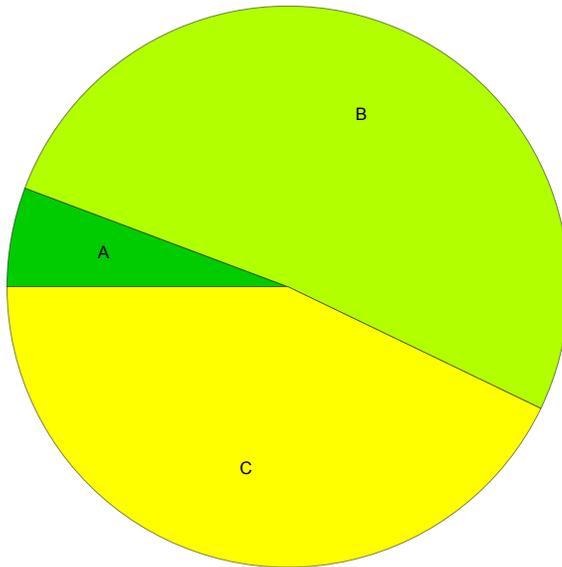
$$\left( 3 a A b d f h \sqrt{\frac{-\frac{d}{-bc+ad} + \frac{1}{a+bx}}{-bc+ad} + \frac{h}{-bg+ah}} \sqrt{\frac{-\frac{f}{-be+af} + \frac{1}{a+bx}}{-be+af} + \frac{h}{-bg+ah}} \left( -\frac{h}{-bg+ah} + \frac{1}{a+bx} \right) \right.$$

$$\left. \text{EllipticF}\left[\text{ArcSin}\left[\sqrt{\frac{(-be+af)\left(-h - \frac{bg}{a+bx} + \frac{ah}{a+bx}\right)}{b(-fg+eh)}}\right], \frac{(-bc+ad)(-fg+eh)}{(-be+af)(-dg+ch)}\right] \right) /$$

$$\left( \sqrt{\frac{-\frac{h}{-bg+ah} + \frac{1}{a+bx}}{\frac{f}{-be+af} - \frac{h}{-bg+ah}}} \sqrt{\left(d + \frac{bc-ad}{a+bx}\right) \left(f + \frac{be-af}{a+bx}\right) \left(h + \frac{bg-ah}{a+bx}\right)} \right)$$

## Summary of Integration Test Results

35 integration problems



A - 2 optimal antiderivatives

B - 18 more than twice size of optimal antiderivatives

C - 15 unnecessarily complex antiderivatives

D - 0 unable to integrate problems

E - 0 integration timeouts